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# Contents

1	Inti	roduction	5
	1.1	About our supplemental material	5
	1.2	Contributing authors	5
2	Dat	a Availability	7
	2.1	Source code	7
	2.2	Training and testing sets	7
	2.3	Experimental results	7
3	Sign	nalGP instruction set	9
	3.1	Default Instructions	10
	3.2	Problem-specific instructions	11
4	Loc	al compilation	13
5	Exp	ploitation rate diagnostic experiments	15
	5.1	Dependencies	15
	5.2	Setup	17
	5.3	Aggregate score	25
	5.4	Number unique individual selected	30
	5.5	Manuscript figures	31

4 CONTENTS

6	Cor	ntradictory objectives diagnostic	<b>43</b>					
	6.1	Dependencies	43					
	6.2	Setup	44					
	6.3	Population-wide satisfactory trait coverage	52					
	6.4	MRCA changes	56					
	6.5	Mean genotype deleterious steps	57					
	6.6	Mean genotype pairwise distance	57					
	6.7	Number unique individual selected	58					
	6.8	Manuscript figures	58					
7	Mu	Multi-path exploration diagnostic						
	7.1	Dependencies	63					
	7.2	Setup	64					
	7.3	Aggregate score	72					
	7.4	Manuscript figures	77					
8	Pro	gram synthesis experiments	81					
	8.1	Dependencies	81					
	8.2	Setup	82					
	8.3	Problem-solving success statistics	89					
	8.4	Average number of unique candidates selected	92					

# Introduction

This is not intended as a stand-alone document, but as a companion to our manuscript.

### 1.1 About our supplemental material

As you may have noticed (unless you're reading a pdf version of this), our supplemental material is hosted using GitHub pages. We compiled our data analyses and supplemental documentation into this nifty web-accessible book using bookdown.

The source code/configuration files for this supplemental material can be found in this GitHub repository.

Our supplemental material includes the following:

- Data availability (Section 2)
- Local compilation (Section 4)
- GP instruction set (Section 3)

### 1.2 Contributing authors

- Alexander Lalejini
- Marcos Sanson
- Jack Garbus
- Emily Dolson

# Data Availability

### 2.1 Source code

The source code for this work is publicly accessible on GitHub: https://github.com/amlalejini/GECCO-2024-phylogeny-informed-subsampling.

#### 2.1.1 Experiment software dependencies

- SignalGP: https://github.com/amlalejini/SignalGP
  - $\ commit\ hash:\ 114e0f07cb31370ab5191516679889e387cda73b$
- Empirical: https://github.com/devosoft/Empirical
  - $\ commit \ hash: \ 5955a1cae2a5de36aa3a65df060a56b38f575bd0$
- psb-cpp: https://github.com/amlalejini/psb-cpp
  - $\ commit\ hash:\ e49896b957574ccd2f9e6e97e812971a0aa77f4b$

## 2.2 Training and testing sets

The training and testing sets used for program synthesis problems can be found on GitHub:  $\label{eq:https://github.com/amlalejini/GECCO-2024-phylogeny-informed-subsampling/tree/main/experiments/2023-12-30-psynth/hpc/config.$ 

### 2.3 Experimental results

All of our experimental data is available online from our OSF respository: https://osf.io/h3f52/

# SignalGP instruction set

Below, we document the instruction set used in our GP system for our 2023 GPTP experiments.

#### Abbreviations:

- EOP: End of program
- Reg: local register
  - Reg[0] indicates the value at the register specified by an instruction's first argument, Reg[1] indicates the value at the register specified by an instruction's second argument, and Reg[2] indicates the value at the register specified by the instruction's third argument.
  - Reg[0], Reg[1], etc: Register 0, Register 1, etc.
- Input: input buffer
  - Follows same scheme as Reg
- Output: output buffer
  - Follows same scheme as Reg
- Global: global memory buffer
  - Follows same scheme as Reg
- Arg: Instruction argument
  - Arg[i] indicates the i'th instruction argument (an integer encoded in the genome)
  - E.g., Arg[0] is an instruction's first argument

Instructions that would produce undefined behavior (e.g., division by zero) are treated as no operations.

## 3.1 Default Instructions

I.e., instructions used across all diagnostic tasks.

Instruction	Arguments Used	Description
Nop	0	No operation
Not	1	Reg[0] = !Reg[0]
Inc	1	Reg[0] = Reg[0] + 1
Dec	1	Reg[0] = Reg[0] - 1
Add	3	Reg[2] = Reg[0] +
		Reg[1]
Sub	3	$\operatorname{Reg}[2] = \operatorname{Reg}[0] -$
26.1		$\operatorname{Reg}[1]$
Mult	3	$\operatorname{Reg}[2] = \operatorname{Reg}[0] *$
D.	9	$\operatorname{Reg}[1]$
Div	3	$\operatorname{Reg}[2] = \operatorname{Reg}[0] /$
Mad	3	$\operatorname{Reg}[1]$
Mod	3	Reg[2] = Reg[0] %  Reg[1]
Nand	2	$ \operatorname{Reg}[1] \\ \operatorname{Reg}[2] = !(\operatorname{Reg}[0] \&  $
rvand	2	Reg[2] = :(Reg[0] & Reg[1])
TestEqu	3	Reg[2] = Reg[0] ==
restEqu	· ·	$\operatorname{Reg}[1] = \operatorname{Reg}[0] = -$
TestNEqu	3	$\operatorname{Reg}[2] = \operatorname{Reg}[0] !=$
100011294	<u> </u>	$\operatorname{Reg}[1]$
TestLess	3	$\operatorname{Reg}[2] = \operatorname{Reg}[0] <$
		Reg[1]
TestLessEqu	3	$\operatorname{Reg}[2] = \operatorname{Reg}[0] <=$
-		Reg[1]
TestGreater	3	$\operatorname{Reg}[2] = \operatorname{Reg}[0] >$
		Reg[1]
TestGreaterEqu	3	$\operatorname{Reg}[2] = \operatorname{Reg}[0] >=$
		Reg[1]
SetMem	2	Reg[0] = Arg[1]
Terminal	1	Reg[0] = double value
		encoded by
C 3.5	2	instruction tag
CopyMem	$\frac{2}{2}$	$\operatorname{Reg}[0] = \operatorname{Reg}[1]$
SwapMem InputToWorking	$\frac{2}{2}$	Swap(Reg[0], Reg[1]) $Reg[1] = Input[0]$
InputToWorking WorkingToOutput	$\frac{2}{2}$	Reg[1] = Input[0]  Output[1] = Reg[0]
If	2 1	$ \begin{aligned} \text{Output}[1] &= \text{Reg}[0] \\ \text{If } \text{Reg}[0] &!= 0, \end{aligned} $
11	1	proceed. Otherwise
		skip to the next Close
		or EOP.
		or Lor.

Instruction	Arguments Used	Description
While	1	While $Reg[0] != 0$ ,
		loop. Otherwise skip
		to next Close or EOP.
Close	0	Indicate the end of a
		control block of code
		(e.g., loop, if).
Break	0	Break out of current
		control flow (e.g.,
		loop).
Call	0	Call a function, using
		this instruction's tag
		to determine which
		function is called.
Routine	0	Same as call, but local
		memory is shared.
		Sort of like a jump
		that will jump back
		when the routine
		ends.
Return	0	Return from the
		current function call.
WorkingToGlobal	2	Global[1] = Reg[0]
GlobalToWorking	2	Reg[1] = Global[0]
FullGlobalToWorking	0	Copy entire global
		memory buffer into
		working memory
		buffer
FullWorkingToGlobal	0	Copy entire working
		memory buffer into
		global memory buffer

Note that Nand performs a bitwise operation.

## 3.2 Problem-specific instructions

Each problem has problem-specific instructions for producing output.

### 3.2.1 Fizz Buzz

- SubmitFizz
- $\bullet$  SubmitBuzz

- $\bullet \quad SubmitFizzBuzz\\$
- $\bullet$  SubmitEcho

### 3.2.2 Median

• SubmitOutput

### **3.2.3** Grade

- SubmitA
- SubmitB
- SubmitC
- SubmitD
- SubmitF

### 3.2.4 Small or large

- SubmitSmall
- SubmitLarge
- SubmitNeither

# Local compilation

You will need a C++ compiler that supports at least C++17. We used g++13 for all local compilations.

First, clone GECCO-2024—phylogeny—informed—subsampling repository that contains the code needed to run our experiment software: https://github.com/amlalejini/GECCO-2024-phylogeny-informed-subsampling.

Once cloned, cd into your local GECCO-2024—phylogeny—informed—subsampling repository directory. Then, initialize and update all of the git submodules:

```
git submodule update —init —recursive
```

Once the submodules are updated, you should be able to compile either the diagnostics or program synthesis experiment code. To specify which experiment you would like to compile, adjust the PROJECT variable in the Makefile.

- PROJECT := prog\_synth for compiling the program synthesis code
- $\bullet$  PROJECT := diagnostics for compiling the selection scheme diagnostics code

To compile in debug mode, run make debug from repository directory, and to compile in release mode (all optimizations turned on), run make native.

If you get the following error:

```
third-party/Empirical/include/emp/matching/../../../third-party/robin-hood-hashing/src/include/robin_hood.h:54:14: fatal error: sys/auxv.h: No such file or directory
54 | # include <sys/auxv.h> // for getauxval
```

you can fix it by doing the following:

```
\begin{array}{ll} cd & third-party/Empirical/third-party/robin-hood-hashing \\ git & checkout & master \end{array}
```

Once you have an executable, you can generate a configuration file by running:

- ./diagnostics ——gen diagnostics.cfg

# Exploitation rate diagnostic experiments

```
experiment_slug <- "2023-12-28-phylo-sampling-diag"
working_directory <- paste0(
  "experiments/",
  experiment_slug,
  "/analysis/"
if (exists("bookdown_wd_prefix")) {
  working_directory <- paste0(
    bookdown_wd_prefix,
    working_directory
}
```

#### 5.1 **Dependencies**

3.4.4

## v ggplot2

```
library(tidyverse)
## — Attaching core tidyverse packages
      tidyverse 2.0.0 —
## v dplyr 1.1.4 v readr
## v forcats 1.0.0 v stringr
## v ggplot2 3.4.4 v tibble
                                                    2.1.4
                                                   1.5.1
```

3.2.1

v tibble

```
## v lubridate 1.9.3
                           v tidyr
                                       1.3.0
## v purrr
                1.0.2
## — Conflicts
     tidyverse_conflicts() —
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                     masks stats::lag()
## i Use the conflicted package (<a href="http://conflicted.r-lib">http://conflicted.r-lib</a>
    .org/>) to force all conflicts to become errors
library (cowplot)
##
## Attaching package: 'cowplot'
## The following object is masked from 'package:lubridate
##
##
       stamp
library (RColorBrewer)
library (khroma)
library (rstatix)
## Attaching package: 'rstatix'
## The following object is masked from 'package:stats':
##
##
        filter
library (knitr)
source ("https://gist.githubusercontent.com/benmarwick/2
    a1bb0133ff568cbe28d/raw/
    fb53bd97121f7f9ce947837ef1a4c65a73bffb3f/geom_flat_
    violin.R")
print(version)
##
## platform
                   aarch64-apple-darwin20
## arch
                   aarch64
## os
                   darwin20
## system
                   aarch64, darwin20
## status
## major
```

```
## minor 2.1
## year 2022
## month 06
## day 23
## svn rev 82513
## language R
## version.string R version 4.2.1 (2022-06-23)
## nickname Funny-Looking Kid
```

### 5.2 Setup

```
# Configure our default graphing theme
theme_set(theme_cowplot())
# Create a directory to store plots
plot_directory <- paste0(working_directory, "plots/")
dir.create(plot_directory, showWarnings=FALSE)
# Constants
focal_diagnostic <- "exploitation-rate"</pre>
```

### 5.2.1 Load experiment summary data

```
summary_data_loc <- paste0(working_directory, "data/</pre>
   aggregate.csv")
summary_data <- read_csv(summary_data_loc)</pre>
## Rows: 1080 Columns: 58
## — Column specification
## Delimiter: ","
## chr (5): DIAGNOSTIC, EVAL_FIT_EST_MODE, EVAL_MODE,
   SELECTION, STOP_MODE
## dbl (53): ACCURACY, CREDIT, DIAGNOSTIC_DIMENSIONALITY,
    EVAL_MAX_PHYLO_SEARCH...
## i Use 'spec()' to retrieve the full column
   specification for this data.
## i Specify the column types or set 'show_col_types =
   FALSE' to quiet this message.
summary data <- summary data %%
  mutate (
```

```
evals_per_gen = case_when(
   EVAL\_MODE = "cohort-full-compete" \sim 1.0 / NUM\_
       COHORTS,
   EVAL MODE == "cohort" ~ 1.0 / NUM COHORTS,
   EVAL_MODE == "down-sample" ~ TEST_DOWNSAMPLE_RATE,
   EVAL\_MODE == "full" \sim 1.0,
   EVAL_MODE == "indiv-rand-sample" ~ TEST_DOWNSAMPLE_
       RATE,
   EVAL_MODE == "phylo-informed-sample" ~ TEST_
       DOWNSAMPLE RATE
 EVAL_FIT_EST_MODE = case_when(
   EVAL\_FIT\_EST\_MODE == "ancestor-opt" \sim "ancestor",
   EVAL_FIT_EST_MODE == "relative-opt" ~ "relative",
    . default = EVAL\_FIT\_EST\_MODE
  ),
  .keep = "all"
) %>%
mutate (
 eval_label = case_when(
    # Clean up down-sample label
   EVAL_MODE == "down-sample" & EVAL_FIT_EST_MODE != "
       none" ~ paste("down-sample", EVAL FIT EST MODE,
       sep="-"),
    .default = EVAL\_MODE
 ),
) %>%
mutate (
 evals_per_gen = as.factor(evals_per_gen),
 DIAGNOSTIC = as.factor(DIAGNOSTIC),
 SELECTION = as.factor(SELECTION),
 EVAL MODE = as.factor(EVAL MODE),
 NUM_COHORTS = as.factor(NUM_COHORTS),
 TEST_DOWNSAMPLE_RATE = as.factor(TEST_DOWNSAMPLE_RATE
 EVAL\_FIT\_EST\_MODE = factor(
   EVAL_FIT_EST_MODE,
    levels = c(
      "none",
      "ancestor",
      "relative"
    ),
    labels = c(
      "None",
      "Ancestor",
      "Relative"
```

```
)
  )
# Grab just the exploitation rate data
exploit_summary_data <- filter(
  summary_data,
  DIAGNOSTIC == "exploitation-rate"
      Load experiment time series data
ts_data_loc <- paste0(working_directory, "data/time_
    series.csv")
\mathbf{ts\_data} \mathrel{<\!\!\!-} \mathbf{read\_csv} (\, \mathbf{ts\_data\_loc} \, )
## Rows: 108000 Columns: 28
## — Column specification
## Delimiter: ","
## chr (4): DIAGNOSTIC, EVAL_FIT_EST_MODE, EVAL_MODE,
   SELECTION
## dbl (24): NUM COHORTS, SEED, TEST DOWNSAMPLE RATE,
   ave_depth, deleterious_st...
##
## i Use 'spec()' to retrieve the full column
    specification for this data.
## i Specify the column types or set 'show_col_types =
   FALSE' to quiet this message.
ts\_data <\!\!- ts\_data \%\!\%
  mutate(
    evals_per_gen = case_when(
      EVAL\_MODE = "cohort-full-compete" \sim 1.0 / NUM\_
          COHORTS,
      EVAL\_MODE = "cohort" \sim 1.0 / NUM\_COHORTS,
      EVAL MODE == "down-sample" ~ TEST DOWNSAMPLE RATE,
      EVAL\_MODE == "full" \sim 1.0,
      EVAL_MODE == "indiv-rand-sample" ~ TEST_DOWNSAMPLE_
          RATE,
      EVAL_MODE == "phylo-informed-sample" ~ TEST_
          DOWNSAMPLE RATE
    EVAL_FIT_EST_MODE = case_when(
```

```
EVAL_FIT_EST_MODE == "ancestor-opt" ~ "ancestor",
      EVAL_FIT_EST_MODE == "relative-opt" ~ "relative",
      . default = EVAL\_FIT\_EST\_MODE
    ),
    . keep = "all"
  ) %>%
  mutate (
    eval_label = case_when(
      EVAL_MODE == "down-sample" & EVAL_FIT_EST_MODE != "
         none" ~ paste("down-sample", EVAL_FIT_EST_MODE,
         sep="-"),
      . default = EVAL\_MODE
  ) %>%
  mutate (
    evals_per_gen = as.factor(evals_per_gen),
    DIAGNOSTIC = as.factor(DIAGNOSTIC),
    SELECTION = as.factor(SELECTION),
    EVAL\_MODE = as.factor(EVAL\_MODE),
   NUM\_COHORTS = as.factor(NUM\_COHORTS),
    TEST_DOWNSAMPLE_RATE = as.factor(TEST_DOWNSAMPLE_RATE
       ),
    EVAL FIT EST MODE = factor(
      EVAL_FIT_EST_MODE,
      levels = c(
        "none",
        "ancestor"
        "relative"
      ),
      labels = c(
        "None",
        "Ancestor",
        "Relative"
# Grab just the exploitation rate data
exploit_ts_data <- ts_data %%
  filter (DIAGNOSTIC == "exploitation-rate")
Summarize time series data:
ts_summary_data <- ts_data %>%
  group by (SEED, DIAGNOSTIC, SELECTION, evals per gen,
     eval_label) %%
```

#### 5.2.3 Plotting helper functions

The following function assist with exploratory plotting of different measurements from summary and time series data. Note that for these plots, standard lexicase reference is rendered at equivalent number of generations (instead of evaluations).

```
build_plot_summary_data <- function(data, diagnostic,</pre>
   selection, response) {
  diag_data <- data %% filter (DIAGNOSTIC == diagnostic)
  full_median <- median(
    filter (
      diag_data,
      eval_label == "full" & SELECTION == selection
    ) [[response]]
  plot <- diag_data %%
    filter (
      eval_label != "full" & SELECTION == selection
    ) %>%
    ggplot (
      aes_string(
        x = "eval\_label",
        y = response,
        fill = "eval label"
    ) +
    geom_hline(
      yintercept = full_median,
      size = 1.0,
      alpha = 0.7,
```

```
color = "black",
      linetype="dashed"
    ) +
    geom_flat_violin(
      position = position\_nudge(x = .2, y = 0),
      alpha = .8,
      adjust = 1.5
    ) +
    geom_point(
      mapping = aes(color = eval_label),
      position = position_jitter(width = .15),
      size = .5,
      alpha = 0.8
    geom_boxplot(
      width = .1,
      outlier.shape = NA,
      alpha = 0.5
    ) +
    scale_y_continuous(
      \# \ limits = c(-0.5, 100)
    ) +
    scale_fill_bright() +
    scale_color_bright() +
    facet_grid(
      SELECTION ~ evals_per_gen,
      \# nrow = 2,
      labeller = label\_both
    ) +
    theme (
      legend.position = "none",
      axis.text.x = element\_text(
        angle = 30,
        hjust = 1
      panel.border = element_rect(color = "gray", size =
         2)
 return (plot)
build_plot_time_series_single_sampling <- function(
 data,
  diagnostic,
  selection,
```

```
sampling_level,
  response
) {
  diag_data <- data %% filter (
    DIAGNOSTIC = diagnostic &
   SELECTION = selection &
    evals_per_gen == sampling_level
  ) %>%
  mutate (
    sampling_level_label = sampling_level
  full_diag_data <- data %% filter(
   DIAGNOSTIC = diagnostic & SELECTION = selection &
       eval_label == "full"
  ) %>%
  mutate (
    \#\ Ensure\ that\ median\ line\ will\ sit\ in\ same\ facet
    sampling_level_label = sampling_level
  plot <- diag_data %%
    filter (
      eval_label != "full"
    ) %>%
    ggplot (
      aes_string(
        x = "ts\_step",
        \# x = "evaluations",
        y = \{\{ exponse \} \}
    ) +
    stat_summary(
      geom = "line",
      fun = mean,
      aes (
        color = eval_label
    ) +
    stat_summary(
      geom = "ribbon",
      fun.data = "mean_cl_boot",
      fun.args = list(conf.int = 0.95),
      alpha = 0.2,
      linetype = 0,
```

```
aes (
        color = eval_label,
        fill = eval\_label
      )
    ) +
    scale_fill_bright() +
    scale_color_bright() +
    # facet_wrap(
      \sim sampling\_level\_label,
    #
        n col = 1,
   #
        labeller = label both
    # ) +
    theme (
      legend.position = "right"
    ) +
    stat_summary(
      data = full_diag_data,
      geom = "line",
      fun = median,
      linetype = "dashed",
      color = "black"
    )
  return (plot)
build_plot_time_series <- function(</pre>
  data,
  diagnostic,
  selection,
 response
 \# Build 1% sampling plot and 10% sampling plot
 p_01 <- data %% build_plot_time_series_single_
     sampling (
    diagnostic,
    selection,
    "0.01",
    response
 p_10 <- data %% build_plot_time_series_single_sampling
    diagnostic,
    selection,
    "0.1",
    response
```

```
)
title <- ggdraw() +
  draw_label(
    pasteO(diagnostic, "u-u", selection),
    fontface = 'bold',
    x = 0,
    hjust = 0
  ) +
  theme (
    # add margin on the left of the drawing canvas,
    # so title is aligned with left edge of first plot
    \mathbf{plot}.\mathbf{margin} = \mathbf{margin}(0, 0, 0, 7)
plot <- plot_grid(</pre>
  title,
  \underline{p}_01 + labs(title = "1\% \cup subsampling") + theme(legend.
      position = "none"),
  p_10 + labs(title = "10% subsampling") + theme(legend
      .position = "bottom"),
  nrow = 3,
  ncol = 1,
  rel\_heights = c(0.075, 1, 1)
return(plot)
```

### 5.3 Aggregate score

#### 5.3.1 Final - Lexicase selection

```
p <- summary_data %% build_plot_summary_data(
    "exploitation-rate",
    "lexicase",
    "elite_true_agg_score"
)

## Warning: 'aes_string()' was deprecated in ggplot2
    3.0.0.
## i Please use tidy evaluation idioms with 'aes()'.
## i See also 'vignette("ggplot2-in-packages")' for more information.</pre>
```

```
## This warning is displayed once every 8 hours.
## Call 'lifecycle::last_lifecycle_warnings()' to see
   where this warning was generated.
## Warning: Using 'size' aesthetic for lines was
   deprecated in ggplot2 3.4.0.
## i Please use 'linewidth' instead.
## This warning is displayed once every 8 hours.
## Call 'lifecycle::last_lifecycle_warnings()' to see
   where this warning was generated.
## Warning: The 'size' argument of 'element_rect()' is
   deprecated as of ggplot2 3.4.0.
## i Please use the 'linewidth' argument instead.
## This warning is displayed once every 8 hours.
## Call 'lifecycle::last_lifecycle_warnings()' to see
   where this warning was generated.
ggsave (
  filename = paste0(plot_directory, "exploit-score-final-
     lex.pdf"),
  plot = p + labs(title = "Exploitation | rate | − Lexicase |
     selection"),
  width = 15.
  height = 10
## Warning: Using the 'size' aesthetic with geom_polygon
   was deprecated in ggplot2 3.4.0.
## i Please use the 'linewidth' aesthetic instead.
## This warning is displayed once every 8 hours.
## Call 'lifecycle::last_lifecycle_warnings()' to see
   where this warning was generated.
```

### 5.3.2 Final - Tournament selection

```
p <- summary_data %>% build_plot_summary_data(
   "exploitation-rate",
   "tournament",
   "elite_true_agg_score"
)
ggsave(
filename = paste0(plot_directory, "exploit-score-final-tourn.pdf"),
```

### 5.3.3 Statistical analysis

First, we'll create a table of median / mean values for easy reference.

DIAGNOSTIC	SELECTION	evals_per_gen	eval_label	score_median	score_mean	repl
exploitation-rate	lexicase	0.01	down-sample	9933.1800	9933.2455	
exploitation-rate	lexicase	0.01	down-sample-ancestor	920.1625	913.6102	
exploitation-rate	lexicase	0.01	indiv-rand-sample	2117.1200	2137.2725	
exploitation-rate	lexicase	0.01	phylo-informed-sample	2157.9350	2162.8605	
exploitation-rate	lexicase	0.1	down-sample	9967.3500	9968.1275	
exploitation-rate	lexicase	0.1	down-sample-ancestor	6976.3600	6985.9325	
exploitation-rate	lexicase	0.1	indiv-rand-sample	9360.5800	9360.2230	
exploitation-rate	lexicase	0.1	phylo-informed-sample	9301.3500	9308.4105	
exploitation-rate	lexicase	1	full	9981.7200	9982.2910	
exploitation-rate	tournament	0.01	down-sample	9650.1650	9650.6660	
exploitation-rate	tournament	0.01	down-sample-ancestor	1023.4150	1011.8228	
exploitation-rate	tournament	0.01	indiv-rand-sample	9969.7650	9969.2945	
exploitation-rate	tournament	0.01	phylo-informed-sample	9970.8950	9970.1455	
exploitation-rate	tournament	0.1	down-sample	9972.3050	9972.0210	
exploitation-rate	tournament	0.1	down-sample-ancestor	9988.9200	9988.9365	
exploitation-rate	tournament	0.1	indiv-rand-sample	9999.8250	9999.8240	
exploitation-rate	tournament	0.1	phylo-informed-sample	9999.7700	9999.7800	
exploitation-rate	tournament	1	full	10000.0000	10000.0000	

Next, we run a Kruskal-Wallis test to check for differences. For these tests, we only compare within a single subsampling level (evals\_per\_gen) and within the same selection scheme.

```
kw_test <- exploit_summary_data %%
filter(eval_label != "full") %%
group_by(SELECTION, evals_per_gen) %%
kruskal_test(elite_true_agg_score ~ eval_label) %%
mutate(sig = (p < 0.05)) %%
unite(
    "comparison_group",
    SELECTION,
    evals_per_gen,
    sep = "_",
    remove = FALSE
)
kable(kw_test)</pre>
```

$comparison\_group$	SELECTION	evals_per_gen	.y.	n	statistic	df	]
lexicase_0.01	lexicase	0.01	elite_true_agg_score	80	67.04167	3	
lexicase_0.1	lexicase	0.1	elite_true_agg_score	80	68.10074	3	(
tournament_0.01	tournament	0.01	elite_true_agg_score	80	66.76541	3	(
tournament_0.1	tournament	0.1	elite_true_agg_score	80	67.17274	3	(

Perform pairwise wilcoxon rank-sum tests for all significant comparison groups.

```
# Grab group names of significant comparisons
sig_kw_groups <- filter(kw_test, p < 0.05)$comparison_
wrs_test <- exploit_summary_data %%
  unite (
    "comparison_group",
    SELECTION,
    evals_per_gen,
    \mathrm{sep} = \overline{\ "} \overline{\ "},
    remove = FALSE
  ) %>%
  filter (
    eval_label != "full" & comparison_group %in% sig_kw_
        groups
  ) %>%
  group_by(SELECTION, evals_per_gen) %>%
  pairwise_wilcox_test(elite_true_agg_score ~ eval_label)
  adjust pvalue (method = "holm") %%
  add_significance("p.adj")
```

kable(wrs\_test)

SELECTION	evals_per_gen	.y.	group1	group2	n1
lexicase	0.01	elite_true_agg_score	down-sample	down-sample-ancestor	20
lexicase	0.01	elite_true_agg_score	down-sample	indiv-rand-sample	20
lexicase	0.01	elite_true_agg_score	down-sample	phylo-informed-sample	20
lexicase	0.01	elite_true_agg_score	down-sample-ancestor	indiv-rand-sample	20
lexicase	0.01	elite_true_agg_score	down-sample-ancestor	phylo-informed-sample	20
lexicase	0.01	elite_true_agg_score	indiv-rand-sample	phylo-informed-sample	20
lexicase	0.1	elite_true_agg_score	down-sample	down-sample-ancestor	20
lexicase	0.1	elite_true_agg_score	down-sample	indiv-rand-sample	20
lexicase	0.1	elite_true_agg_score	down-sample	phylo-informed-sample	20
lexicase	0.1	elite_true_agg_score	down-sample-ancestor	indiv-rand-sample	20
lexicase	0.1	elite_true_agg_score	down-sample-ancestor	phylo-informed-sample	20
lexicase	0.1	elite_true_agg_score	indiv-rand-sample	phylo-informed-sample	20
tournament	0.01	elite_true_agg_score	down-sample	down-sample-ancestor	20
tournament	0.01	elite_true_agg_score	down-sample	indiv-rand-sample	20
tournament	0.01	elite_true_agg_score	down-sample	phylo-informed-sample	20
tournament	0.01	elite_true_agg_score	down-sample-ancestor	indiv-rand-sample	20
tournament	0.01	elite_true_agg_score	down-sample-ancestor	phylo-informed-sample	20
tournament	0.01	elite_true_agg_score	indiv-rand-sample	phylo-informed-sample	20
tournament	0.1	elite_true_agg_score	down-sample	down-sample-ancestor	20
tournament	0.1	elite_true_agg_score	down-sample	indiv-rand-sample	20
tournament	0.1	elite_true_agg_score	down-sample	phylo-informed-sample	20
tournament	0.1	elite_true_agg_score	down-sample-ancestor	indiv-rand-sample	20
tournament	0.1	elite_true_agg_score	down-sample-ancestor	phylo-informed-sample	20
tournament	0.1	elite_true_agg_score	indiv-rand-sample	phylo-informed-sample	20

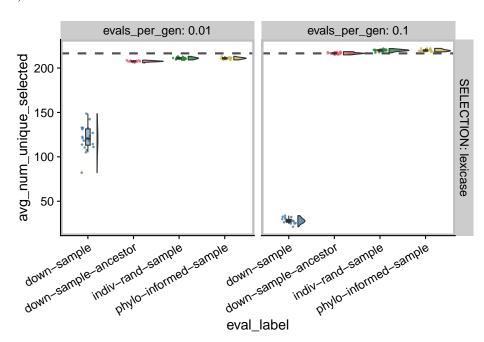
### 5.3.4 Over time - Lexicase

#### 5.3.5 Over time - Tournament

```
p <- ts_data %% build_plot_time_series(
   "exploitation-rate",
   "tournament",
   "max_agg_score"
)
ggsave(
  filename = paste0(plot_directory, "exploit-score-ts-tourn.pdf"),
  plot = p,
   width = 15,
   height = 10
)</pre>
```

## 5.4 Number unique individual selected

```
build_plot_summary_data(
    ts_summary_data,
    focal_diagnostic,
    "lexicase",
    "avg_num_unique_selected"
)
```



```
Average number selected by standard lexicase?
mean (filter (
   ts_summary_data,
  SELECTION == "lexicase" &
  DIAGNOSTIC == "exploitation-rate" &
   evals\_per\_gen == "1"
) $avg_num_unique_selected)
## [1] 216.6185
mean (filter (
   ts_summary_data,
  {\tt SELECTION} = "lexicase" \&
  \label{eq:discrete_discrete_discrete_discrete} \text{DIAGNOSTIC} == \text{"exploitation-rate" \&}
   evals\_per\_gen == "0.1",
   eval_label == "down-sample"
) $avg_num_unique_selected)
## [1] 28.099
mean (filter (
   ts summary data,
  SELECTION == "lexicase" &
  \label{eq:definition} {\rm DIAGNOSTIC} == \ "exploitation-rate" \ \& \\
   evals\_per\_gen == "0.01",
   eval_label == "down-sample"
) $avg_num_unique_selected)
## [1] 120.7455
```

## 5.5 Manuscript figures

Figures customized / cleaned up for the manuscript.

```
full_eval_steps <- as.numeric(</pre>
  levels (
    as.factor(
      filter(exploit_ts_data, eval_label == "full" &
         evaluations >= max_eval) $ evaluations # nolint:
           line\_length\_linter.
full_eval <- full_eval_steps [which.min( full_eval_steps
     - max_eval )]
full_median_score_evals <- median(
  filter (
    exploit_ts_data,
    SELECTION = selection & eval_label = "full" &
        evaluations == full_eval
  ) $max_agg_score
plot <- exploit_summary_data %%
  filter (
    eval label != "full" &
    SELECTION == selection &
    evals\_per\_gen == subsample\_rate
  ) %>%
  ggplot (
    aes (
      x = eval\_label,
      y = elite_true_agg_score,
      fill = eval\_label
  ) +
  geom_hline(
    yintercept = full_median_score_evals ,
    size = 1.0,
    alpha = 0.7,
    color = "black",
    linetype="dashed"
  geom_flat_violin(
    position = position\_nudge(x = .2, y = 0),
    alpha = .8,
    adjust = 1.5
  ) +
  geom_point (
```

```
mapping = aes(color = eval_label),
        position = position_jitter(width = .15),
        size = .5,
        alpha = 0.8
     geom_boxplot(
        width = .1,
        outlier.shape = NA,
        alpha = 0.5
     ) +
     scale_y_continuous(
       name = "Aggregate \_score",
        limits = c(0, 10010)
     scale_x_discrete(
       name = "Subsampling regimes",
        \label{eq:breaks} breaks \, = \, \mathbf{c} \, (\, " \, down - sample \, " \, , \, \ " \, down - sample - ancestor \, " \, , \, \ "
            indiv-rand-sample", "phylo-informed-sample"),
        \mathbf{labels} \; = \; \mathbf{c} \, (\; "\mathrm{DS}" \; , \quad "\mathrm{DS}\!\!+\!\!\mathrm{EST}" \; , \quad "\mathrm{IRS}" \; , \quad "\mathrm{ABS}" \; )
     scale_fill_bright() +
     scale_color_bright() +
     theme (
        legend. position = "none",
       \# axis.text.x = element\_text
       \# \quad angle = 30,
       #
           hjust = 1
       #),
  return (plot)
Build time series manuscript plot:
build_score_over_time_manuscript_plot <- function(
  selection,
  subsample_rate
) {
  \max_{eval} <- \max(
     filter(exploit_ts_data, evals_per_gen == subsample_
         rate) $ evaluations
  full_eval_steps <- as.numeric(
     levels (
        as.factor(
```

```
filter(exploit_ts_data, eval_label == "full" &
         evaluations >= max_eval) $ evaluations # nolint:
           line\_length\_linter.
full_eval <- full_eval_steps [which.min( full_eval_steps
     - max_eval )]
data <- exploit_ts_data %%
  filter (
    SELECTION = selection &
    evals_per_gen == subsample_rate
  ) %>%
  mutate (
    sampling_level_label = subsample_rate
full_diag_data <- exploit_ts_data %%
  filter (
    SELECTION == selection & eval_label == "full" &
       evaluations <= full_eval
  ) %>%
  mutate (
    \# Ensure that median line will sit in same facet
    sampling_level_label = subsample_rate
plot <- data %>%
  filter (
    eval_label != "full"
  ) %>%
  ggplot (
    aes (
      x = evaluations,
      y = max_agg_score
  ) +
  stat_summary(
    geom = "line",
    fun = mean,
    aes (
      color = eval_label
  ) +
  stat_summary(
```

```
geom = "ribbon",
    fun.data = "mean\_cl\_boot",
    fun.args = list(conf.int = 0.95),
    alpha = 0.2,
    linetype = 0,
    aes (
       color = eval_label,
       fill = eval\_label
  ) +
  scale_y_continuous(
    name = "Aggregate \_score",
    limits = c(0, 10010)
  scale_x_continuous(
    name = "Evaluations"
  ) +
  scale_fill_bright(
    labels=c(
       "Down-sampling \sqcup (DS), \sqcup no \sqcup estimation",
       "Down-sampling_{\sqcup}+_{\sqcup}Estimation_{\sqcup}(DS+EST)"
       "Individualized_{\square}random_{\square}sampling_{\square}(IRS)",
       "Ancestor-based_sampling_(ABS)"
  ) +
  scale_color_bright(
    labels=c(
       "Down-sampling (DS), no estimation",
       "Down-sampling _ + _ Estimation _ (DS+EST) "
       "Individualized random sampling (IRS)",
       "Ancestor-based_sampling_(ABS)"
  ) +
    legend.position = "none"
  stat_summary(
    data = full_diag_data,
    geom = "line",
    fun = median,
    linetype = "dashed",
    color = "black"
return (plot)
```

```
Build plots of final scores (after fixed number of evaluations)
plot final lex 01 <- build final score manuscript plot(
  "lexicase",
  "0.01"
plot_final_lex_10 <- build_final_score_manuscript_plot(</pre>
  "lexicase",
  " 0.1 "
plot_final_tourn_01 <- build_final_score_manuscript_plot(</pre>
  "tournament",
  "0.01"
plot_final_tourn_10 <- build_final_score_manuscript_plot(</pre>
  "tournament",
  " 0.1 "
Build time series plots (with evaluations on x-axis)
plot_ts_lex_01 <- build_score_over_time_manuscript_plot(</pre>
  "lexicase",
  " 0.01 "
plot_ts_lex_10 <- build_score_over_time_manuscript_plot(</pre>
  "lexicase",
  " 0.1 "
plot_ts_tourn_01 <- build_score_over_time_manuscript_plot</pre>
  "tournament",
  "0.01"
plot_ts_tourn_10 <- build_score_over_time_manuscript_plot</pre>
  "tournament",
  " 0.1 "
```

#### 5.5.1 Lexicase selection manuscript figure

```
txt_size <- 16
legend <- get_legend(</pre>
  plot_ts_lex_01 +
    guides (
      color = guide_legend(nrow = 2, title = "Subsampling
          □regime:"),
      fill = guide_legend(nrow = 2, title = "Subsampling_
          regime: ")
    ) +
    theme (
      legend. position = "bottom",
      legend.text = element_text(size = txt_size - 2),
      legend.title = element_text(size = txt_size)
)
grid <- plot_grid(
  plot_ts_lex_01 +
    labs(title = "1% Subsampling") +
    theme (
      axis.text.x = element\_text(size = txt\_size - 2),
      axis.text.y = element_text(size = txt_size),
      axis.title.x = element_text(size = txt_size),
      axis.title.y = element_text(size = txt_size)
  plot_final_lex_01 +
    theme (
      axis.text.y = element blank(),
      axis.title.y = element_blank(),
      axis.ticks.y = element_blank(),
      \mathbf{plot}.\mathbf{margin} = \mathbf{margin}(0, 0, 0, 1, "cm"),
      axis.text.x = element_text(size = txt_size),
      axis.title.x = element_text(size = txt_size)
  plot_ts_lex_10 +
    labs(title = "10% Subsampling") +
      axis.text.x = element\_text(size = txt\_size - 2),
      axis.text.y = element_text(size = txt_size),
      axis.title.x = element_text(size = txt_size),
      axis.title.y = element_text(size = txt_size)
  plot_final_lex_10 +
    theme (
      axis.text.y = element blank(),
      axis.title.y = element_blank(),
```

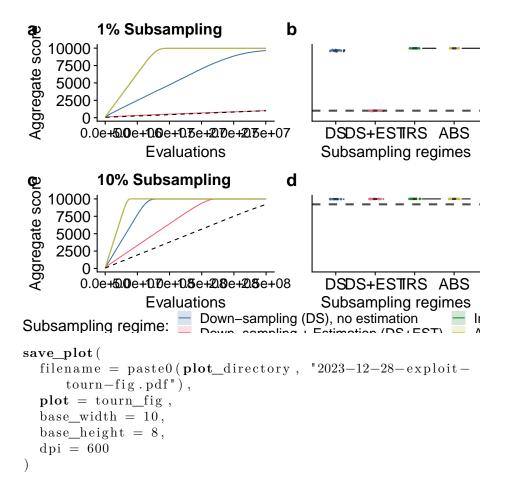
```
axis.ticks.y = element_blank(),
      \mathbf{plot}.\mathbf{margin} = \mathbf{margin}(0, 0, 0, 1, "cm"),
      axis.text.x = element_text(size = txt_size),
      axis.title.x = element_text(size = txt_size)
    ),
  \mathbf{nrow} = 2,
  ncol = 2,
  align = "h",
  labels = c("a", "b", "c", "d"),
  label\_size = 18,
  rel_{widths} = c(1.3, 1, 1.3, 1)
grid
          1% Subsampling
                                      b
Aggregate scor
   10000
    7500
    5000
    2500
       0.0e+500e+0.6e+0.5e+20.0e+20.5e+07
                                           DSDS+ESTIRS ABS
                 Evaluations
                                           Subsampling regimes
          10% Subsampling
                                     d
Aggregate scor®
   10000 -
    7500
    5000
    2500
       0.0e+500e+0.70e+0.5e+20.8e+20.5e+08
                                           DSDS+ESTIRS ABS
                 Evaluations
                                           Subsampling regimes
lex_fig <- plot_grid(</pre>
  grid,
  legend,
  nrow = 2,
  ncol = 1,
  rel\_heights = c(1, 0.05)
# lex_fig
save_plot(
  filename = paste0(plot_directory, "2023-12-28-exploit-
```

```
lex-fig.pdf"),
plot = lex_fig,
base_width = 10,
base_height = 8,
dpi = 600
)
```

#### 5.5.2 Tournament selection manuscript figures

```
legend <- get_legend(</pre>
  plot_ts_tourn_01 +
    guides (
      color = guide_legend(nrow = 2, title = "Subsampling
          □regime:"),
      fill = guide_legend(nrow = 2, title = "Subsampling_
          regime: ")
    ) +
    theme (
      legend.position = "bottom"
      legend.text = element_text(size = txt_size - 2),
      legend.title = element_text(size = txt_size)
)
grid <- plot_grid(
  plot ts tourn 01 +
    labs(title = "1%_Subsampling") +
      axis.text.x = element\_text(size = txt\_size - 2),
      axis.text.y = element_text(size = txt_size),
      axis.title.x = element_text(size = txt_size),
      axis.title.y = element_text(size = txt_size)
  {\bf plot\_final\_tourn\_01} \ +
    theme (
      axis.text.y = element_blank(),
      axis.title.y = element_blank(),
      axis.ticks.y = element_blank(),
      \mathbf{plot}.\mathbf{margin} = \mathbf{margin}(0, 0, 0, 1, "cm"),
      axis.text.x = element_text(size = txt_size),
      axis.title.x = element_text(size = txt_size)
    ),
  plot ts tourn 10 +
    labs(title = "10% Subsampling") +
```

```
theme (
      axis.text.x = element\_text(size = txt\_size - 2),
      axis.text.y = element_text(size = txt_size),
      axis.title.x = element_text(size = txt_size),
      axis.title.y = element_text(size = txt_size)
    ),
  plot_final_tourn_10 +
    theme (
      axis.text.y = element_blank(),
      axis.title.y = element_blank(),
      axis.ticks.y = element_blank(),
      \mathbf{plot}.\mathbf{margin} = \mathbf{margin}(0, 0, 0, 1, "cm"),
      axis.text.x = element_text(size = txt_size),
      axis.title.x = element_text(size = txt_size)
    ),
 nrow = 2,
  ncol = 2,
  align = "h",
  labels = c("a", "b", "c", "d"),
  label\_size = 18,
  rel\_widths = c(1.3, 1, 1.3, 1)
tourn_fig <- plot_grid(
  grid,
 legend,
 \mathbf{nrow} = 2,
 ncol = 1,
  rel\_heights = c(1, 0.05)
tourn_fig
```



## Chapter 6

# Contradictory objectives diagnostic

```
experiment_slug <- "2023-12-28-phylo-sampling-diag"
working_directory <- paste0(
   "experiments/",
   experiment_slug,
   "/analysis/"
)

if (exists("bookdown_wd_prefix")) {
   working_directory <- paste0(
      bookdown_wd_prefix,
      working_directory
   )
}</pre>
```

## 6.1 Dependencies

```
fb53bd97121f7f9ce947837ef1a4c65a73bffb3f/geom_flat_
    violin.R")
print(version)
                   aarch64-apple-darwin20
## platform
## arch
                   aarch64
## os
                   darwin20
                   aarch64, darwin20
## system
## status
## major
\#\# minor
                   2.1
                   2022
## year
\#\# month
                   06
## day
                   23
## svn rev
                   82513
## language
                   R
## version string R version 4.2.1 (2022-06-23)
## nickname
                   Funny-Looking Kid
```

## 6.2 Setup

```
# Configure our default graphing theme
theme_set(theme_cowplot())
# Create a directory to store plots
plot_directory <- paste0(working_directory, "plots/")
dir.create(plot_directory, showWarnings=FALSE)
# Constants
focal_diagnostic <- "contradictory-objectives"</pre>
```

#### 6.2.1 Load experiment summary data

```
summary_data_loc <- paste0(working_directory, "data/
    aggregate.csv")
summary_data <- read_csv(summary_data_loc)

## Rows: 1080 Columns: 58
## — Column specification</pre>
```

## Delimiter: ","

```
## chr (5): DIAGNOSTIC, EVAL_FIT_EST_MODE, EVAL_MODE,
   SELECTION, STOP_MODE
## dbl (53): ACCURACY, CREDIT, DIAGNOSTIC DIMENSIONALITY,
    EVAL_MAX_PHYLO_SEARCH...
## i Use 'spec()' to retrieve the full column
    specification for this data.
## i Specify the column types or set 'show_col_types =
   FALSE' to quiet this message.
summary data <- summary data %%
  mutate (
    evals_per_gen = case_when(
      EVAL\_MODE = "cohort-full-compete" \sim 1.0 / NUM_
          COHORTS,
      \label{eq:eval_MODE} = "cohort" ~ 1.0 / NUM\_COHORTS,
      EVAL_MODE == "down-sample" ~ TEST_DOWNSAMPLE_RATE,
      EVAL\ MODE = "full" \sim 1.0,
      EVAL_MODE == "indiv-rand-sample" ~ TEST_DOWNSAMPLE_
          RATE,
      EVAL_MODE == "phylo-informed-sample" ~ TEST_
          DOWNSAMPLE RATE
    EVAL_FIT_EST_MODE = case_when(
      EVAL_FIT_EST_MODE == "ancestor-opt" ~ "ancestor",
      EVAL_FIT_EST_MODE == "relative-opt" ~ "relative",
       .\;\mathbf{default}\;=\;\mathrm{EVAL}\underline{\ }\mathrm{FIT}\underline{\ }\mathrm{EST}\underline{\ }\mathrm{MODE}
    ),
    .keep = "all"
  ) %>%
  mutate (
    eval_label = case_when(
      # Clean up down-sample label
      EVAL_MODE == "down-sample" & EVAL_FIT_EST_MODE != "
          none" ~ paste ("down-sample", EVAL_FIT_EST_MODE,
          sep="-"),
      . default = EVAL\_MODE
    ),
  ) %>%
  mutate (
    evals_per_gen = as.factor(evals_per_gen),
    DIAGNOSTIC = as.factor(DIAGNOSTIC),
    SELECTION = as.factor(SELECTION),
    EVAL_MODE = as.factor(EVAL_MODE),
    NUM COHORTS = as.factor(NUM COHORTS),
    TEST_DOWNSAMPLE_RATE = as.factor(TEST_DOWNSAMPLE_RATE
```

mutate (

```
EVAL_FIT_EST_MODE = factor(
      EVAL FIT EST MODE,
      levels = c(
        "none",
        "ancestor",
        "relative"
      ),
      labels = c(
        "None",
        "Ancestor",
        "Relative"
    )
  )
# Grab just the contradictory objectives data
con_obj_summary_data <- filter(
  summary_data,
  DIAGNOSTIC == "contradictory-objectives"
6.2.2
      Load experiment time series data
ts_data_loc <- paste0(working_directory, "data/time_
   series.csv")
ts_data <- read_csv(ts_data_loc)
## Rows: 108000 Columns: 28
## — Column specification
## Delimiter: ","
## chr (4): DIAGNOSTIC, EVAL_FIT_EST_MODE, EVAL_MODE,
   SELECTION
## dbl (24): NUM_COHORTS, SEED, TEST_DOWNSAMPLE RATE,
   ave_depth, deleterious_st...
## i Use 'spec()' to retrieve the full column
   specification for this data.
## i Specify the column types or set 'show_col_types =
   FALSE' to quiet this message.
ts data <- ts data %%
```

```
evals_per_gen = case_when(
    EVAL\_MODE = "cohort-full-compete" \sim 1.0 / NUM\_
       COHORTS,
    EVAL_MODE == "cohort" ~ 1.0 / NUM_COHORTS,
   EVAL_MODE == "down-sample" ~ TEST_DOWNSAMPLE_RATE,
   \overline{\text{EVAL}} \underline{\text{MODE}} = "full" \sim 1.0,
    EVAL_MODE == "indiv-rand-sample" ~ TEST_DOWNSAMPLE_
       RATE,
   EVAL MODE == "phylo-informed-sample" ~ TEST
       DOWNSAMPLE RATE
 EVAL_FIT_EST_MODE = case_when(
    EVAL\_FIT\_EST\_MODE == "ancestor-opt" \sim "ancestor",
    EVAL_FIT_EST_MODE == "relative-opt" ~ "relative",
    . default = EVAL\_FIT\_EST\_MODE
  .keep = "all"
) %>%
mutate(
  eval_label = case_when(
    EVAL_MODE == "down-sample" & EVAL_FIT_EST_MODE != "
       none" ~ paste("down-sample", EVAL_FIT_EST_MODE,
        sep="-"),
    . default = EVAL\_MODE
) %>%
mutate (
  evals per gen = as.factor(evals per gen),
  DIAGNOSTIC = as.factor(DIAGNOSTIC),
  SELECTION = as.factor(SELECTION),
 EVAL\_MODE = as.factor(EVAL\_MODE),
 NUM COHORTS = as. factor (NUM COHORTS),
  TEST_DOWNSAMPLE_RATE = as.factor(TEST_DOWNSAMPLE_RATE
 EVAL_FIT_EST_MODE = factor(
   EVAL_FIT_EST_MODE,
    levels = c(
      "none",
      "ancestor",
      "relative"
    labels = c(
      "None",
      "Ancestor",
      "Relative"
```

```
# Grab just the contradictory objectives data
con_obj_ts_data <- ts_data %%
  filter (DIAGNOSTIC == "contradictory-objectives")
Summarize time series data:
ts_summary_data <- ts_data %>%
  group_by(SEED, DIAGNOSTIC, SELECTION, evals_per_gen,
     eval_label) %%
  summarize (
    n = n()
    avg_num_unique_selected = mean(num_unique_selected),
    total_optimal_trait_coverage_loss = sum(optimal_trait
       _coverage_loss)
  )
## 'summarise()' has grouped output by 'SEED', '
   DIAGNOSTIC', 'SELECTION',
## 'evals_per_gen'. You can override using the '.groups'
   argument.
```

#### 6.2.3 Plotting helper functions

The following function assist with exploratory plotting of different measurements from summary and time series data. Note that for these plots, standard lexicase reference is rendered at equivalent number of generations (instead of evaluations).

```
build_plot_summary_data <- function(data, diagnostic,
    selection, response) {
    diag_data <- data %% filter(DIAGNOSTIC == diagnostic)

    full_median <- median(
        filter(
            diag_data,
            eval_label == "full" & SELECTION == selection
        ) [[response]]
    )

    plot <- diag_data %%
        filter(
        eval_label != "full" & SELECTION == selection
        ) %%</pre>
```

```
ggplot (
  aes_string(
    x = "eval\_label",
    y = response,
    fill = "eval\_label"
  )
) +
geom_hline (
  yintercept = full_median,
  size = 1.0,
  alpha = 0.7,
  color = "black"
  linetype="dashed"
geom_flat_violin(
  position = position\_nudge(x = .2, y = 0),
  alpha = .8,
  adjust = 1.5
) +
geom_point (
  mapping = aes(color = eval_label),
  position = position_jitter(width = .15),
  size = .5,
  alpha = 0.8
) +
geom_boxplot(
  width = .1,
  outlier.shape = NA,
  alpha = 0.5
scale_y_continuous(
  \# \ limits = c(-0.5, 100)
) +
scale_fill_bright() +
scale_color_bright() +
facet_grid(
  SELECTION ~ evals_per_gen,
  \# nrow = 2,
  labeller = label\_both
) +
theme (
  legend.position = "none",
  axis.text.x = element_text(
    angle = 30,
    hjust = 1
  ),
```

```
panel.border = element_rect(color = "gray", size =
         2)
 return (plot)
build_plot_time_series_single_sampling <- function(</pre>
 data,
 diagnostic,
 selection,
 sampling_level,
 response
 diag_data <- data %% filter (
   DIAGNOSTIC = diagnostic &
   SELECTION = selection &
   evals_per_gen == sampling_level
 ) %>%
 mutate (
   sampling_level_label = sampling_level
  full_diag_data <- data %% filter (
   DIAGNOSTIC = diagnostic & SELECTION = selection &
       eval label == "full"
 ) %>%
 mutate (
   # Ensure that median line will sit in same facet
   sampling_level_label = sampling_level
 plot <- diag_data %>%
    filter (
      eval_label != "full"
    ) %>%
   ggplot (
      aes_string(
       x = "ts\_step",
       \# x = "evaluations",
        y = \{\{ exponse \} \}
    ) +
    stat summary(
     geom = "line",
```

```
fun = mean,
      aes (
        color = eval_label
    ) +
    stat_summary(
      geom = "ribbon",
      fun.data = "mean\_cl\_boot",
      fun.args = list(conf.int = 0.95),
      alpha = 0.2,
      linetype = 0,
      aes (
        color = eval_label,
        fill = eval\_label
      )
    ) +
    scale_fill_bright() +
    scale_color_bright() +
    # facet_wrap(
      \sim sampling\_level\_label,
    #
        n col = 1,
    #
        labeller = label\_both
    # ) +
    theme (
      legend.position = "right"
    stat_summary(
      data = full_diag_data,
      geom = "line",
      fun = median,
      linetype = "dashed",
      color = "black"
  return (plot)
build_plot_time_series <- function(</pre>
  data,
  diagnostic,
  selection,
 response
 # Build 1% sampling plot and 10% sampling plot
 p_01 <- data %% build_plot_time_series_single_
     sampling (
```

}

```
diagnostic,
  selection,
  "0.01",
  response
p_10 <- data %% build_plot_time_series_single_sampling
  diagnostic,
  selection,
  "0.1",
  response
)
title <- ggdraw() +
  draw_label(
    paste0 (diagnostic, "u-u", selection),
    fontface = 'bold',
    x = 0,
    hjust = 0
  ) +
  theme (
    # add margin on the left of the drawing canvas,
    \# so title is aligned with left edge of first plot
    plot.margin = margin(0, 0, 0, 7)
plot <- plot_grid(</pre>
  title,
  \underline{p}_01 + labs(title = "1\% subsampling") + theme(legend.
      position = "none"),
  p_10 + labs(title = "10%_subsampling") + theme(legend
     .position = "bottom"),
  nrow = 3,
  ncol = 1,
  rel\_heights = c(0.075, 1, 1)
return (plot)
```

## 6.3 Population-wide satisfactory trait coverage

#### 6.3.1 Final - Lexicase selection

```
p <- summary_data %% build_plot_summary_data(
   focal_diagnostic,
   "lexicase",
   "pop_optimal_trait_coverage"
)
ggsave(
   filename = paste0(plot_directory, "con-obj-sat-cov-final-lex.pdf"),
   plot = p + labs(title = "Contradictory_objectives_-
        Lexicase_selection"),
   width = 15,
   height = 10
)</pre>
```

#### 6.3.1.1 Statistics

First, we'll create a table of median / mean values for easy reference.

vals_per_gen .01 .01 .01 .01 .01 .1 .1	eval_label down-sample down-sample-ancestor indiv-rand-sample phylo-informed-sample down-sample down-sample-ancestor	cov_median 1.0 2.5 8.0 8.5 1.0 17.5	c
.01 .01 .01 .1	down-sample-ancestor indiv-rand-sample phylo-informed-sample down-sample down-sample-ancestor	2.5 8.0 8.5 1.0	
.01	indiv-rand-sample phylo-informed-sample down-sample down-sample-ancestor	8.0 8.5 1.0	
.01 .1 .1	phylo-informed-sample down-sample down-sample-ancestor	8.5 1.0	
.1	down-sample down-sample-ancestor	1.0	
.1	down-sample-ancestor		
	4	17.5	
1			
.1	indiv-rand-sample	24.5	
.1	phylo-informed-sample	24.0	
	full	38.0	
.01	down-sample	1.0	
.01	down-sample-ancestor	1.0	
.01	indiv-rand-sample	1.0	
.01	phylo-informed-sample	1.0	
.1	down-sample	1.0	
.1	down-sample-ancestor	1.0	
.1	indiv-rand-sample	1.0	
.1	phylo-informed-sample	1.0	
	full	1.0	
.1	L L	phylo-informed-sample down-sample down-sample-ancestor indiv-rand-sample phylo-informed-sample	D1         phylo-informed-sample         1.0           L         down-sample         1.0           L         down-sample-ancestor         1.0           L         indiv-rand-sample         1.0           L         phylo-informed-sample         1.0

Next, we run a Kruskal-Wallis test to check for differences. For these tests, we only compare within a single subsampling level (evals\_per\_gen) and within the same selection scheme.

comparison_group	SELECTION	evals_per_gen	.y.	n	statistic
lexicase_0.01	lexicase	0.01	pop_optimal_trait_coverage	80	58.24682
lexicase_0.1	lexicase	0.1	pop_optimal_trait_coverage	80	62.11510
tournament_0.01	tournament	0.01	pop_optimal_trait_coverage	80	NaN
tournament_0.1	tournament	0.1	pop_optimal_trait_coverage	80	NaN

 $<sup>\#\</sup> Grab\ group\ names\ of\ significant\ comparisons$ 

```
sig_kw_groups <- filter(kw_test, p < 0.05)$comparison_
   group
wrs_test <- con_obj_summary_data %%
  unite (
    "comparison_group",
   SELECTION,
    evals_per_gen,
    sep = "_{"},
    remove = FALSE
  ) %>%
  filter (
    eval_label != "full" & comparison_group %in% sig_kw_
       groups
  ) %>%
  group_by(SELECTION, evals_per_gen) %%
  pairwise_wilcox_test(pop_optimal_trait_coverage ~ eval_
     label) %>%
  adjust_pvalue(method = "holm") %%
 add_significance("p.adj")
kable (wrs_test)
```

SELECTION	evals_per_gen	.y.	group1	group2
lexicase	0.01	pop_optimal_trait_coverage	down-sample	down-sample-ancestor
lexicase	0.01	pop_optimal_trait_coverage	down-sample	indiv-rand-sample
lexicase	0.01	pop_optimal_trait_coverage	down-sample	phylo-informed-sample
lexicase	0.01	pop_optimal_trait_coverage	down-sample-ancestor	indiv-rand-sample
lexicase	0.01	pop_optimal_trait_coverage	down-sample-ancestor	phylo-informed-sample
lexicase	0.01	pop_optimal_trait_coverage	indiv-rand-sample	phylo-informed-sample
lexicase	0.1	pop_optimal_trait_coverage	down-sample	down-sample-ancestor
lexicase	0.1	pop_optimal_trait_coverage	down-sample	indiv-rand-sample
lexicase	0.1	pop_optimal_trait_coverage	down-sample	phylo-informed-sample
lexicase	0.1	pop_optimal_trait_coverage	down-sample-ancestor	indiv-rand-sample
lexicase	0.1	pop_optimal_trait_coverage	down-sample-ancestor	phylo-informed-sample
lexicase	0.1	pop_optimal_trait_coverage	indiv-rand-sample	phylo-informed-sample

#### 6.3.2 Over time - lexicase selection

```
p <- ts_data %% build_plot_time_series(
  focal_diagnostic,
  "lexicase",
  "pop_optimal_trait_coverage"
)
ggsave(</pre>
```

```
filename = paste0(plot_directory, "con-obj-sat-cov-ts-
    lex.pdf"),
plot = p,
width = 15,
height = 10
```

#### 6.3.3 Final - Tournament selection

```
p <- summary_data %% build_plot_summary_data(
    focal_diagnostic,
    "tournament",
    "pop_optimal_trait_coverage"
)
ggsave(
    filename = paste0(plot_directory, "con-obj-sat-cov-
        final-tourn.pdf"),
plot = p + labs(title = "Contradictory_objectives_-
        Tournament_selection"),
width = 15,
height = 10
)</pre>
```

#### 6.3.4 Over time - tournament selection

```
p <- ts_data %% build_plot_time_series(
  focal_diagnostic,
  "tournament",
  "pop_optimal_trait_coverage"
)
ggsave(
  filename = paste0(plot_directory, "con-obj-sat-cov-ts-tourn.pdf"),
  plot = p,
  width = 15,
  height = 10
)</pre>
```

## 6.4 MRCA changes

## 6.5 Mean genotype deleterious steps

```
p <- summary_data %% build_plot_summary_data(
   focal_diagnostic,
   "lexicase",
   "phylo_mean_genoetype_deleterious_steps"
)
ggsave(
   filename = paste0(plot_directory, "con-obj-del-steps-
        final-lex.pdf"),
   plot = p + labs(title = "Contradictory_objectives_-
        Lexicase_selection"),
   width = 15,
   height = 10
)</pre>
```

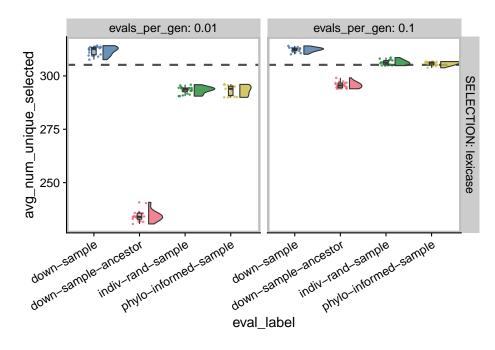
## 6.6 Mean genotype pairwise distance

```
p <- summary_data %% build_plot_summary_data(
  focal_diagnostic,
  "lexicase",
  "phylo_mean_genotype_pairwise_distance"
)
ggsave(
  filename = paste0(plot_directory, "con-obj-pw-dist-
        final-lex.pdf"),
  plot = p + labs(title = "Contradictory_objectives_-
        Lexicase_selection"),</pre>
```

```
width = 15, 
 height = 10
```

## 6.7 Number unique individual selected

```
build_plot_summary_data(
    ts_summary_data,
    focal_diagnostic,
    "lexicase",
    "avg_num_unique_selected")
```



## 6.8 Manuscript figures

```
Time series graphs don't add a ton here, so just final graphs.
```

```
build_final_score_manuscript_plot <- function(
    selection ,
    subsample_rate
) {</pre>
```

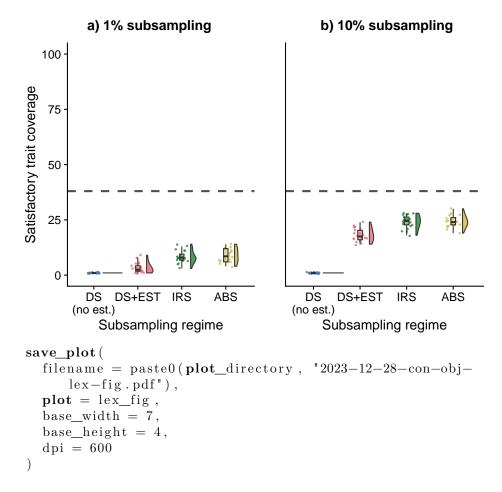
```
\# Extract median values for max aggregate score at same
     evaluation level as sampling regimes
\max_{e} eval \leftarrow \max(
  filter (con_obj_summary_data, evals_per_gen ==
     subsample_rate) $ evaluations
full_eval_steps <- as.numeric(
  levels (
    as.factor(
      filter(con_obj_summary_data, eval_label == "full"
          & evaluations >= max_eval)$evaluations #
          nolint: line\_length\_linter.
  )
full_eval <- full_eval_steps [which.min(full_eval_steps
     - \max_{eval}
full_median_score_evals <- median(
  filter (
    con_obj_summary_data,
    SELECTION = selection & eval_label = "full" &
        evaluations == full_eval
  ) $pop_optimal_trait_coverage
plot <- con_obj_summary_data %%
  filter (
    eval label != "full" &
    SELECTION = selection &
    evals_per_gen == subsample_rate
  ) %>%
  ggplot (
    aes (
      x = eval\_label,
      y = pop_optimal_trait_coverage,
      fill = eval\_label
  ) +
  geom hline (
    yintercept = full_median_score_evals,
    size = 1.0,
    alpha = 0.7,
    color = "black"
    linetype="dashed"
  geom_flat_violin(
```

```
position = position\_nudge(x = .2, y = 0),
      alpha = .8,
      adjust = 1.5
    ) +
    geom_point(
      mapping = aes(color = eval_label),
      position = position_jitter(width = .15),
      size = .5,
      alpha = 0.8
    ) +
    geom boxplot(
      width = .1,
      outlier.shape = NA,
      alpha = 0.5
    ) +
    scale_y_continuous(
      name = "Satisfactory trait coverage",
      limits = \mathbf{c}(0, 100)
    ) +
    scale_x_discrete(
      name = "Subsampling_regime",
      breaks = c("down-sample", "down-sample-ancestor", "
          indiv-rand-sample", "phylo-informed-sample"),
      labels = c("DS \setminus n(no_{\square}est.)", "DS + EST", "IRS", "ABS")
    scale_fill_bright() +
    scale_color_bright() +
    theme (
      legend.position = "none",
      \# \ axis.text.x = element\_text(
           angle = 30,
      #
           hjust = 1
      #),
  return (plot)
Build end-of-run plots (fixed number of evaluations)
plot_final_lex_01 <- build_final_score_manuscript_plot(</pre>
  "lexicase",
  "0.01"
plot_final_lex_10 <- build_final_score_manuscript_plot(</pre>
  "lexicase",
  " 0.1 "
```

)

Combine into single figure

```
{\bf plot\_final\_lex\_01} \ +
    # labs (
    \# title = "1\% subsampling"
    # ) +
    theme (
       \mathbf{plot}.\mathbf{margin} = \mathbf{margin}(1, 0, 0, 0, "cm")
  {\bf plot\_final\_lex\_10} \ +
    # labs(
    \# title = "10\% subsampling"
    # ) +
    theme (
       axis.text.y = element_blank(),
       axis.title.y = element_blank(),
       axis.ticks.y = element_blank(),
       \mathbf{plot}.\mathbf{margin} = \mathbf{margin}(1, 0, 0, 1, "cm")
    ),
  \mathbf{nrow} = 1,
  ncol = 2,
  align = "h",
  labels = c("a) 1\% subsampling", "b) 10\% subsampling"),
  rel\_widths = c(1, 1)
lex_fig
```



## Chapter 7

# Multi-path exploration diagnostic

```
experiment_slug <- "2023-12-28-phylo-sampling-diag"
working_directory <- paste0(
   "experiments/",
   experiment_slug,
   "/analysis/"
)

if (exists("bookdown_wd_prefix")) {
   working_directory <- paste0(
      bookdown_wd_prefix,
      working_directory
   )
}</pre>
```

## 7.1 Dependencies

```
fb53bd97121f7f9ce947837ef1a4c65a73bffb3f/geom_flat_
    violin.R")
print(version)
                   aarch64-apple-darwin20
## platform
## arch
                   aarch64
                   darwin20
## os
                   aarch64, darwin20
## system
## status
## major
\#\# minor
                   2.1
                   2022
## year
\#\# month
                   06
## day
                   23
## svn rev
                   82513
## language
                   R
## version string R version 4.2.1 (2022-06-23)
## nickname
                   Funny-Looking Kid
```

## 7.2 Setup

```
# Configure our default graphing theme
theme_set(theme_cowplot())
# Create a directory to store plots
plot_directory <- paste0(working_directory, "plots/")
dir.create(plot_directory, showWarnings=FALSE)
# Constants
focal_diagnostic <- "multipath-exploration"</pre>
```

#### 7.2.1 Load experiment summary data

```
summary_data_loc <- paste0(working_directory, "data/
    aggregate.csv")
summary_data <- read_csv(summary_data_loc)

## Rows: 1080 Columns: 58
## — Column specification</pre>
```

## Delimiter: ","

```
## chr (5): DIAGNOSTIC, EVAL_FIT_EST_MODE, EVAL_MODE,
    SELECTION, STOP_MODE
## dbl (53): ACCURACY, CREDIT, DIAGNOSTIC DIMENSIONALITY,
    EVAL_MAX_PHYLO_SEARCH...
##
## i Use 'spec()' to retrieve the full column
    specification for this data.
## i Specify the column types or set 'show_col_types =
    FALSE' to quiet this message.
summary data <- summary data %%
  mutate (
     evals_per_gen = case_when(
      EVAL\_MODE = "cohort-full-compete" \sim 1.0 / NUM_
          COHORTS,
      \label{eq:eval_MODE} = "cohort" ~ 1.0 / NUM\_COHORTS,
      EVAL_MODE == "down-sample" ~ TEST_DOWNSAMPLE_RATE,
      EVAL MODE = "full" \sim 1.0,
      EVAL_MODE == "indiv-rand-sample" ~ TEST_DOWNSAMPLE_
          RATE,
      EVAL_MODE == "phylo-informed-sample" ~ TEST_
          DOWNSAMPLE RATE
    EVAL_FIT_EST_MODE = case_when(
      EVAL_FIT_EST_MODE == "ancestor-opt" ~ "ancestor",
      EVAL_FIT_EST_MODE == "relative-opt" ~ "relative",
       .\;\mathbf{default}\;=\;\mathrm{EVAL}\underline{\ }\mathrm{FIT}\underline{\ }\mathrm{EST}\underline{\ }\mathrm{MODE}
    ),
     .keep = "all"
  ) %>%
  mutate (
    eval_label = case_when(
       # Clean up down-sample label
      EVAL_MODE == "down-sample" & EVAL_FIT_EST_MODE != "
          none" ~ paste ("down-sample", EVAL_FIT_EST_MODE,
          sep="-"),
       . default = EVAL\_MODE
    ),
  ) %>%
  mutate (
    evals_per_gen = as.factor(evals_per_gen),
    DIAGNOSTIC = as.factor(DIAGNOSTIC),
    SELECTION = as.factor(SELECTION),
    EVAL_MODE = as.factor(EVAL_MODE),
    NUM COHORTS = as.factor(NUM COHORTS),
    TEST_DOWNSAMPLE_RATE = as.factor(TEST_DOWNSAMPLE_RATE
```

```
EVAL_FIT_EST_MODE = factor(
      EVAL FIT EST MODE,
      levels = c(
        "none",
        "ancestor",
        "relative"
      ),
      labels = c(
        "\,\mathrm{None}\," ,
        "Ancestor",
        "Relative"
    )
  )
explore_summary_data <- filter(
  summary_data,
  DIAGNOSTIC = "multipath-exploration"
      Load experiment time series data
ts_data_loc <- paste0(working_directory, "data/time_
   series.csv")
ts_data <- read_csv(ts_data_loc)
## Rows: 108000 Columns: 28
## — Column specification
## Delimiter: ","
## chr (4): DIAGNOSTIC, EVAL_FIT_EST_MODE, EVAL_MODE,
   SELECTION
## dbl (24): NUM_COHORTS, SEED, TEST_DOWNSAMPLE_RATE,
   ave_depth, deleterious_st...
## i Use 'spec()' to retrieve the full column
   specification for this data.
## i Specify the column types or set 'show_col_types =
   FALSE' to quiet this message.
ts_data <- ts_data %%
  mutate (
    evals_per_gen = case_when(
```

```
 = "cohort-full-compete" \sim 1.0 / NUM_{\_} 
       COHORTS,
    EVAL MODE == "cohort" ~ 1.0 / NUM COHORTS,
    EVAL MODE == "down-sample" ~ TEST_DOWNSAMPLE RATE,
   \label{eq:eval_mode} \text{EVAL\_MODE} == \text{"full"} \sim \text{1.0} \,,
    EVAL_MODE == "indiv-rand-sample" ~ TEST_DOWNSAMPLE_
       RATE,
   EVAL_MODE == "phylo-informed-sample" ~ TEST_
       DOWNSAMPLE_RATE
  ),
 EVAL FIT EST MODE = case when(
    EVAL_FIT_EST_MODE == "ancestor-opt" ~ "ancestor",
    EVAL_FIT_EST_MODE == "relative-opt" ~ "relative",
    .default = EVAL\_FIT\_EST\_MODE
  ),
  .keep = "all"
) %>%
mutate (
  eval_label = case_when(
    EVAL\_MODE == "down-sample" \& EVAL\_FIT\_EST\_MODE != "
       none" ~ paste("down-sample", EVAL_FIT_EST_MODE,
       sep="-"),
    . default = EVAL\_MODE
) %>%
mutate(
  evals_per_gen = as.factor(evals_per_gen),
  DIAGNOSTIC = as.factor(DIAGNOSTIC),
 SELECTION = as.factor(SELECTION),
 EVAL MODE = as.factor(EVAL MODE),
 NUM\_COHORTS = as.factor(NUM\_COHORTS),
  TEST_DOWNSAMPLE_RATE = as.factor(TEST_DOWNSAMPLE_RATE
     ),
 EVAL_FIT_EST_MODE = factor(
    EVAL_FIT_EST_MODE,
    levels = c(
      "none",
      "ancestor",
      "relative"
    ),
    labels = c(
      "None",
      "Ancestor"
      "Relative"
    )
  )
```

```
)
explore_ts_data <- ts_data %%
  filter (DIAGNOSTIC == "multipath-exploration")
Summarize time series data
ts_summary_data <- ts_data %%
  group_by(SEED, DIAGNOSTIC, SELECTION, evals_per_gen,
     eval_label) %>%
  summarize (
    n = n()
    avg_num_unique_selected = mean(num_unique_selected),
    total_optimal_trait_coverage_loss = sum(optimal_trait
       _coverage_loss)
  )
## 'summarise()' has grouped output by 'SEED', '
   DIAGNOSTIC', 'SELECTION',
## 'evals_per_gen'. You can override using the '.groups'
   argument.
```

#### 7.2.3 Plotting helper functions

The following function assist with exploratory plotting of different measurements from summary and time series data. Note that for these plots, standard lexicase reference is rendered at equivalent number of generations (instead of evaluations).

```
build_plot_summary_data <- function(data, diagnostic,
    selection, response) {
    diag_data <- data %% filter(DIAGNOSTIC == diagnostic)

    full_median <- median(
        filter(
            diag_data,
            eval_label == "full" & SELECTION == selection
        ) [[response]]
    )

    plot <- diag_data %%
        filter(
            eval_label != "full" & SELECTION == selection
        ) %%
        ggplot(
            aes_string()</pre>
```

```
x = "eval\_label",
    y = response,
    fill = "eval_label"
  )
) +
geom_hline (
  yintercept = full_median,
  \mathrm{size} \ = \ 1.0 \ ,
  alpha = 0.7,
  color = "black".
  linetype="dashed"
) +
geom_flat_violin(
  position = position\_nudge(x = .2, y = 0),
  alpha = .8,
  adjust = 1.5
) +
geom_point (
  mapping = aes(color = eval_label),
  position = position_jitter(width = .15),
  size = .5,
  alpha = 0.8
) +
geom_boxplot(
  width = .1,
  outlier.shape = NA,
  alpha = 0.5
scale_y_continuous (
  \# \ limits = c(-0.5, 100)
) +
scale_fill_bright() +
scale_color_bright() +
facet_grid(
  SELECTION ~ evals_per_gen,
  \# nrow = 2,
  labeller = label\_both
) +
theme (
  legend.position = "none",
  axis.text.x = element_text(
    angle = 30,
    hjust = 1
  panel.border = element_rect(color = "gray", size =
      2)
```

```
)
 return (plot)
build_plot_time_series_single_sampling <- function(
 data,
  diagnostic,
  selection,
  sampling_level,
 response
) {
  diag_data <- data %>% filter (
   DIAGNOSTIC = diagnostic &
   SELECTION == selection &
    evals_per_gen == sampling_level
  ) %>%
  mutate (
    sampling_level_label = sampling_level
  full_diag_data <- data %>% filter (
   DIAGNOSTIC = diagnostic & SELECTION = selection &
       eval_label == "full"
  ) %>%
 mutate (
    # Ensure that median line will sit in same facet
    sampling\_level\_label = sampling\_level
  plot <- diag_data %%
    filter (
      eval_label != "full"
    ) %>%
    ggplot (
      aes_string(
       x = "ts\_step",
        \# x = "evaluations",
        y = \{\{ exponse \} \}
    ) +
    stat_summary(
      geom = "line",
      fun = mean,
      aes (
```

```
color = eval_label
    ) +
    stat_summary(
      geom = "ribbon",
      fun.data = "mean_cl_boot",
      fun.args = list(conf.int = 0.95),
      alpha = 0.2,
      linetype = 0,
      aes (
         color = eval_label,
         fill = eval\_label
      )
    ) +
    scale\_fill\_bright() +
    scale_color_bright() +
    # facet_wrap(
        \sim sampling\_level\_label,
    #
        n col = 1,
    #
         labeller = label\_both
    # ) +
    theme (
      legend.position = "right"
    ) +
    \mathbf{stat}\underline{\mathbf{summary}}(
      data = full_diag_data,
      geom = "line",
      fun = median,
      linetype = "dashed",
      color = "black"
    )
  return (plot)
build_plot_time_series <- function(</pre>
  data,
  diagnostic,
  selection,
  response
) {
  \# Build 1% sampling plot and 10% sampling plot
  p_01 <- data %% build_plot_time_series_single_
     sampling (
    diagnostic,
    selection,
```

```
"0.01",
  response
p_10 <- data %% build_plot_time_series_single_sampling
  diagnostic,
  selection,
  "0.1",
  response
title <- ggdraw() +
  draw_label(
    pasteO(diagnostic, "u-u", selection),
    fontface = 'bold',
    x = 0,
    hjust = 0
  ) +
  theme (
    # add margin on the left of the drawing canvas,
    # so title is aligned with left edge of first plot
    \mathbf{plot}.\mathbf{margin} = \mathbf{margin}(0, 0, 0, 7)
plot <- plot_grid(</pre>
  title,
  p_01 + labs(title = "1%_subsampling") + theme(legend.
      position = "none"),
  \underline{p}_10 + labs(title = "10\% \cup subsampling") + theme(legend)
      .position = "bottom"),
  nrow = 3,
  ncol = 1,
  rel\_heights = c(0.075, 1, 1)
return (plot)
```

## 7.3 Aggregate score

#### 7.3.1 Final - Lexicase selection

Note that lexicase baseline is shown @ 50,000 generations (not same number of evaluations).

#### 7.3.1.1 Statistics

First, we'll create a table of median / mean values for easy reference.

DIAGNOSTIC	SELECTION	evals_per_gen	eval_label	score_median	s
multipath-exploration	lexicase	0.01	down-sample	481.7515	
multipath-exploration	lexicase	0.01	down-sample-ancestor	343.1445	
multipath-exploration	lexicase	0.01	indiv-rand-sample	1321.9050	
multipath-exploration	lexicase	0.01	phylo-informed-sample	1259.1250	
multipath-exploration	lexicase	0.1	down-sample	588.2735	
multipath-exploration	lexicase	0.1	down-sample-ancestor	2532.2150	
multipath-exploration	lexicase	0.1	indiv-rand-sample	2295.0250	
multipath-exploration	lexicase	0.1	phylo-informed-sample	2579.3150	
multipath-exploration	lexicase	1	full	9082.8750	
multipath-exploration	tournament	0.01	down-sample	656.5385	
multipath-exploration	tournament	0.01	down-sample-ancestor	547.7415	
multipath-exploration	tournament	0.01	indiv-rand-sample	3524.0450	
multipath-exploration	tournament	0.01	phylo-informed-sample	2894.6900	
multipath-exploration	tournament	0.1	down-sample	2349.5100	
multipath-exploration	tournament	0.1	down-sample-ancestor	3789.5600	
multipath-exploration	tournament	0.1	indiv-rand-sample	5149.1700	
multipath-exploration	tournament	0.1	phylo-informed-sample	5449.0750	
multipath-exploration	tournament	1	full	4649.8450	

Next, we run a Kruskal-Wallis test to check for differences. For these tests, we only compare within a single subsampling level (evals\_per\_gen) and within the same selection scheme.

comparison_group	SELECTION	evals_per_gen	.y.	n	statistic	df	
lexicase_0.01	lexicase	0.01	elite_true_agg_score	80	63.64833	3	(
lexicase_0.1	lexicase	0.1	elite_true_agg_score	80	48.94519	3	(
tournament_0.01	tournament	0.01	elite_true_agg_score	80	30.85796	3	
tournament_0.1	tournament	0.1	elite_true_agg_score	80	10.82091	3	П

```
\# Grab group names of significant comparisons sig_kw_groups \leftarrow filter(kw_test , p < 0.05) $comparison_group
```

```
wrs\_test <\!\!- explore\_summary\_data \%\%
  unite (
    "comparison_group",
   SELECTION,
    evals_per_gen,
    sep = "\_",
    remove = FALSE
  ) %>%
  filter (
    eval_label != "full" & comparison_group %in% sig_kw_
       groups
  ) %>%
  group_by(SELECTION, evals_per_gen) %%
  pairwise_wilcox_test(elite_true_agg_score ~ eval_label)
      %>%
  adjust\_pvalue(method = "holm") \%\%
  add_significance("p.adj")
kable (wrs_test)
```

SELECTION	evals_per_gen	.y.	group1	group2
lexicase	0.01	elite_true_agg_score	down-sample	down-sample-ances
lexicase	0.01	elite_true_agg_score	down-sample	indiv-rand-sample
lexicase	0.01	elite_true_agg_score	down-sample	phylo-informed-san
lexicase	0.01	elite_true_agg_score	down-sample-ancestor	indiv-rand-sample
lexicase	0.01	elite_true_agg_score	down-sample-ancestor	phylo-informed-san
lexicase	0.01	elite_true_agg_score	indiv-rand-sample	phylo-informed-san
lexicase	0.1	elite_true_agg_score	down-sample	down-sample-ances
lexicase	0.1	elite_true_agg_score	down-sample	indiv-rand-sample
lexicase	0.1	elite_true_agg_score	down-sample	phylo-informed-san
lexicase	0.1	elite_true_agg_score	down-sample-ancestor	indiv-rand-sample
lexicase	0.1	elite_true_agg_score	down-sample-ancestor	phylo-informed-san
lexicase	0.1	elite_true_agg_score	indiv-rand-sample	phylo-informed-san
tournament	0.01	elite_true_agg_score	down-sample	down-sample-ances
tournament	0.01	elite_true_agg_score	down-sample	indiv-rand-sample
tournament	0.01	elite_true_agg_score	down-sample	phylo-informed-san
tournament	0.01	elite_true_agg_score	down-sample-ancestor	indiv-rand-sample
tournament	0.01	elite_true_agg_score	down-sample-ancestor	phylo-informed-san
tournament	0.01	elite_true_agg_score	indiv-rand-sample	phylo-informed-san
tournament	0.1	elite_true_agg_score	down-sample	down-sample-ances
tournament	0.1	elite_true_agg_score	down-sample	indiv-rand-sample
tournament	0.1	elite_true_agg_score	down-sample	phylo-informed-san
tournament	0.1	elite_true_agg_score	down-sample-ancestor	indiv-rand-sample
tournament	0.1	elite_true_agg_score	down-sample-ancestor	phylo-informed-san
tournament	0.1	elite_true_agg_score	indiv-rand-sample	phylo-informed-san

#### 7.3.2 Over time - Lexicase selection

#### 7.4 Manuscript figures

```
Figures customized / cleaned up for the manuscript.
```

```
build_final_score_manuscript_plot <- function(</pre>
  selection,
  subsample_rate
) {
  # Extract median values for max aggregate score at same
       evaluation level as sampling regimes
  \max_{eval} <- \max(
    filter(explore_ts_data, evals_per_gen == subsample_
       rate) $ evaluations
  full_eval_steps <- as.numeric(</pre>
    levels (
      as.factor(
        filter(explore_ts_data, eval_label == "full" &
            evaluations >= max_eval) $ evaluations # nolint:
             line\_length\_linter .
    )
  full_eval <- full_eval_steps[which.min(full_eval_steps
       - max_eval )]
  full_median_score_evals <- median(
    filter (
      explore_ts_data,
      SELECTION == selection & eval_label == "full" &
          evaluations == full_eval
    ) $max_agg_score
  plot <- explore_summary_data %%
    filter (
      eval\_label != "full" &
      SELECTION = selection &
      evals_per_gen == subsample_rate
    ) %>%
    ggplot (
      aes (
        x = eval\_label,
        y = elite_true_agg_score,
        fill = eval label
```

) +

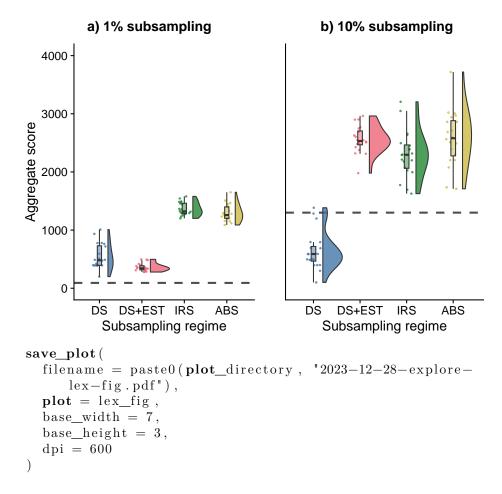
```
geom_hline(
    yintercept = full_median_score_evals ,
    size = 1.0,
    alpha = 0.7,
    color = "black"
    linetype="dashed"
  ) +
  geom_flat_violin(
    position = position\_nudge(x = .2, y = 0),
    alpha = .8,
    adjust = 1.5
  geom_point(
    mapping = aes(color = eval_label),
    position = position_jitter(width = .15),
    size = .5,
    alpha = 0.8
  ) +
  geom_boxplot(
    width = .1,
    outlier.shape = NA,
    alpha = 0.5
  ) +
  scale_y_continuous(
    name = "Aggregate_score",
    limits = c(0, 4000)
  scale_x_discrete(
    name = "Subsampling_regime",
    breaks = c("down-sample", "down-sample-ancestor", "
       indiv-rand-sample", "phylo-informed-sample"),
    labels = c("DS", "DS+EST", "IRS", "ABS")
  ) +
  scale_fill_bright() +
  scale_color_bright() +
  theme (
    legend.position = "none",
    \# axis.text.x = element\_text(
    \# angle = 30,
    #
      hjust = 1
    #),
return (plot)
```

Build end-of-run plots (fixed number of evaluations)

```
plot_final_lex_01 <- build_final_score_manuscript_plot(
   "lexicase",
   "0.01"
)
plot_final_lex_10 <- build_final_score_manuscript_plot(
   "lexicase",
   "0.1"
)</pre>
```

Combine into single figure

```
lex_fig <- plot_grid(</pre>
   plot_final_lex_01 +
      theme (
         \mathbf{plot}.\mathbf{margin} = \mathbf{margin}(1, 0, 0, 0, "cm")
   {\bf plot\_final\_lex\_10} \ +
      theme (
         axis.text.y = element_blank(),
         axis.title.y = element_blank(),
         axis.ticks.y = element_blank(),
         \mathbf{plot}.\mathbf{margin} = \mathbf{margin}(1, 0, 0, 1, "cm")
      ),
   nrow = 1,
   ncol = 2,
   align = "h",
   {\bf labels} \, = \, {\bf c} \, (\, \tt"a) \sqcup 1\% \sqcup {\bf subsampling} \, \tt" \, , \, \, \tt"b) \sqcup 10\% \sqcup {\bf subsampling} \, \tt" \, ) \, ,
   rel widths = \mathbf{c}(1, 1)
lex_fig
```



# Chapter 8

# Program synthesis experiments

```
experiment_slug <- "2023-12-30-psynth"

working_directory <- paste0(
   "experiments/",
   experiment_slug,
   "/analysis/"
)

if (exists("bookdown_wd_prefix")) {
   working_directory <- paste0(
      bookdown_wd_prefix,
      working_directory
)
}</pre>
```

# 8.1 Dependencies

```
library(tidyverse)
library(ggplot2)
library(cowplot)
library(RColorBrewer)
library(khroma)
library(rstatix)
library(knitr)
library(kableExtra)
```

```
##
## Attaching package: 'kableExtra'
## The following object is masked from 'package:dplyr':
##
##
       group_rows
source ("https://gist.githubusercontent.com/benmarwick/2
    a1bb0133ff568cbe28d/raw/
    fb53bd97121f7f9ce947837ef1a4c65a73bffb3f/geom_flat_
    violin.R")
print(version)
##
                   aarch 64-apple-darwin 20
## platform
## arch
                   aarch64
                   darwin 20
## os
## system
                   aarch64, darwin20
## status
## major
                   4
\#\# minor
                   2.1
                   2022
## year
## month
                   06
## day
                   23
## svn rev
                   82513
## language
                   \mathbf{R}
## version.string R version 4.2.1 (2022-06-23)
## nickname
                   Funny-Looking Kid
```

### 8.2 Setup

```
# Configure our default graphing theme
theme_set(theme_cowplot())
# Create a directory to store plots
plot_directory <- paste0(working_directory, "plots/")
dir.create(plot_directory, showWarnings=FALSE)</pre>
```

#### 8.2.1 Load summary data

```
summary_data_loc <- paste0(working_directory, "data/
    aggregate.csv")
summary_data <- read_csv(summary_data_loc)</pre>
```

8.2. SETUP 83

```
## Rows: 5000 Columns: 73
## — Column specification
## Delimiter: ","
## chr (11): ANCESTOR_FILE_PATH, EVAL_FIT_EST_MODE,
   EVAL_MODE, POP_INIT_MODE, P...
## dbl (62): EVAL_CPU_CYCLES_PER_TEST,
   EVAL_MAX_PHYLO_SEARCH_DEPTH, MAX_ACTIVE_...
##
## i Use 'spec()' to retrieve the full column
   specification for this data.
## i Specify the column types or set 'show_col_types =
   FALSE' to quiet this message.
summary_data <- summary_data %%
  mutate (
    eval_mode_row = case_when(
      EVAL_MODE == "full" & TEST_DOWNSAMPLE_RATE == "1" ~
           "down-sample".
      EVAL_MODE == "full" & NUM_COHORTS == "1" ~ "cohort"
      . default = EVAL\_MODE
    ),
    evals_per_gen = case_when(
      EVAL_MODE == "cohort" ~ 1.0 / NUM_COHORTS,
      EVAL_MODE == "down-sample" ~ TEST_DOWNSAMPLE_RATE,
      EVAL\_MODE == "indiv-rand-sample" ~ TEST\_DOWNSAMPLE\_
         RATE,
      EVAL_MODE == "phylo-informed-sample" ~ TEST_
         DOWNSAMPLE_RATE,
      EVAL MODE = "full" \sim 1.0
    EVAL FIT EST MODE = case when (
      EVAL_FIT_EST_MODE == "ancestor-opt" ~ "ancestor",
      EVAL_FIT_EST_MODE == "relative-opt" ~ "relative",
      . default = EVAL\_FIT\_EST\_MODE
    ),
    est_mode_with_depth = paste(
      EVAL FIT EST MODE,
      EVAL MAX PHYLO SEARCH DEPTH,
      sep = "-"
    eval_mode_est_mode_depth = paste(
      EVAL MODE,
      EVAL_FIT_EST_MODE,
```

PROBLEM,

```
EVAL MAX PHYLO SEARCH DEPTH,
     sep = "-"
   ),
   .keep = "all"
 ) %>%
 mutate (
   eval_label = case_when(
     # Clean up down-sample label
     EVAL_MODE == "down-sample" & EVAL_FIT_EST_MODE != "
         none" ~ paste("down-sample", EVAL_FIT_EST_MODE,
         sep="-"),
      .default = EVAL\_MODE
   ),
 ) %>%
 mutate (
    evals_per_gen = as.factor(evals_per_gen),
    est_mode_with_depth = as.factor(est_mode_with_depth),
   eval_mode_est_mode_depth = as.factor(eval_mode_est_
       mode_depth),
   EVAL_MAX_PHYLO_SEARCH_DEPTH = as.factor(EVAL_MAX_
       PHYLO SEARCH DEPTH),
   PROBLEM = as.factor(PROBLEM),
   SELECTION = as.factor(SELECTION),
   EVAL_MODE = as.factor(EVAL_MODE),
   NUM_COHORTS = as.factor(NUM_COHORTS) ,
   TEST_DOWNSAMPLE_RATE = as.factor(TEST_DOWNSAMPLE_RATE
   EVAL FIT EST MODE = factor(
     EVAL_FIT_EST_MODE,
     levels = c(
        "none",
        "ancestor",
        "relative"
     ),
      labels = c(
        "None",
        "Ancestor",
        "Relative"
    ),
    .keep = "all"
solution_counts <- summary_data %%
 group by(
```

8.2. SETUP 85

##

```
evals_per_gen,
    eval_mode_row,
    EVAL_FIT_EST_MODE,
    est_mode_with_depth,
    eval_mode_est_mode_depth,
    EVAL MODE,
    eval_label,
    EVAL MAX PHYLO SEARCH DEPTH
  ) %>%
  summarize (
    solution count = sum(found solution == "1"),
    replicates = n(),
    no\_solution\_count = n() - sum(found\_solution == "1")
## 'summarise()' has grouped output by 'PROBLEM', '
   evals\_per\_gen', 'eval\_mode\_row', 'EVAL\_FIT\_EST\_MODE',
    "est\_mode\_with\_depth", "eval\_mode\_est\_mode\_depth", \\
   EVAL_MODE', 'eval_label'. You can override using
## the '.groups' argument.
\# print(solution\_counts, n=208)
solution_table <- kable (solution_counts) %>%
  kable_styling(latex_options = "striped", font_size =
save_kable(solution_table, paste0(plot_directory, "
   solution_counts_table.pdf"))
solution table
# Summarize avg num selected
# -- Not totally great because weird stuff happens when a
     solution is found (population collapses, etc)
ts_data_loc <- paste0(working_directory, "data/time_
   series.csv")
ts_data <- read_csv(ts_data_loc)
## Rows: 99773 Columns: 24
## — Column specification
## Delimiter: ","
## chr (6): EVAL_FIT_EST_MODE, EVAL_MODE, PROBLEM,
   SELECTION, TESTING_SET_PATH...
## dbl (18): EVAL_MAX_PHYLO_SEARCH_DEPTH, NUM_COHORTS,
   SEED, TEST DOWNSAMPLE RA...
```

figg hugg

 $\cap$  1

PROBLEM	evals_	_per_	_gen	eval_mo	$de_{\underline{}}$
bouncing-balls	0.01			down-san	nple
bouncing-balls	0.01			down-sar	nple
bouncing-balls	0.01			indiv-ran	.d-sa
bouncing-balls	0.01			phylo-inf	orm
bouncing-balls	0.1			down-sar	nple
bouncing-balls	0.1			down-sar	nple
bouncing-balls	0.1			indiv-ran	.d-sa
bouncing-balls	0.1			phylo-inf	orm
bouncing-balls	1			full	
dice-game	0.01			down-san	nple
dice-game	0.01			down-san	nple
dice-game	0.01			indiv-ran	_
dice-game	0.01			phylo-inf	orm
dice-game	0.1			down-sar	nple
dice-game	0.1			down-sar	nple
dice-game	0.1			indiv-ran	.d-sa
dice-game	0.1			phylo-inf	orm
dice-game	1			full	
fizz-buzz	0.01			down-san	nple
fizz-buzz	0.01			down-sar	nple
fizz-buzz	0.01			indiv-ran	.d-sa
fizz-buzz	0.01			phylo-inf	orm
fizz-buzz	0.1			down-san	nple

8.2. SETUP 87

```
## i Use 'spec()' to retrieve the full column
    specification for this data.
## i Specify the column types or set 'show col types =
   FALSE' to quiet this message.
ts_data <- ts_data %%
  mutate (
    eval_mode_row = case_when(
      EVAL\_MODE = "full" \& TEST\_DOWNSAMPLE\_RATE = "1" ~
            "down-sample".
      EVAL MODE == "full" & NUM COHORTS == "1" ~ "cohort"
       . default = EVAL MODE
    ),
    evals_per_gen = case_when(
      \label{eq:eval_mode} \mbox{EVAL\_MODE} == \mbox{"cohort"} \sim 1.0 \mbox{/ NUM\_COHORTS},
      \label{eq:eval_mode} \mbox{EVAL\_MODE} = \mbox{"down-sample"} \sim \mbox{TEST\_DOWNSAMPLE\_RATE},
      EVAL_MODE == "indiv-rand-sample" ~ TEST_DOWNSAMPLE_
          RATE,
      EVAL_MODE == "phylo-informed-sample" ~ TEST_
          DOWNSAMPLE RATE,
      EVAL\_MODE == "full" \sim 1.0
    EVAL_FIT_EST_MODE = case_when(
      EVAL_FIT_EST_MODE == "ancestor-opt" ~ "ancestor",
      EVAL_FIT_EST_MODE == "relative-opt" ~ "relative",
       .default = EVAL FIT EST MODE
    est_mode_with_depth = paste(
      EVAL FIT EST MODE,
      EVAL MAX PHYLO SEARCH DEPTH,
      sep = "-"
    ),
    eval_mode_est_mode_depth = paste(
      EVAL_MODE,
      EVAL_FIT_EST_MODE,
      EVAL MAX PHYLO SEARCH DEPTH,
      sep = "-"
    .keep = "all"
  ) %>%
  mutate (
    eval_label = case_when(
       # Clean up down-sample label
      EVAL MODE == "down-sample" & EVAL FIT EST MODE != "
          none" ~ paste ("down-sample", EVAL_FIT_EST_MODE,
```

```
sep="-"),
      .default = EVAL\_MODE
   ),
 ) %>%
 mutate (
    evals_per_gen = as.factor(evals_per_gen),
    est_mode_with_depth = as.factor(est_mode_with_depth),
   eval_mode_est_mode_depth = as.factor(eval_mode_est_
       mode_depth),
   EVAL MAX_PHYLO_SEARCH_DEPTH = as.factor(EVAL_MAX_
       PHYLO SEARCH DEPTH),
   PROBLEM = as.factor(PROBLEM),
   SELECTION = as.factor(SELECTION),
   EVAL\_MODE = as.factor(EVAL\_MODE),
   NUM_COHORTS = as.factor(NUM_COHORTS),
   TEST_DOWNSAMPLE_RATE = as.factor(TEST_DOWNSAMPLE_RATE
       ),
   EVAL_FIT_EST_MODE = factor(
     EVAL_FIT_EST_MODE,
      levels = c(
        "none",
        "ancestor",
        "relative"
      ),
      labels = c(
        "None",
        "Ancestor"
        "Relative"
      )
    .keep = "all"
ts_avgs <- ts_data %%
 group_by(
   SEED,
   eval_label,
   evals_per_gen,
   PROBLEM
 ) %>%
 summarize (
   n = n(),
   avg_num_unique_selected = mean(num_unique_selected),
   avg_entropy_selected_ids = mean(entropy_selected_ids)
 ) %>%
 mutate (
```

```
eval_label = as.factor(eval_label),
    evals_per_gen = as.factor(evals_per_gen),
    PROBLEM = as.factor(PROBLEM)
)

## 'summarise()' has grouped output by 'SEED', '
    eval_label', 'evals_per_gen'. You
## can override using the '.groups' argument.
```

## 8.3 Problem-solving success statistics

```
sol_stats_data <- solution_counts %%
  filter (EVAL MODE != "full") %>%
  ungroup() %>%
  unite (
    "grouping",
   PROBLEM,
    evals_per_gen,
    sep="_"
  ) %>%
  select (
    grouping, eval_label, solution_count, no_solution_
       count
  ) %>%
  mutate (
    grouping = as. factor (grouping)
fisher_results <- data.frame(
  comparison = character(),
  group1 = character(),
  group2 = character(),
  n = integer(),
  p = double(),
  p.adj = double(),
 p.adj.signif = character()
groupings <- levels(sol_stats_data$grouping)
for (g in groupings) {
  ft_results <- sol_stats_data %%
    filter (grouping == g) %%
    select (!grouping) %%
```

```
column_to_rownames(var = "eval_label") %>%
    pairwise_fisher_test (
      p.adjust.method = "holm"
    ) %>%
    add_significance("p.adj")
  ft_results <- ft_results %%
    mutate (
      comparison = rep(g, nrow(ft_results)),
      .keep = "all"
    ) %>%
    relocate (comparison)
  fisher_results <- rbind(
    fisher_results,
    ft\_results
fisher_results <- as.tibble(fisher_results)
## Warning: 'as.tibble()' was deprecated in tibble 2.0.0.
## i Please use 'as_tibble()' instead.
## i The signature and semantics have changed, see '?
   as_tibble '.
## This warning is displayed once every 8 hours.
## Call 'lifecycle::last_lifecycle_warnings()' to see
   where this warning was generated.
fisher_results <- fisher_results %%
  mutate (
    comparison = as. factor (comparison),
    group1 = as.factor(group1),
    group2 = as.factor(group2),
  ) %>%
  group_by(
    comparison
  )
fisher_table <- kbl(fisher_results) %% kable_styling()
save_kable(fisher_table, paste0(plot_directory, "stats_
   table.pdf"))
fisher table
```

				1		
comparison	group1	group2	n	p	p.adj	p.adj.signif
bouncing-balls_0.01	down-sample	down-sample-ancestor	100	3.09e-02	1.85e-01	ns
bouncing-balls_0.01	down-sample	indiv-rand-sample	100	5.94e-02	2.97e-01	ns
bouncing-balls_0.01	down-sample	phylo-informed-sample	100	3.62e-01	1.00e+00	ns
bouncing-balls_0.01	down-sample-ancestor	indiv-rand-sample	100	1.00e+00	1.00e+00	ns
bouncing-balls_0.01	down-sample-ancestor	phylo-informed-sample	100	3.57e-01	1.00e+00	ns
bouncing-balls_0.01	indiv-rand-sample	phylo-informed-sample	100	5.25e-01	1.00e+00	ns
bouncing-balls_0.1	down-sample	down-sample-ancestor	100	1.17e-01	7.02e-01	ns
bouncing-balls_0.1	down-sample	indiv-rand-sample	100	4.95e-01	1.00e+00	ns
bouncing-balls_0.1	down-sample	phylo-informed-sample	100	2.42e-01	1.00e+00	ns
bouncing-balls_0.1	down-sample-ancestor	indiv-rand-sample	100	6.78e-01	1.00e+00	ns
bouncing-balls_0.1	down-sample-ancestor	phylo-informed-sample	100	1.00e+00	1.00e+00	ns
bouncing-balls_0.1	indiv-rand-sample	phylo-informed-sample	100	1.00e+00	1.00e+00	ns
$dice-game\_0.01$	down-sample	down-sample-ancestor	100	0.00e+00	0.00e+00	****
$dice-game\_0.01$	down-sample	indiv-rand-sample	100	0.00e+00	0.00e+00	****
$dice-game\_0.01$	down-sample	phylo-informed-sample	100	0.00e+00	0.00e+00	****
$dice-game\_0.01$	down-sample-ancestor	indiv-rand-sample	100	1.00e+00	1.00e+00	ns
$dice-game\_0.01$	down-sample-ancestor	phylo-informed-sample	100	4.19e-01	9.42e-01	ns
dice-game_0.01	indiv-rand-sample	phylo-informed-sample	100	3.14e-01	9.42e-01	ns
dice-game_0.1	down-sample	down-sample-ancestor	100	1.00e+00	1.00e+00	ns
dice-game_0.1	down-sample	indiv-rand-sample	100	5.21e-01	1.00e+00	ns
dice-game_0.1	down-sample	phylo-informed-sample	100	1.00e+00	1.00e+00	ns
dice-game_0.1	down-sample-ancestor	indiv-rand-sample	100	3.95e-01	1.00e+00	ns
dice-game_0.1	down-sample-ancestor	phylo-informed-sample	100	1.00e+00	1.00e+00	ns
dice-game_0.1	indiv-rand-sample	phylo-informed-sample	100	5.21e-01	1.00e+00	ns
fizz-buzz_0.01	down-sample	down-sample-ancestor	100	2.62e-01	5.24e-01	ns
fizz-buzz_0.01	down-sample	indiv-rand-sample	100	8.60e-06	4.28e-05	****
fizz-buzz_0.01	down-sample	phylo-informed-sample	100	2.00e-07	1.20e-06	****
fizz-buzz_0.01	down-sample-ancestor	indiv-rand-sample	100	1.59e-03	4.77e-03	**
fizz-buzz_0.01	down-sample-ancestor	phylo-informed-sample	100	8.31e-05	3.32e-04	***
fizz-buzz_0.01	indiv-rand-sample	phylo-informed-sample	100	5.46e-01	5.46e-01	ns
fizz-buzz_0.1	down-sample	down-sample-ancestor	100	8.03e-01	8.38e-01	ns
fizz-buzz_0.1	down-sample	indiv-rand-sample	100	9.55e-05	4.78e-04	***
fizz-buzz_0.1	down-sample	phylo-informed-sample	100	3.46e-03	1.04e-02	*
fizz-buzz 0.1	down-sample-ancestor	indiv-rand-sample	100	1.26e-05	7.56e-05	****
fizz-buzz 0.1	down-sample-ancestor	phylo-informed-sample	100	6.80e-04	2.72e-03	**
fizz-buzz_0.1	indiv-rand-sample	phylo-informed-sample	100	4.19e-01	8.38e-01	ns
for-loop-index_0.01	down-sample	down-sample-ancestor	100	0.00e+00	0.00e+00	****
for-loop-index_0.01	down-sample	indiv-rand-sample	100	0.00e+00	0.00e+00	****
for-loop-index 0.01	down-sample	phylo-informed-sample	100	0.00e+00	0.00e+00	****
for-loop-index 0.01	down-sample-ancestor	indiv-rand-sample	100	1.12e-01	2.24e-01	ns
for-loop-index_0.01	down-sample-ancestor	phylo-informed-sample	100	2.67e-02	8.01e-02	ns
for-loop-index_0.01	indiv-rand-sample	phylo-informed-sample	100	1.00e+00	1.00e+00	ns
for-loop-index_0.1	down-sample	down-sample-ancestor	100	2.98e-01	1.00e+00	ns
for-loop-index_0.1	down-sample	indiv-rand-sample	100	6.82e-01	1.00e+00	ns
for-loop-index_0.1	down-sample	phylo-informed-sample	100	8.40e-01	1.00e+00	ns
for-loop-index_0.1	down-sample-ancestor	indiv-rand-sample	100	6.71e-01	1.00e+00	ns
for-loop-index_0.1	down-sample-ancestor	phylo-informed-sample	100	1.49e-01	8.94e-01	ns
for-loop-index_0.1	indiv-rand-sample	phylo-informed-sample	100	4.16e-01	1.00e+00	ns
gcd_0.01	down-sample	down-sample-ancestor	100	2.31e-04	9.24e-04	***
$\frac{\text{gcd}\_0.01}{\text{gcd}\_0.01}$	down-sample	indiv-rand-sample	100	1.20e-06	5.90e-06	****
$\frac{\text{gcd\_0.01}}{\text{gcd\_0.01}}$	down-sample	phylo-informed-sample	100	1.20c-00 1.00e-07	4.00e-07	****
gcd_0.01	down-sample-ancestor	indiv-rand-sample	100	2.75e-01	5.50e-01	
<u> </u>		_				ns
gcd_0.01	down-sample-ancestor	phylo-informed-sample	100	8.81e-02	2.64e-01	ns

# 8.4 Average number of unique candidates selected

```
full_avgs <- ts_data %%
  filter (eval_label == "full") %%
 group_by(PROBLEM) %>%
 summarize (
   n = n()
   median_num_unique_selected = median(num_unique_
       selected),
   median_entropy_selected_ids = median(entropy_selected
       _ids),
   avg_num_unique_selected = mean(num_unique_selected),
   avg_entropy_selected_ids = mean(entropy_selected_ids)
build_plot_summary_data <- function(
 data,
 response
 plot <- data %%
    filter (
      eval_label != "full"
    ) %>%
   ggplot (
      aes_string(
       x = "eval\_label",
        y = response,
        fill = "eval\_label"
    ) +
   geom_flat_violin(
      position = position\_nudge(x = .2, y = 0),
      alpha = .8,
      adjust = 1.5
    ) +
   geom_point(
      mapping = aes(color = eval_label),
      position = position_jitter(width = .15),
      size = .5,
      alpha = 0.8
   geom_boxplot(
      width = .1,
```

```
outlier.shape = NA,
      alpha = 0.5
    ) +
    scale_y_continuous(
      \# \ limits = c(-0.5, 100)
    scale_fill_bright() +
    scale_color_bright() +
    facet grid(
      PROBLEM ~ evals_per_gen,
      \# nrow = 2,
      labeller = label\_both
    ) +
    theme (
      legend.position = "none",
      axis.text.x = element_text(
        angle = 30,
        hjust = 1
      ),
      panel.border = element_rect(color = "gray", size =
    )
  return (plot)
plt <- build_plot_summary_data(
  ts avgs,
  "avg_num_unique_selected"
ggsave (
  filename = paste0(plot_directory, "avg_num_unique_
      selected.pdf"),
  plot = plt
## Saving 6.5 \times 4.5 in image
plt <- build_plot_summary_data(
  ts_avgs,
  "avg_entropy_selected_ids"
ggsave (
  filename = paste0(plot_directory, "avg_entropy_selected
     _ids.pdf"),
  plot = plt
```

```
94 CHAPTER 8. PROGRAM SYNTHESIS EXPERIMENTS ) \#\# \  \, \text{Saving} \  \, 6.5 \  \, \text{x} \  \, 4.5 \  \, \text{in image}
```