

IDS - Assignment # 5

Gr II.

Name: Ammar Asif

Reg no: FA19-BCS-088

Question NO # 1.

Compute the bow, TF, IDF and TF, IDF.

S1 "Sunshine state enjoy sunshine"

S2 "Brown fox jump high, brown fox run"

S3 "Sunshine state for run fast"

For Bow document term matrix.

	sunshine	state	enjoy	brown	fox	jump	high	run	for
S1	2	1	1	0	0	0	0	0	0
S2	0	0	0	2	2	1	1	1	0
S3	1	1	0	0	1	0	0	0	1

Vector S1: [2, 1, 1, 0, 0, 0, 0, 0, 0]

Vector S2: [0, 0, 0, 2, 2, 1, 1, 0]

Vector S3: [1, 1, 0, 0, 1, 0, 0, 1, 1]

Now for term frequency.

Term frequency

	sunshine	state	enjoy	brown	fox	jump	high	run	fast
tf-s1	2/4	1/4	1/4	0	0	0	0	0	0
tf-s2	0	0	0	2/7	2/7	1/7	1/7	1/7	0
tf-s3	1/5	1/5	0	0	1/5	0	0	1/5	1/5

IDF Inverse document frequency

$$\text{idf}(\text{sunshine}) = \log(3/2) = 0.18$$

$$\text{idf}(\text{state}) = \log(3/2) = 0.18$$

$$\text{idf}(\text{enjoy}) = \log(3/1) = 0.48$$

$$\text{idf}(\text{brown}) = \log(3/1) = 0.48$$

$$\text{idf}(\text{fox}) = \log(3/2) = 0.18$$

$$\text{idf}(\text{jump}) = \log(3/1) = 0.48$$

$$\text{idf}(\text{high}) = \log(3/1) = 0.48$$

$$\text{idf}(\text{run}) = \log(3/2) = 0.18$$

$$\text{idf}(\text{fast}) = \log(3/1) = 0.48$$

TF-IDF

S1 → sunshine state enjoy sunshine.

$$\text{tf} \cdot \text{idf}(\text{sunshine}) = \frac{2}{4} \times 0.18 = 0.09$$

$$\text{tf} \cdot \text{idf}(\text{state}) = \frac{1}{4} \times 0.18 = 0.045$$

$$\text{tf} \cdot \text{idf}(\text{enjoy}) = \frac{1}{4} \times 0.48 = 0.12$$

S2 → "brown fox jump high, brown fox run"

$$tf \cdot idf(\text{brown}) = 2/7 \times 0.48 = 0.14$$

$$tf \cdot idf(\text{fox}) = 2/7 \times 0.18 = 0.05$$

$$tf \cdot idf(\text{jump}) = 1/7 \times 0.48 = 0.07$$

$$tf \cdot idf(\text{high}) = 1/7 \times 0.48 = 0.07$$

$$tf \cdot idf(\text{run}) = 1/7 \times 0.18 = 0.03$$

S3 → "sunshine state fox run fast"

$$tf \cdot idf(\text{sunshine}) = 1/5 \times 0.18 = 0.04$$

$$tf \cdot idf(\text{state}) = (1/5 \times 0.18) = 0.04$$

$$tf \cdot idf(\text{fox}) = 1/5 \times 0.18 = 0.04$$

$$tf \cdot idf(\text{run}) = 1/5 \times 0.18 = 0.04$$

$$tf \cdot idf(\text{fast}) = 1/5 \times 0.48 = 0.096$$

Question NO # 2

Cosine - Similarity

S₁ and S₃

TF - IDF vectors :-

$$S_1 = [0.09, 0.045, 0.12, 0, 0, 0, 0, 0, 0]$$

$$S_3 = [0.04, 0.04, 0, 0, 0.04, 0, 0, 0, 0.04, 0.096]$$

$$\cos(S_1, S_3) = \frac{S_1 \cdot S_3}{|S_1| |S_3|}$$

$$\begin{aligned} S_1 \cdot S_3 &= (0.09 \times 0.04) + (0.045 \times 0.04) \\ &\quad + 0 + 0 + 0 + 0 \\ &\quad + 0 + 0 + 0 = 0.0054 \end{aligned}$$

$$\begin{aligned} |S_1| &= \sqrt{(0.09 \times 0.09) + (0.045 \times 0.045) + 0 + 0 + (0.12 \times 0.12)} \\ &= 0.15660 \end{aligned}$$

$$\begin{aligned} |S_3| &= \sqrt{(0.04 \times 0.04) + (0.04 \times 0.04) + (0.04 \times 0.04) + (0.04 \times 0.04) + (0.096 \times 0.096)} \end{aligned}$$

$$\begin{aligned} &= \sqrt{0.0016 + 0.0016 + 0.0016 + 0.0016 + 0.0092} \end{aligned}$$

$$|S_3| = 0.125$$

$$\cos(s_1, s_3) = \frac{0.0054}{0.15660 \times 0.125}$$
$$= 0.275$$