

# HUFFMAN CODING

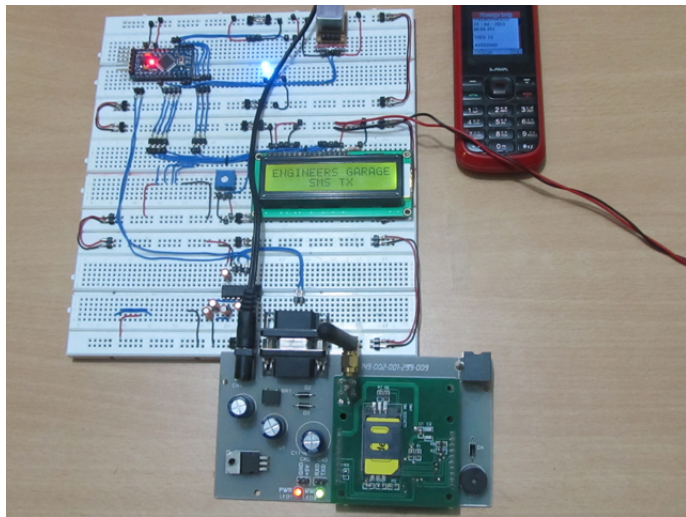


COMPRESSION ALGORITHM

# Huffman Coding

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And  
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May 23, 2015



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*How To Solve This Problem???*

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*Can we minimize the number of bits for representing the character?*

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**Yes**

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**How.....???**



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**Yes**

**How.....???**

We can solve this problem using **Huffman Coding**

# Principle of Huffman Coding

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- **Huffman Coding** works in **Greedy Approach**

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- **Huffman Coding** works in **Greedy Approach**
- It focuses on **frequency** of each character appearing in the text to construct an optimal binary representation of the characters.

# Greedy Approach

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- Example: 'Activity Selection Problem' , 'Coin Changing Problem' , 'Fractional Knapsack Problem' etc

# Retriving Lowest Frequency Of Characters



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To implement this technique Huffman Algorithm uses Priority Queue

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## Concepts Of Priority Queue

- Is an abstract data type like array where additionally each element has a "priority" associated with it.
- An element with high priority is served before an element with low priority
- If two elements have the same priority, they are served according to their order in the queue.

# Back To Huffman Coding

- Is a procedure to generate a binary code tree
- this was invented by David Huffman in 1952

# Huffman Coding Algorithm

- Initialization: put all symbols on a list sorted according to their frequency counts
- Repeat until the list has only one symbol left:
  - a) From the list pick two symbols with the lowest frequency counts
  - b) From a Huffman sub-tree that has these two symbols as child nodes and create a parent node
  - c) Assign the sum of the children's frequency counts to the parent and insert it into the list such that the order is maintained
  - d) Delete the children from the list
- Assign A codeword for each leaf based on the path from the root

## Continued....

```
n = |C|
Q = C
for i =1 to n-1:
    allocate a new node z
    z.left = x= EXTRACT-MIN(Q)
    z.right = y = EXTRACT-MIN(Q)
    z.freq = x.freq + y.freq
    Insert(Q,z)
return EXTRACT-MIN(Q)
```

# Number of Bits

To encode a file , the total number of bits ,  $B(T) = \sum c.freq * d_t(c)$

Where T is the encoded tree  
c belongs to the character set

# Back To The MISSISSIPPI RIVER

**Splitting the word**

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**Splitting the word**

<b>M</b>	<b>I</b>	<b>S</b>	<b>P</b>	<b>R</b>	<b>V</b>	<b>E</b>	<b>""</b>
<b>1</b>	<b>5</b>	<b>4</b>	<b>2</b>	<b>2</b>	<b>1</b>	<b>1</b>	<b>1</b>



# Back To The MISSISSIPPI RIVER

**Splitting the word**

<b>M</b>	<b>I</b>	<b>S</b>	<b>P</b>	<b>R</b>	<b>V</b>	<b>E</b>	<b>"""</b>
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**Decending Order of Numbers**

<b>I</b>	<b>S</b>	<b>P</b>	<b>R</b>	<b>M</b>	<b>V</b>	<b>E</b>	<b>"""</b>
<b>5</b>	<b>4</b>	<b>2</b>	<b>2</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>

# Before Huffman Coding Tree:

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$$5*8+4*8+2*8+2*8+1*8+1*8+1*8+1*8=136$$

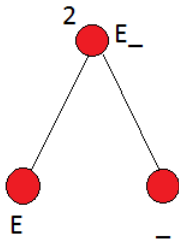
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$$5*8+4*8+2*8+2*8+1*8+1*8+1*8+1*8=136$$

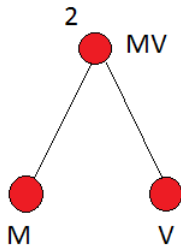
Huge!!!!

# Graphical Overview Of Huffman Coding

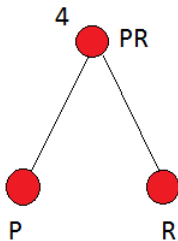
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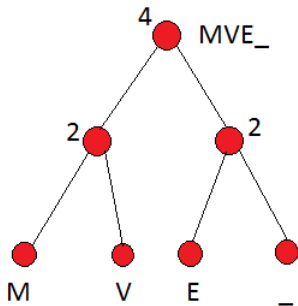


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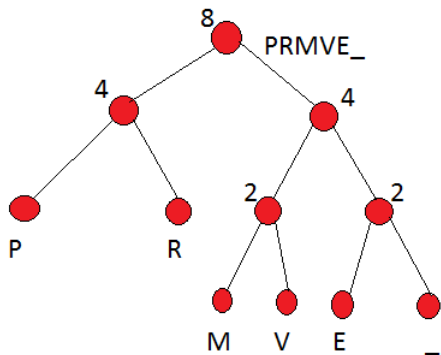




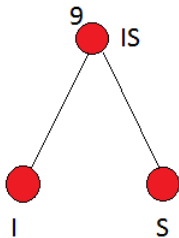
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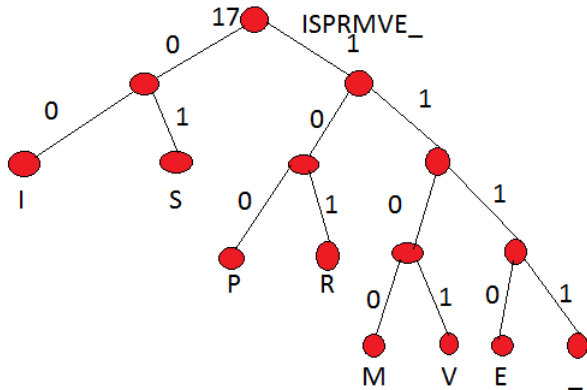
# Graphical Overview Of Huffman Coding



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# Finally ....

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<b>I</b>	<b>S</b>	<b>P</b>	<b>R</b>	<b>M</b>	<b>V</b>	<b>E</b>	<b>""</b>
<b>00</b>	<b>01</b>	<b>100</b>	<b>101</b>	<b>1100</b>	<b>1101</b>	<b>1110</b>	<b>1111</b>

# After Huffman Coding Tree

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Number of bits=

$$5*2+4*2+2*3+2*3+4*1+4*1+4*1+4*1=46$$



# After Huffman Coding Tree

Number of bits=

$$5*2+4*2+2*3+2*3+4*1+4*1+4*1+4*1=46$$

**Improvement:** 66.2%

# Complexity

- time complexity is  $n \log n$
- can be improved by using Van Embde Boss

# Usefulness

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- Easy To decode

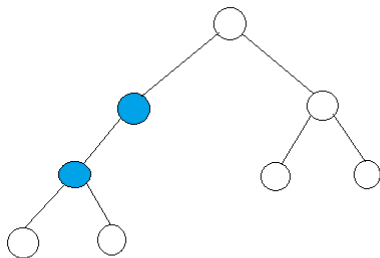
# Usefulness

- Easy To decode
- Prefix free code

# Usefulness

- Easy To decode
- Prefix free code
- The tree generated by Huffman Code is a Full Binary Tree

# Full Binary Tree



Message sent!



# Resources

Introduction To Algorithms by Thomas H. Cormen ,  
Charles E. Leiserson , Ronald L. Rivest, Clifford Stein.