

3D IMAGE (VOLUME) ORIENTATION AND LOCATION IN SPACE:

There are 3 different methods by which continuous coordinates can

attached to voxels. The discussion below emphasizes 3D volumes, and

the continuous coordinates are referred to as (x,y,z). The voxel

index coordinates (i.e., the array indexes) are referred to as (i,j,k),

with valid ranges:

i = 0 .. dim[1]-1

j = 0 .. dim[2]-1 (if dim[0] >= 2)

k = 0 .. dim[3]-1 (if dim[0] >= 3)

The (x,y,z) coordinates refer to the CENTER of a voxel. In methods

2 and 3, the (x,y,z) axes refer to a subject-based coordinate system,

with

+x = Right +y = Anterior +z = Superior.

This is a right-handed coordinate system. However, the exact direction

these axes point with respect to the subject depends on qform_code

(Method 2) and sform_code (Method 3).

N.B.: The i index varies most rapidly, j index next, k index slowest.

Thus, voxel (i,j,k) is stored starting at location

(i + j*dim[1] + k*dim[1]*dim[2]) * (bitpix/8)

into the dataset array.

N.B.: The ANALYZE 7.5 coordinate system is

+x = Left +y = Anterior +z = Superior

which is a left-handed coordinate system. This backwardness is

too difficult to tolerate, so this NIFTI-1 standard specifies the

coordinate order which is most common in functional neuroimaging.

N.B.: The 3 methods below all give the locations of the voxel centers

in the (x,y,z) coordinate system. In many cases, programs will wish

to display image data on some other grid. In such a case,

the program

will need to convert its desired (x,y,z) values into (i,j,k) values

in order to extract (or interpolate) the image data. This operation

would be done with the inverse transformation to those described below.

N.B.: Method 2 uses a factor 'qfac' which is either -1 or 1; qfac is

stored in the otherwise unused pixdim[0]. If pixdim[0]=0.0 (which

should not occur), we take qfac=1. Of course, pixdim[0] is only used

when reading a NIFTI-1 header, not when reading an ANALYZE 7.5 header.

In NIFTI-1 files, dimensions 1,2,3 are for space, dimension 4 is for time,

and dimension 5 is for storing multiple values at each spatiotemporal

voxel. Some examples:

- A typical whole-brain fMRI experiment's time series:

- dim[0] = 4

- dim[1] = 64 pixdim[1] = 3.75 xyzt_units =

NIFTI_UNITS_MM

- dim[2] = 64 pixdim[2] = 3.75 |

NIFTI_UNITS_SEC

- dim[3] = 20 pixdim[3] = 5.0

- dim[4] = 120 pixdim[4] = 2.0

- A typical T1-weighted anatomical volume:

- dim[0] = 3

- dim[1] = 256 pixdim[1] = 1.0 xyzt_units =

NIFTI_UNITS_MM

- dim[2] = 256 pixdim[2] = 1.0

- dim[3] = 128 pixdim[3] = 1.1

- A single slice EPI time series:

- dim[0] = 4

- dim[1] = 64 pixdim[1] = 3.75 xyzt_units =

NIFTI_UNITS_MM

- dim[2] = 64 pixdim[2] = 3.75 |

NIFTI_UNITS_SEC

- dim[3] = 1 pixdim[3] = 5.0

- dim[4] = 1200 pixdim[4] = 0.2

- A 3-vector stored at each point in a 3D volume:

- dim[0] = 5

- dim[1] = 256 pixdim[1] = 1.0 xyzt_units =

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NIFTI_UNITS_MM
    - dim[2] = 256   pixdim[2] = 1.0
    - dim[3] = 128   pixdim[3] = 1.1
    - dim[4] = 1     pixdim[4] = 0.0
    - dim[5] = 3     intent_code =
NIFTI_INTENT_VECTOR
    - A single time series with a 3x3 matrix at each point:
    - dim[0] = 5
    - dim[1] = 1     xyzt_units =
NIFTI_UNITS_SEC
    - dim[2] = 1
    - dim[3] = 1
    - dim[4] = 1200 pixdim[4] = 0.2
    - dim[5] = 9     intent_code =
NIFTI_INTENT_GENMATRIX
    - intent_p1 = intent_p2 = 3.0   (indicates matrix
dimensions)
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METHOD 2 (used when qform_code > 0, which should be the "normal" case):

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The (x,y,z) coordinates are given by the pixdim[] scales, a rotation

matrix, and a shift. This method is intended to represent "scanner-anatomical" coordinates, which are often embedded in the

image header (e.g., DICOM fields (0020,0032), (0020,0037), (0028,0030),

and (0018,0050)), and represent the nominal orientation and

location of

the data. This method can also be used to represent
"aligned"

coordinates, which would typically result from some post-
acquisition

alignment of the volume to a standard orientation (e.g., the
same

subject on another day, or a rigid rotation to true
anatomical

orientation from the tilted position of the subject in the
scanner).

The formula for (x,y,z) in terms of header parameters and
(i,j,k) is:

$$\begin{aligned} \begin{bmatrix} x \\ \text{qoffset_x} \end{bmatrix} &= \begin{bmatrix} R11 & R12 & R13 \end{bmatrix} \begin{bmatrix} \text{pixdim}[1] * i \\ \text{qoffset_y} \end{bmatrix} \\ \begin{bmatrix} y \\ \text{qoffset_y} \end{bmatrix} &= \begin{bmatrix} R21 & R22 & R23 \end{bmatrix} \begin{bmatrix} \text{pixdim}[2] * j \\ \text{qoffset_z} \end{bmatrix} + \\ \begin{bmatrix} z \\ \text{qoffset_z} \end{bmatrix} &= \begin{bmatrix} R31 & R32 & R33 \end{bmatrix} \begin{bmatrix} \text{qfac} * \text{pixdim}[3] * k \end{bmatrix} \end{aligned}$$

The qoffset_* shifts are in the NIFTI-1 header. Note that
the center

of the $(i,j,k)=(0,0,0)$ voxel (first value in the dataset array) is

just $(x,y,z)=(qoffset_x,qoffset_y,qoffset_z)$.

The rotation matrix R is calculated from the `quatern_*` parameters.

This calculation is described below.

The scaling factor `qfac` is either 1 or -1. The rotation matrix R

defined by the quaternion parameters is "proper" (has determinant 1).

This may not fit the needs of the data; for example, if the image

grid is

i increases from Left-to-Right

j increases from Anterior-to-Posterior

k increases from Inferior-to-Superior

Then (i,j,k) is a left-handed triple. In this example, if `qfac=1`,

the R matrix would have to be

$$\begin{bmatrix} 1 & 0 & 0 \end{bmatrix}$$

$\begin{bmatrix} 0 & -1 & 0 \end{bmatrix}$ which is "improper" (determinant = -1).

$\begin{bmatrix} 0 & 0 & 1 \end{bmatrix}$

If we set $qfac=-1$, then the R matrix would be

$\begin{bmatrix} 1 & 0 & 0 \end{bmatrix}$

$\begin{bmatrix} 0 & -1 & 0 \end{bmatrix}$ which is proper.

$\begin{bmatrix} 0 & 0 & -1 \end{bmatrix}$

This R matrix is represented by quaternion $[a,b,c,d] =$
 $[0,1,0,0]$

(which encodes a 180 degree rotation about the x-axis).