PHYS430 - Thermal Physics

Alfaifi, Ammar

Chapter 1

Energy in Thermal Physics

1.1 Thermal Equilibrium

- After two objects have been in contact long enough, we say that they are in **thermal equilibrium**.
- The time required for a system to come to thermal equilibrium is called the **relaxation time**.
- **Temperature** is a measure of the tendency of an object to spontaneously give up energy to its surroundings.
- The flow of energy is from the object with a higher temperature to the lower on.
- For low-density gas at constant pressure, the volume should go to zero at approximately -273° C. which defines the absolute zero, in the absolute temperature scale, in K (kelvin).

1.2 The Ideal Gas

$$PV = nRT; R = 8.31 \text{ J/mol K} (1.1)$$

- A mole of molecules is Avogadro's number of them, 6.02×10^{23} .
- Number of molecules is $N = n \times N_A$
- Ideal gas law becomes PV = NkT, where k is Boltzmann's constant.
- The average transnational kinetic energy is $\bar{K}_{\text{trans}} = \frac{3}{2}kT$, where $kT = \frac{1}{40}\text{eV}$

1.3 Equipartition of Energy

Equipartition theorem At a temperature T, the average energy of any quadratic degree of freedom is $\frac{1}{2}kT$. For a system of N molecules, each with f degree of freedom, and there are no other (non-quadratic) temperature-dependent forms of energy, then its **total thermal energy** is

$$U = Nf \frac{1}{2}kT \tag{1.2}$$

Note, This is the average total thermal energy, but for large N, fluctuations become negligible.

1.4 Heat and Work

- Total amount of energy in the universe never changes, Conservation of energy
- Heat any spontaneous flow of energy form on e object to another, caused by difference in temperature.
- Work, in thermodynamics, is any other transfer of energy into or out of a system.
- Work and heat refer to energy in transit.
- The total energy in a system is determined, but not the work nor the heat, it's meaningless.
- We ask about how much heat entered a system and how much work was done on a system.
- $\Delta U = Q + W$ is just a statement of the law of conservation of energy, but it's still called **first law of thermodynamics**.
- Processes of heat transfer: Conduction, Convection, and Radiation.

1.5 Commpression Work

- From classical mmechanics work is $W = \vec{F} \cdot d\vec{r}$
- Consider compressing gas with a piston of area A a distance Δx , the change in volume is $\Delta V = -A\Delta x$
- Volume change should be quasistatic, meaning very slow so that the pressure defined is uniform. then $W = PA\Delta V$, but $\Delta x = -\Delta V$; minus since the volume decreases.
- $W = -PA\Delta V$ quasistatic.
- If P is not constant,

$$W = -\int_{V_i}^{V_f} P(V) \, dV \tag{1.3}$$

- isothermal compression is slow that the temperature doesn't raise.
- adiabatic compression is so fast that no heat escapes from the gas.
- Isothermal process
 - the change will be along an **isotherm** line, with P = NkT/V.
 - The work done is

$$W = -\int_{V_i}^{V_f} P(V) \, dV = NkT \ln \frac{V_i}{V_f}$$
 (1.4)

- The heat enters the system, from the first law, is

$$Q = \Delta U - W = \underbrace{\Delta(\frac{1}{2}NfkT)}_{0} - W = NkT \ln \frac{V_f}{V_i}$$
(1.5)

1.6. HEAT CAPACITIES 5

- adiabatic process
 - In the PV plot the change is from one isotherm to another.
 - There should be no trasfer of heat so

$$\Delta U = Q + W = W \tag{1.6}$$

- If it's *ideal* gas, U is proportional to T, so the temperature increases.
- By the equipartition theorem $U = \frac{f}{2}NkT$, so $dU = \frac{f}{2}Nk\,dT$, then from (1.3)

$$\frac{f}{2}Nk\,dT = -P\,dV\tag{1.7}$$

Using the ideal gas law for P and integrate

$$\frac{f}{2} \ln \frac{T_f}{T_i} = -\frac{V_f}{V_i}$$
 or $V_f T_f^{f/2} = V_i T_i^{f/2} = \text{const.}$ (1.8)

- Using the ideal gas law to eliminate $T, V^{\gamma}P = \text{const.}, \gamma$ is the adiabatic exponent.

1.6 Heat Capacities

• Heat capacity of an object is the amount of heat needed to raise its temperature, per degree change

$$C = \frac{Q}{\Delta T} \tag{1.9}$$

• The more matter you have the larger the heat capacity, by factoring out the mass m we get specific heat

$$c \equiv \frac{C}{m} \tag{1.10}$$

• Note (1.10) is ambiguous, plug in the first law

$$C = \frac{Q}{\Delta T} = \frac{\Delta U - W}{\Delta T} \tag{1.11}$$

Even if the energy of an object is a well-defined function of its temperature alone, the work W done on the object is not; it depends on the process path on PV plot.

• From (1.11) The heat capacity at constant volume, denoted C_V

$$C_V = \left(\frac{\Delta U}{\Delta T}\right)_V = \left(\frac{\partial U}{\partial T}\right)_V \tag{1.12}$$

• From (1.11) and (1.3) the heat capacity at constant pressure, denoted C_P

$$C_{P} = \left(\frac{\Delta U - (-P\Delta V)}{\Delta T}\right)_{P} = \left(\frac{\partial U}{\partial T}\right)_{P} + P\left(\frac{\partial V}{\partial T}\right)_{P}$$
(1.13)

for solid last term is almost negligible.

- At a phase transformation, you add heat in a system without increasing its temperature; such as melting of boiling water. Then $C=\frac{Q}{\Delta T}=\infty$
- ullet The amount of heat needed to do this phase transformation is called **latent heat** L, and the **specific latent heat** is

$$l \equiv \frac{L}{m} = \frac{Q}{m} \tag{1.14}$$

It's ambiguous, but we assume the pressure is constant, and no other work done.

 \bullet Adding PV onto the energy gives the **enthalpy**

$$H = U + PV \tag{1.15}$$

it's the total energy you would need to create the system out of nothing.

Chapter 2

The Second Law

2.1 Two-State system

- Irreversible processes are not *inevitable*, they are just overwhelmingly *probable*.
- A microstate is an outcome.
- A macrostate is saying number of particle for each state, e.g., two heads.
- multiplcity of a macrostate is the number of microstates for a given macrostate.
- Total multiplicity of all macrostates is the total number of microstates. Then the probability of a macrostate is

$$p = \frac{\Omega(n)}{\Omega(\text{all})} \tag{2.1}$$

• Number of different ways of choosing n items out of N, or the combination of n chosen from N.

$$\Omega(N,n) = \frac{N!}{n!(N-n)!} = \binom{N}{n}$$
(2.2)

2.2 The Einstein Model of a Solid

Consider a collection of microscopic system that can each store any number of energy 'units' Equal-size energy units as in quantum harmonic oscillator.

- In three-dimensional solid, each atom can oscillate in three independent directions, for N oscillators there are N/3 atoms.
- \bullet The multiplicity of an Einstein solid with N oscillators and q energy units is

$$\Omega(N,q) = \binom{q+N-1}{q} = \frac{(q+N-1)!}{q!(N-1)!}$$
(2.3)

2.3 Interacting Systems

To understand the heat flow and irreversible processes, consider two Einstein solids that can share energy back and forth

- Assume the two solids are **weakly coupled**; the exchange of energy between them is slower then the exchange of energy among atom within each solid.
- Then the inidivisual energies of solids, U_A and U_B , will change slowly; over short time they are fixed.
- on longer time scales the values of U_A and U_B will change, so we consider $U_{\text{total}} = U_A + U_A$
- The total multiplicity for independent system is just the product of Ω_A and $Omega_B$.
- Fundamental assumption statistical mechanics In an isolated system in thermal equilibrium, all accessible microstates are equally probable.
- Invoking this principle on the two Einstein solids, we conclude that, while all the *microstates* are equally probable, some *macrostates* are more probable than others.
- The *heat*, then, is a probabilistic phenomenon; if system started *initially* with all the energy in solid B and wait for a while, it's more certain to find that the energy has flowed from B to A.