## 3D IMAGE (VOLUME) ORIENTATION AND LOCATION IN SPACE:

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There are 3 different methods by which continuous coordinates can

attached to voxels. The discussion below emphasizes 3D volumes, and

the continuous coordinates are referred to as (x,y,z). The voxel

index coordinates (i.e., the array indexes) are referred to as (i,j,k),

with valid ranges:

$$i = 0 ... dim[1]-1$$
  
 $j = 0 ... dim[2]-1$  (if  $dim[0] >= 2$ )

k = 0 .. dim[3]-1 (if dim[0] >= 3)

The (x,y,z) coordinates refer to the CENTER of a voxel. In methods

2 and 3, the (x,y,z) axes refer to a subject-based coordinate system,

with

+x = Right +y = Anterior+z = Superior.

This is a right-handed coordinate system. However, the exact direction

these axes point with respect to the subject depends on qform code

(Method 2) and sform\_code
(Method 3).

N.B.: The i index varies most rapidly, j index next, k index

slowest.

Thus, voxel (i,j,k) is stored starting at location (i + j\*dim[1] + k\*dim[1]\*dim[2]) \* (bitpix/8) into the dataset array.

N.B.: The ANALYZE 7.5
coordinate system is
 +x = Left +y = Anterior
+z = Superior

which is a left-handed coordinate system. This backwardness is

too difficult to tolerate, so this NIFTI-1 standard specifies the

coordinate order which is most common in functional neuroimaging.

N.B.: The 3 methods below all

give the locations of the voxel centers

in the (x,y,z) coordinate system. In many cases, programs will wish

to display image data on some other grid. In such a case, the program

will need to convert its
desired (x,y,z) values into
(i,j,k) values

in order to extract (or interpolate) the image data. This operation

would be done with the inverse transformation to those described below.

N.B.: Method 2 uses a factor 'qfac' which is either -1 or 1; qfac is

stored in the otherwise

unused pixdim[0]. If
pixdim[0]=0.0 (which

should not occur), we take qfac=1. Of course, pixdim[0] is only used

when reading a NIFTI-1 header, not when reading an ANALYZE 7.5 header.

In NIFTI-1 files, dimensions 1,2,3 are for space, dimension 4 is for time,

and dimension 5 is for storing multiple values at each spatiotemporal

voxel. Some examples:

- A typical whole-brain
  FMRI experiment's time series:
  - $-\dim[0] = 4$
  - $\dim[1] = 64$

pixdim[1] = 3.75 xyzt\_units =
NIFTI\_UNITS\_MM

```
- \dim[2] = 64
pixdim[2] = 3.75
NIFTI UNITS SEC
        - \dim[3] = 20
pixdim[3] = 5.0
        - \dim[4] = 120
pixdim[4] = 2.0
     - A typical T1-weighted
anatomical volume:
        -\dim[0] = 3
        - dim[1] = 256
pixdim[1] = 1.0 xyzt units =
NIFTI UNITS MM
        - \dim[2] = 256
pixdim[2] = 1.0
        - \dim[3] = 128
pixdim[3] = 1.1
     - A single slice EPI time
series:
        -\dim[0] = 4
        - dim[1] = 64
pixdim[1] = 3.75 xyzt units =
```

```
NIFTI UNITS MM
        - \dim[2] = 64
pixdim[2] = 3.75
NIFTI UNITS SEC
        - \dim[3] = 1
pixdim[3] = 5.0
        - \dim[4] = 1200
pixdim[4] = 0.2
     - A 3-vector stored at each
point in a 3D volume:
        -\dim[0] = 5
        - \dim[1] = 256
pixdim[1] = 1.0 xyzt units =
NIFTI UNITS MM
        - \dim[2] = 256
pixdim[2] = 1.0
        - \dim[3] = 128
pixdim[3] = 1.1
        -\dim[4] = 1
pixdim[4] = 0.0
        - \dim[5] = 3
intent code =
```

```
NIFTI INTENT VECTOR
     - A single time series with
a 3x3 matrix at each point:
        - \dim[0] = 5
        - \dim[1] = 1
xyzt units = NIFTI_UNITS_SEC
        - \dim[2] = 1
        -\dim[3] = 1
        - \dim[4] = 1200
pixdim[4] = 0.2
        -\dim[5] = 9
intent code =
NIFTI INTENT GENMATRIX
        - intent_p1 = intent_p2
= 3.0 (indicates matrix
dimensions)
____*/
```

METHOD 2 (used when qform\_code >
0, which should be the "normal"
case):

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The (x,y,z) coordinates are given by the pixdim[] scales, a rotation

matrix, and a shift. This

method is intended to represent "scanner-anatomical" coordinates, which are often embedded in the image header (e.g., DICOM fields (0020,0032), (0020,0037), (0028,0030),and (0018,0050), and represent the nominal orientation and location of

the data. This method can

also be used to represent
"aligned"

coordinates, which would typically result from some post-acquisition

alignment of the volume to a standard orientation (e.g., the same

subject on another day, or a rigid rotation to true anatomical

orientation from the tilted position of the subject in the scanner).

The formula for (x,y,z) in terms of header parameters and (i,j,k) is:

```
[ x ] [ R11 R12 R13 ]
[ pixdim[1] * i ]
[ qoffset_x ]
[ y ] = [ R21 R22 R23 ]
```

The qoffset\_\* shifts are in the NIFTI-1 header. Note that the center

of the (i,j,k)=(0,0,0) voxel (first value in the dataset array) is
 just

(x,y,z)=(qoffset\_x,qoffset\_y,qof
fset\_z).

The rotation matrix R is calculated from the quatern\_\* parameters.

This calculation is described below.

The scaling factor qfac is either 1 or -1. The rotation matrix R

defined by the quaternion parameters is "proper" (has determinant 1).

This may not fit the needs of the data; for example, if the image

grid is

i increases from Left-to-

Right

j increases from Anteriorto-Posterior

k increases from Inferiorto-Superior

Then (i,j,k) is a left-handed triple. In this example, if qfac=1,

the R matrix would have to be

[ 1 0 0]

```
[ 0 -1 0 ] which is "improper" (determinant = -1).
[ 0 0 1 ]
```

If we set qfac=-1, then the R matrix would be

```
[ 1 0 0]
[ 0 -1 0] which is
```

 $[ \quad 0 \quad 0 \quad -1 \quad ]$ 

proper.

This R matrix is represented by quaternion [a,b,c,d] = [0,1,0,0]

(which encodes a 180 degree rotation about the x-axis).