

# Deep Generative Modeling

used to create synthetic data

## So far Supervised Learning

Data:  $(x, y)$

$x$  is data,  $y$  is label

Goal: Learn function to map  
 $x \rightarrow y$

Examples: Classification, regression,

Object detection, semantic segmentation

## This topic: UnSupervised Learning

Data:  $\mathcal{D}$

$x$  is data, no labels!

Goal: Learn the hidden or underlying structure of data

E.g. Clustering, dimensionality reduction, allow insight to fundamental structure of data. This can be used to generate data.

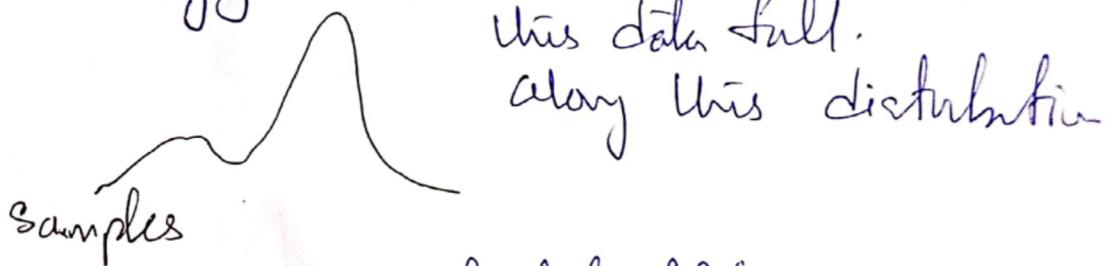
## Generative Modeling (Unsupervised Learning)

Goal: Take as input training samples from some distribution and learn a model that represents distribution of the model

### 1) Density Estimation:

Given a set of data samples they fall according to some density.

The task of GAN is to learn the underlying PDF that describe how this data fall.



We can understand PDF and we can use this information to generate new synthetic samples

We are considering some input examples that fall and are drawn from same training data distribution

generate synthetic examples

2) <u>Sample Generation</u>	Input Samples	Generated Samples
Training data $\sim P_{\text{data}}(x)$		Generated $\sim P_{\text{model}}(x)$

How can we learn  $P_{\text{model}}(x)$  similar to  $P_{\text{data}}(x)$ . ?

GANs enable us automatically uncover underlying features in a dataset.

How these features are distributed within a dataset.

Question: How can we learn probability distribution using our model.

### GANs Applications:

- 1) automatically uncover underlying features in a dataset.  
given a facial dataset. We need to group according features (skin color)  
dataset may be biased.  
data can be sampled accordingly

(GANs

2) Outlier detection:

Self driving car:

Resultant model can be better equipped.

Problem: How can we detect when we encounter something new

Strategy: detect outliers using GAN  
Use outliers during training.

Labeled

Latent Variable:

A variable which is not directly measured but is inferred e.g. happiness or quality of life.

Can we learn the true explanatory factors e.g. latent variables.

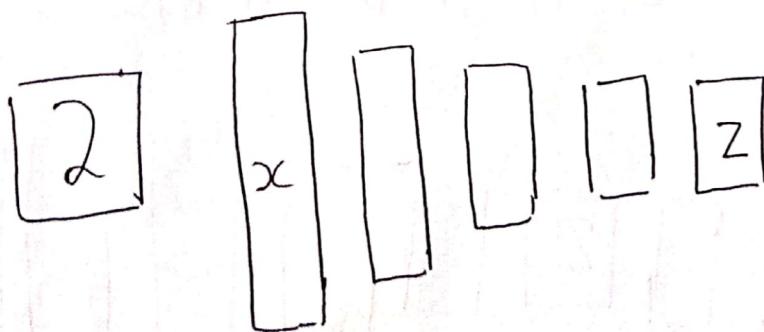
find ways of actually Learning hidden latent variables.

NN can handle multi-dimensional datasets and learn combinations of non-linear functions that can approximate complex data distributions.

A. Simple Model: which can learn by self-encoding the input Auto Encoders

Auto Encoders:

Unsupervised approach for learning a low-dimensional feature representation from unlabelled training data



Encoder learns mapping from the data  $x$ , to a Low-dimensional Latent Space,  $z$

Latent Cave example:

shadows

Why do we ~~care about~~ need to ensure that  $z$  has low-dimensional data?

Encoder: Mapping (data) to a low-dimensional latent data  $z$ .

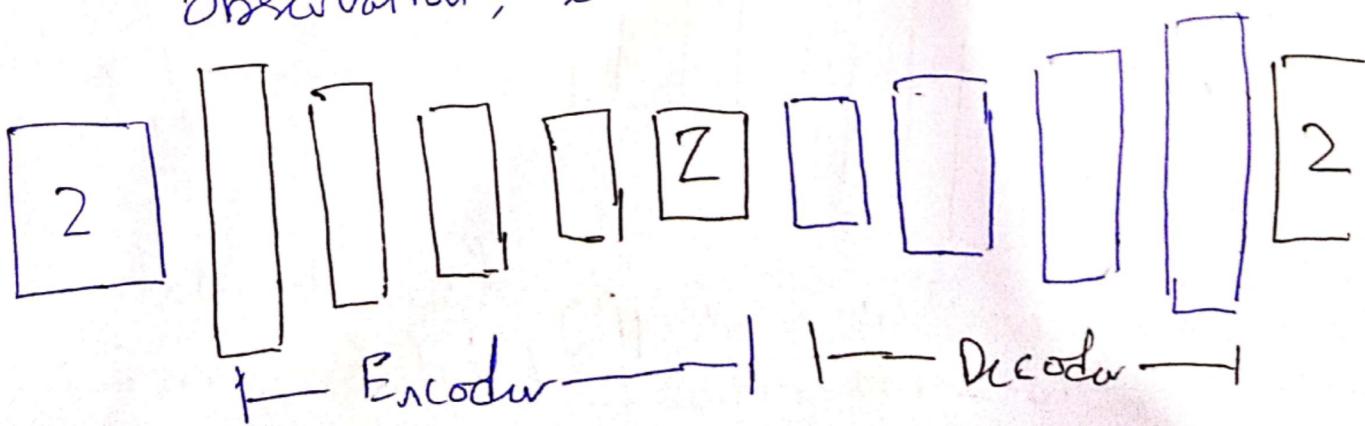
Low dimensions: able to compress into a small latent factor, we can learn compact feature representation.

How can we train?

Data is unlabelled.

- Use a Decoder
- Train the model to use these features to reconstruct the original data.

Decoder: Learns mapping back from latent space,  $z$ , to a reconstructed observation,  $\hat{x}$



Decoder portion of the Auto Encoder  
is going to be a series of NN layers.  
take this hidden layer and map it  
back to the hidden space.

$\hat{x} \rightarrow$  estimated

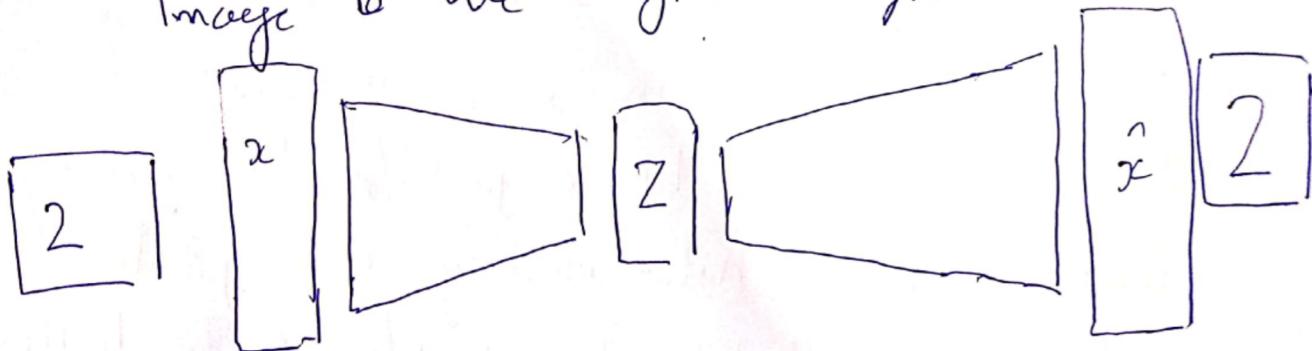
$$L(z, \hat{x}) = \|x - \hat{x}\|^2$$

Loss function  
does not use  
any labels.

loss function: RMS E

for images, subtract one image from  
the another and squaring the difference  
pixel-wise difference of images.

Measure how close our reconstructed  
image to the original image.



we cannot observe  $z'$

Dimensionality is important in re-construction  
of input.

Auto encoding is a form of compression  
Smaller latent space will force a larger  
training bottleneck.

2D latent space might ~~be~~ have higher loss as compared to 5D

Information bottleneck

lower dimensions  $\rightarrow$  poor quality

Auto encoders for representation Learning

Auto encoder ~~complex~~ ~~representation~~ can limit nodes in Bottleneck hidden layer: forces network to learn a ~~compromised~~ compressed latent representation.

without presence of bottleneck layer, network could simply learn to memorize the input values.

Reconstruction Loss: forces the latent representation to capture (or encode) as much "information" about the data as possible. Diff b/w original i/p and encoded i/p

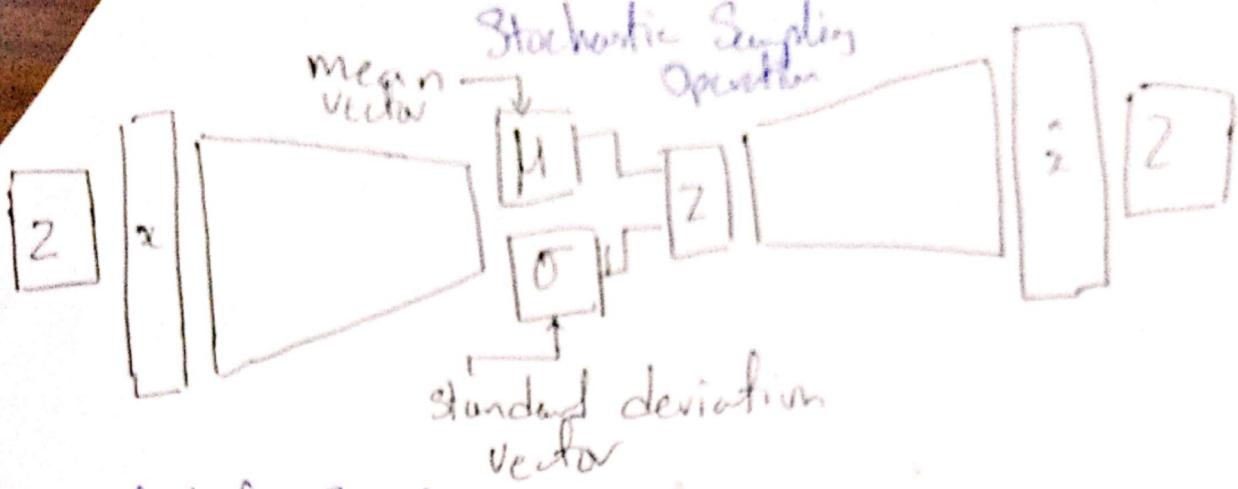
Auto encoding = Automatically encoding data

~~But~~ autoencoder holds variations in i/p without holding redundancies

VARIATIONAL Auto encoders

impose a variational stochastic twist

- generate smoother representations of the input data
  - improve the quality of reconstruction
  - generate new images similar to the input dataset. (not just direct reconstruction of the i/p data)
- stochastic sampling operation



Ideal Auto Encoder:

- Sensitive to the inputs to build reconstruction
- Insensitive to the inputs that the model does not memorize or overfit training data

$h(x, \hat{x}) + \text{regularizer} \rightarrow$  discovery  
memorization

Instead of the latent variable directly VAEs learn the mean and variance associated with that variable. They parameterized association for that latent variable instead of learning a vector of latent variables, we learn a vector of mean and standard deviation of latent variables and define

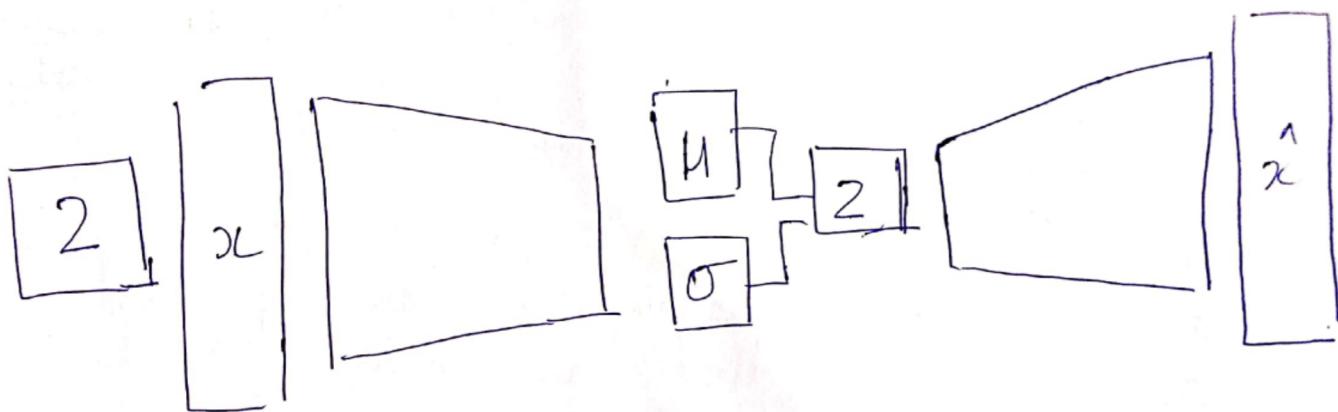
They parameterized probability distribution for that variable.

Traditional Auto Encoders are deterministic. O/P<sup>is</sup> single value for each encoding dimension.

Variational auto encoders are a probabilistic twist on auto encoders. A probability distribution for each latent variable. Sample from the mean and standard deviation to compute the latent sample.

probabilistic twist to compute sample information ↗

Encoder and decoder are now probabilistic



Encoder computes  $q_{\phi}(z|x)$       Decoder computes  
 $p_{\theta}(x|z)$

Performing sampling information to  
sample each of the latent variables

Encoder is now try to learn a PDF  
of latent distribution  $z$  given the  
data  $x$ .