

Spring 2023

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1. Searching B+ Trees

1.1.

SELECT * FROM table WHERE ID = 12

Solution : B0, B1, B3

1.2.

SELECT * FROM table WHERE ID <= 41

Solution : B0, B1, B3, B4, B5

1.3.

SELECT * FROM table WHERE ID > 68

Solution : B0, B2, B6, B7, B8

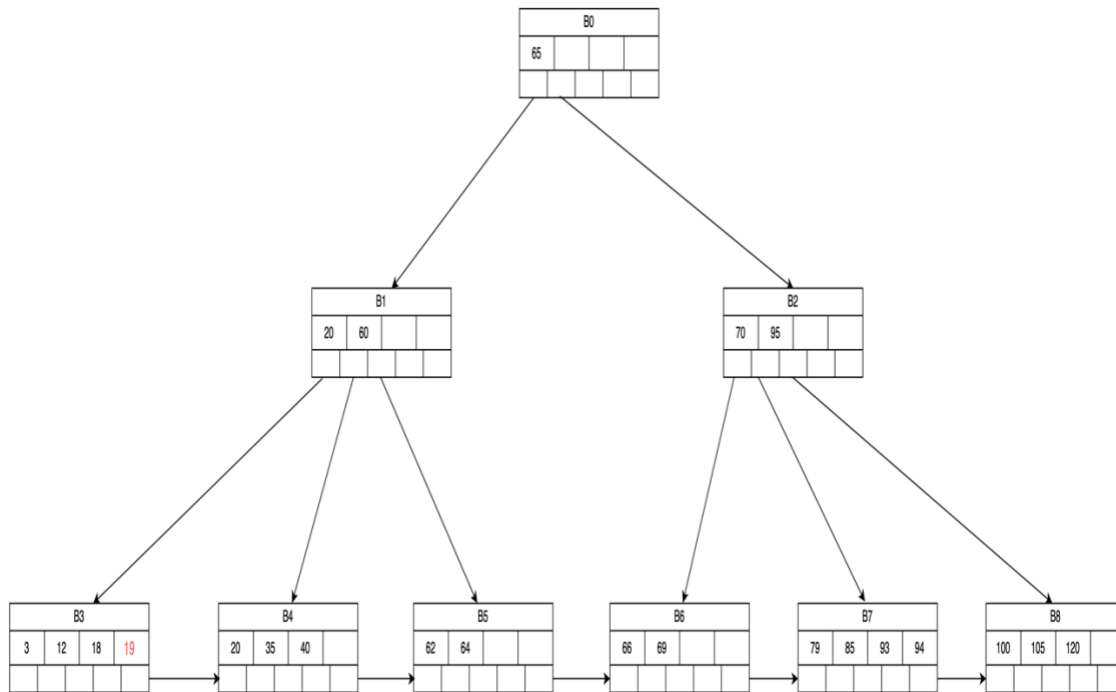
1.4.

SELECT * FROM table WHERE ID > 80 AND ID < 120

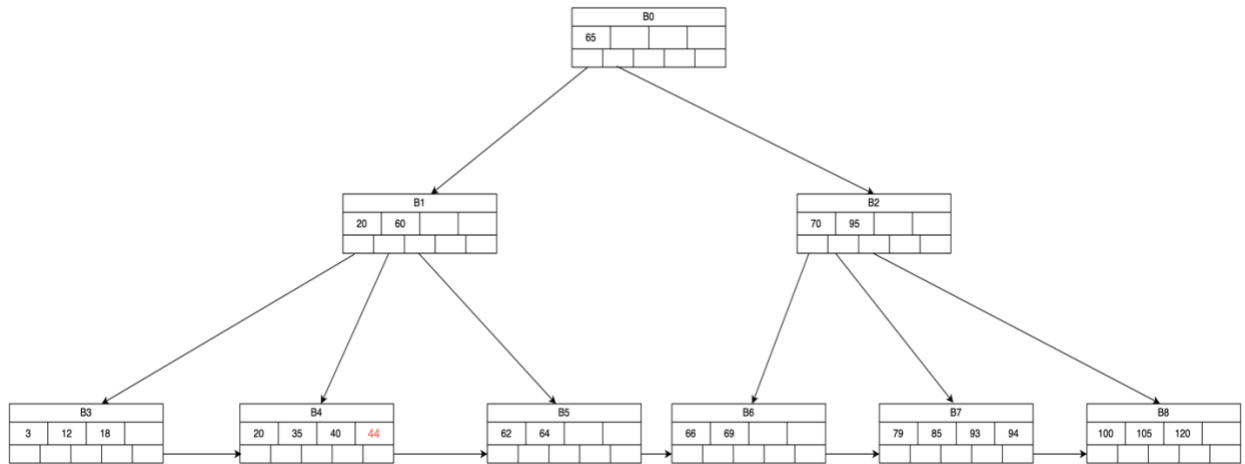
Solution: B0, B2, B7, B8

2. Insertion in a B+ Tree

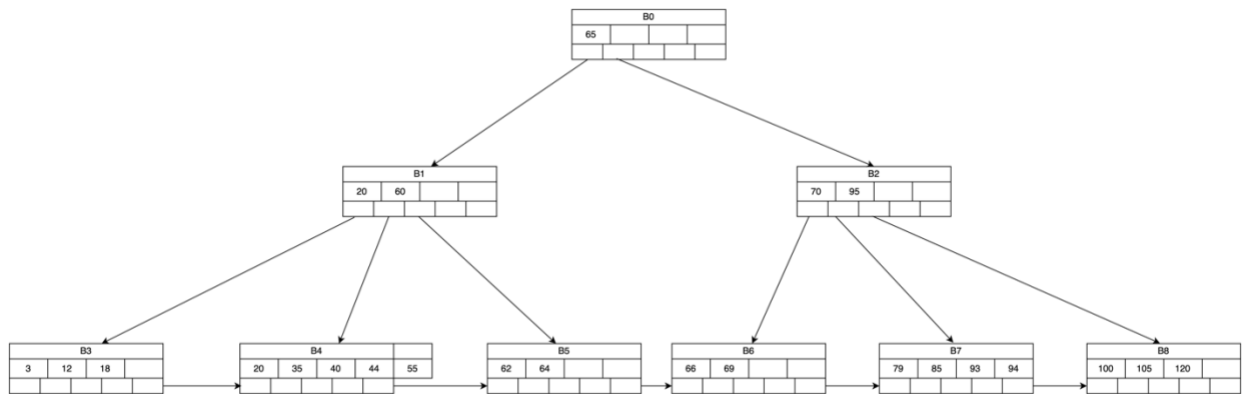
2.1. Insert 19 in B0->B1->B3



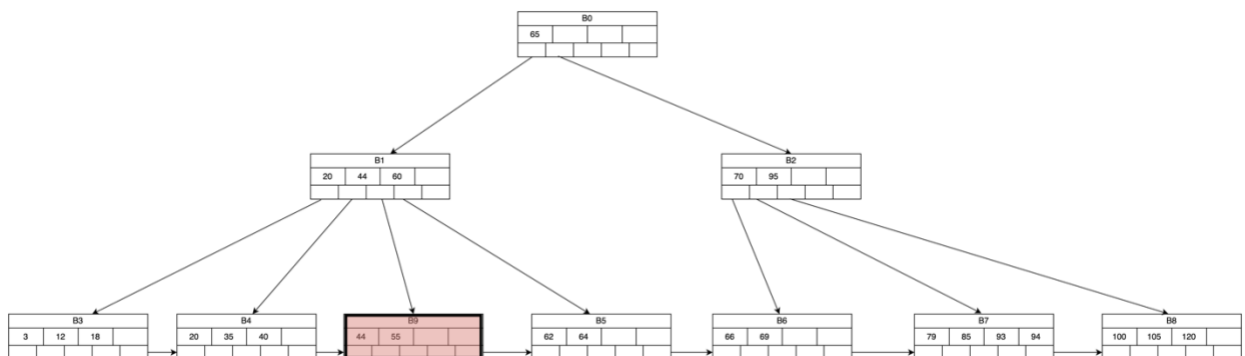
2.2. After inserting 44 -> Insert 44 at B3



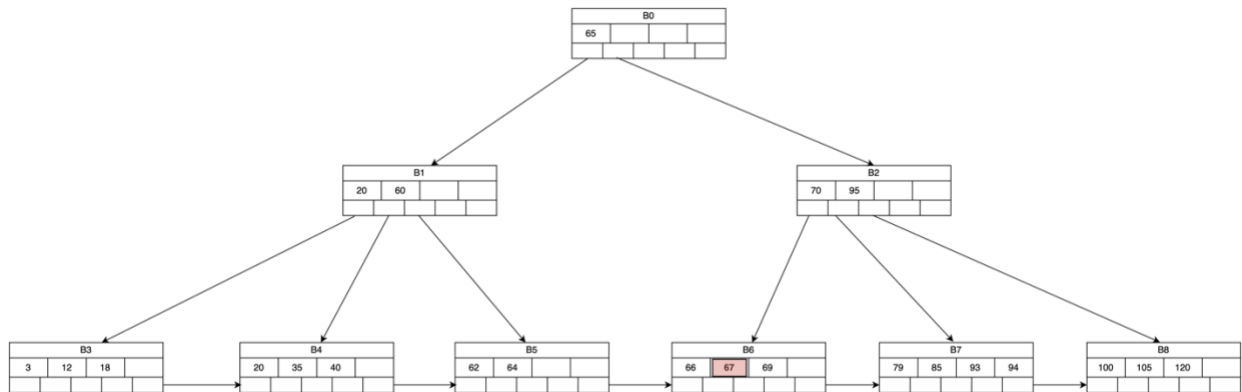
After inserting 55



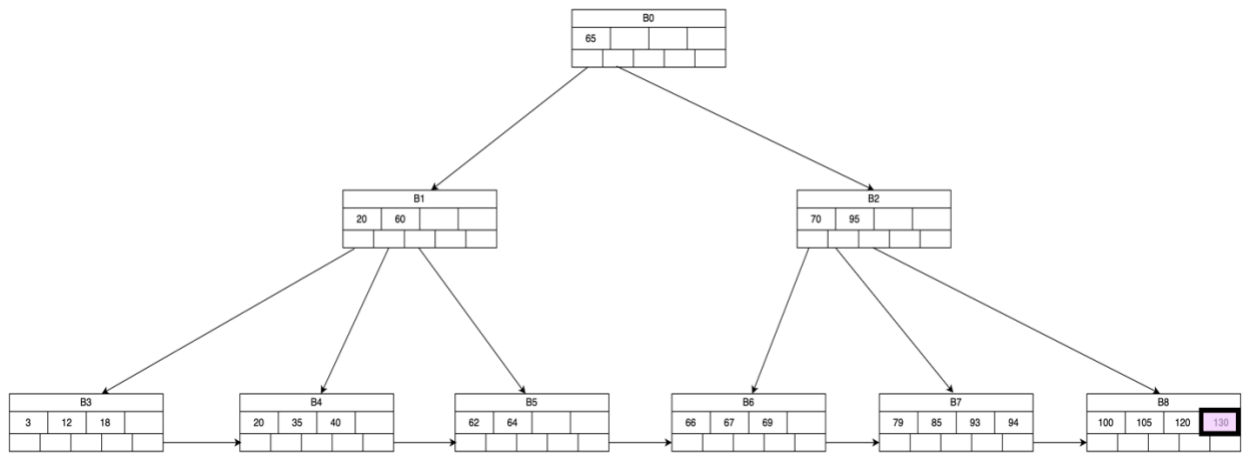
Splitting



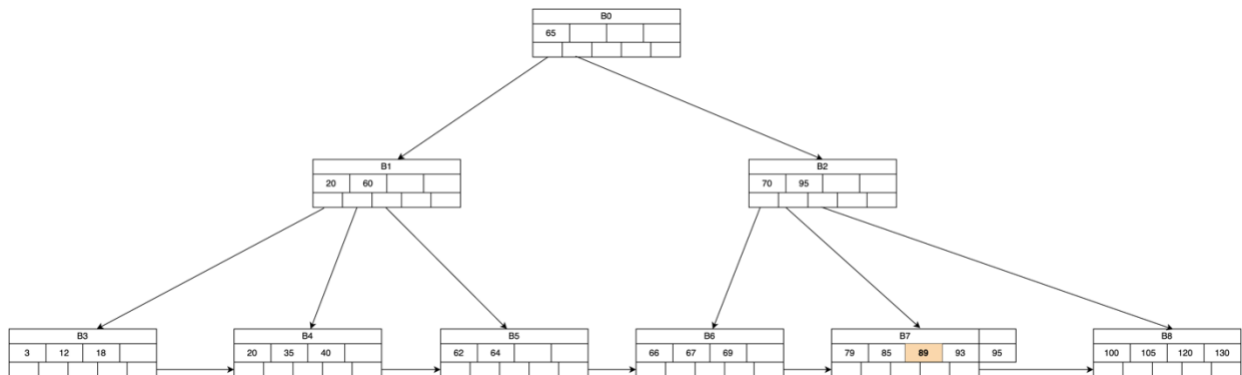
2.3. After inserting 67



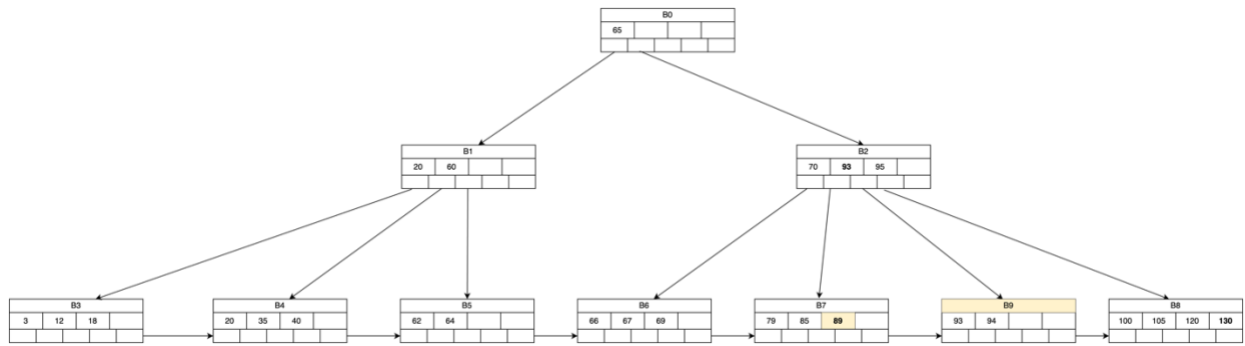
After inserting 130



After inserting 89

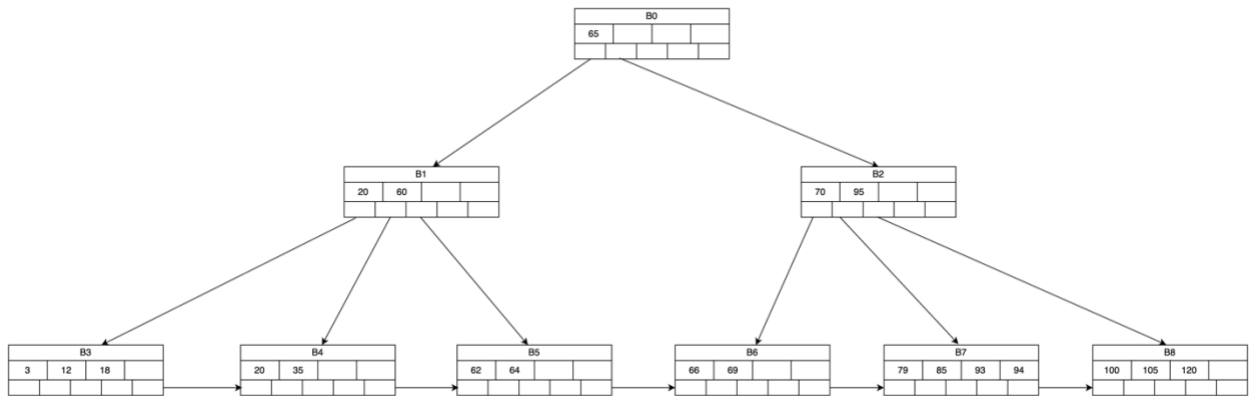


Now we have to split the block B7

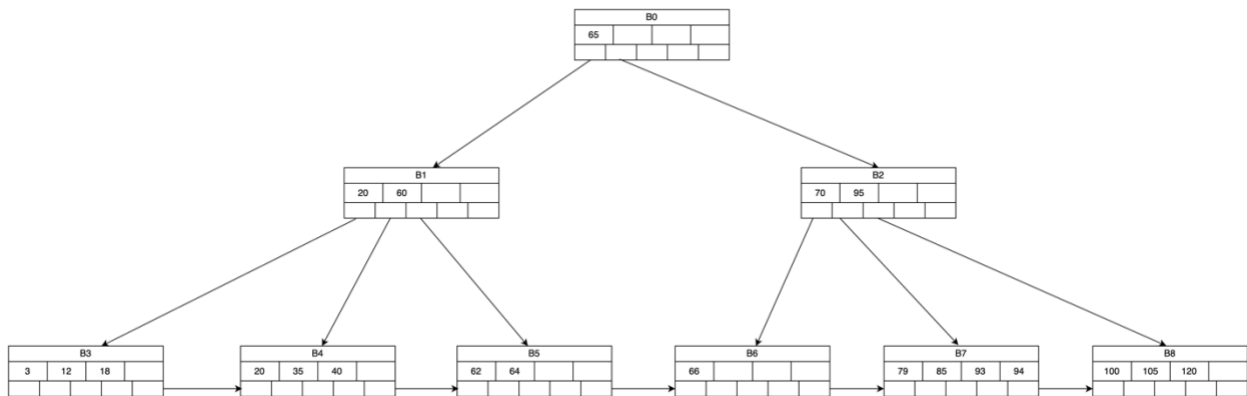


3. Deletion from a B+ Tree

3.1. Deletion of 40 – traverse B0->B1->B4

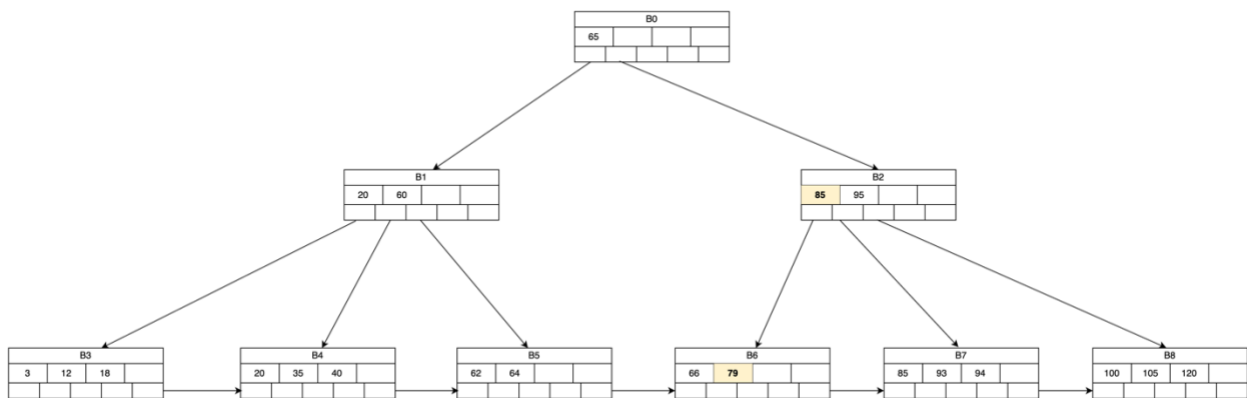


3.2. Remove 69- Traverse B0->B1->B6



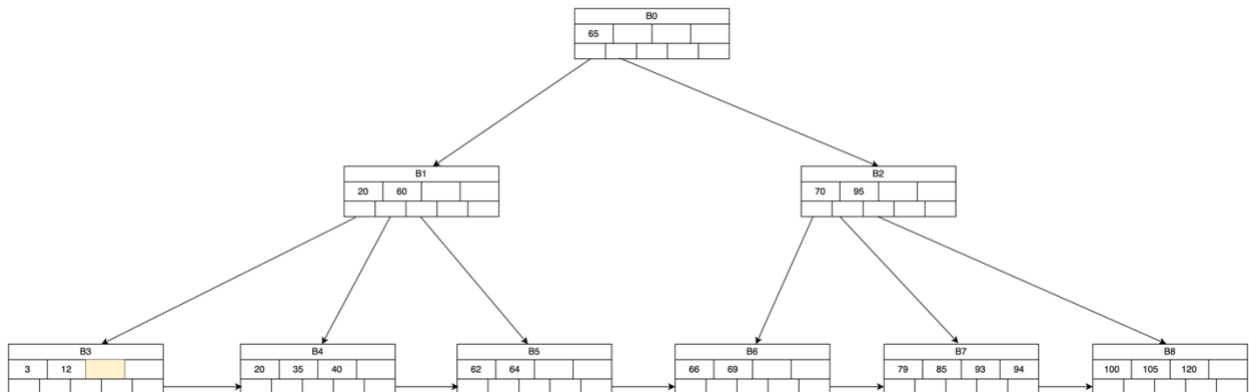
Since B6 has only one value , it will borrow from right sibling

After Rotation

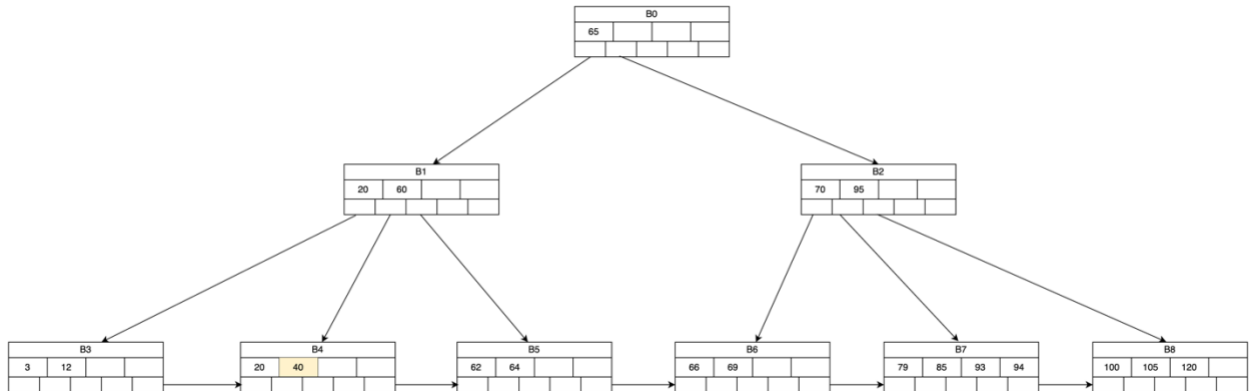


3.3.

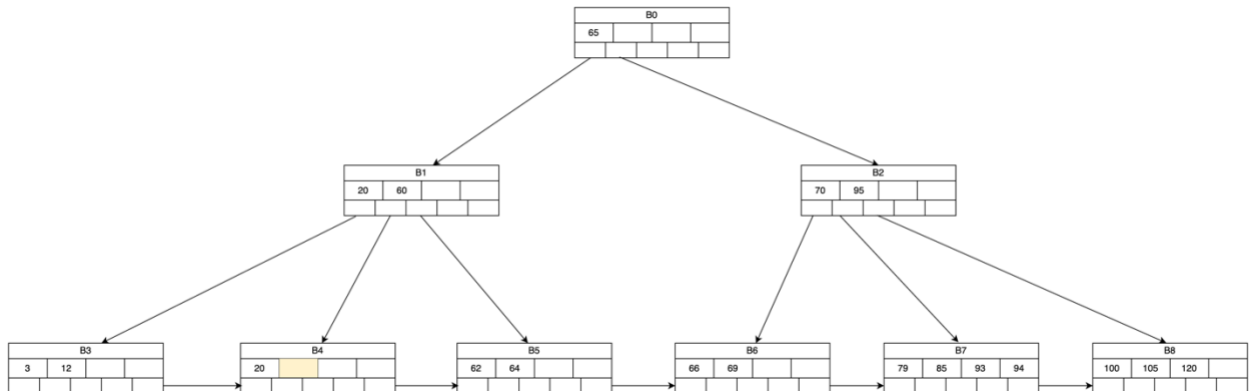
Remove 18 from B3



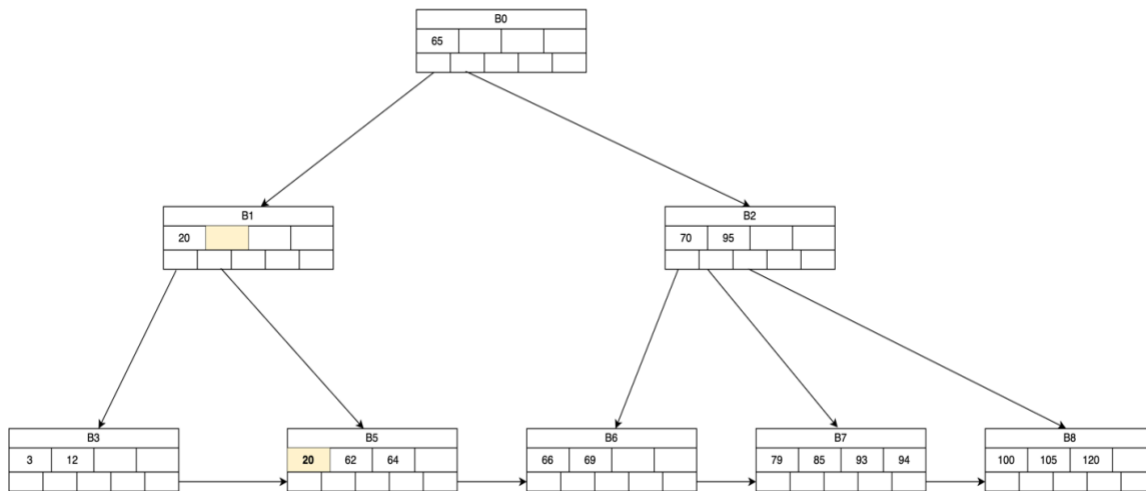
Delete 35 from B4



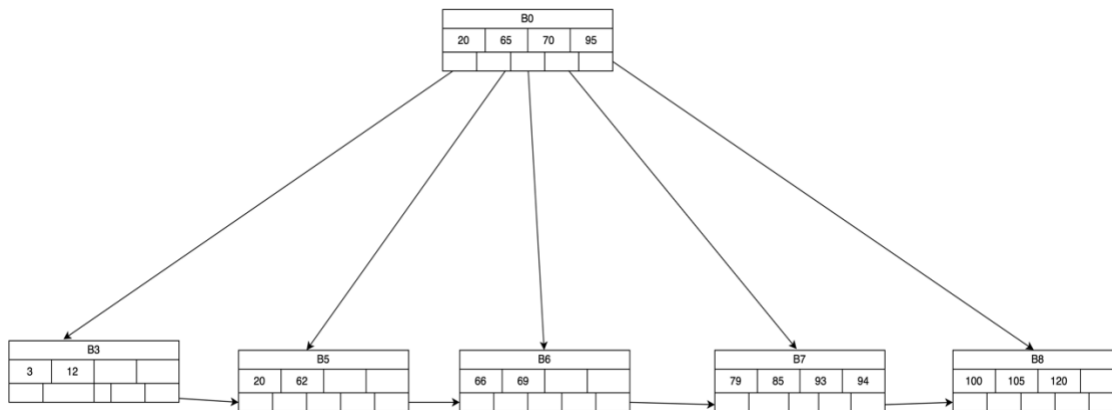
Delete 40 – B4 becomes unbalanced



**Rotation not possible. So Nodes B4 and B5 are merged.
Parent Node is updated**

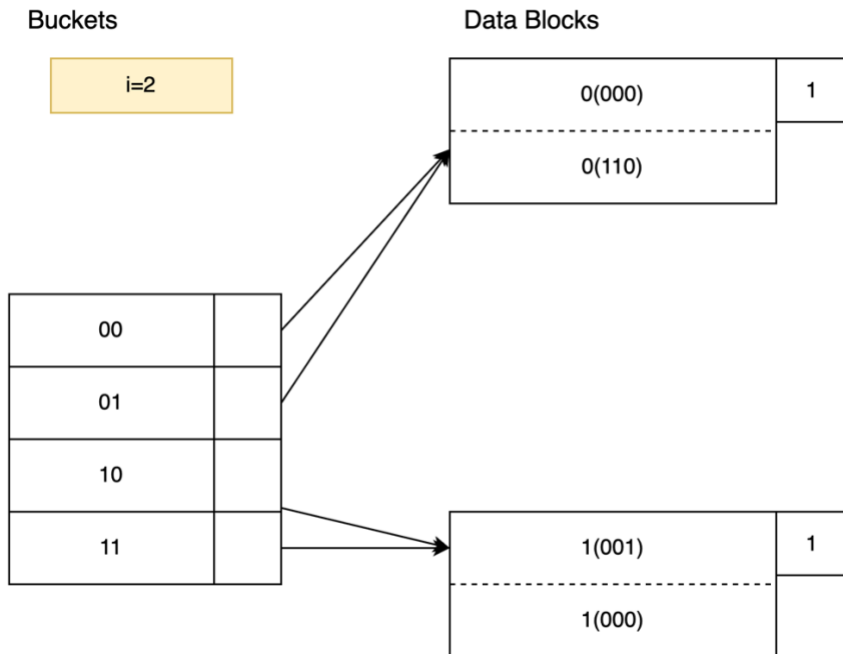


Now B1 is unbalanced. Hence merge B1, B0, B2

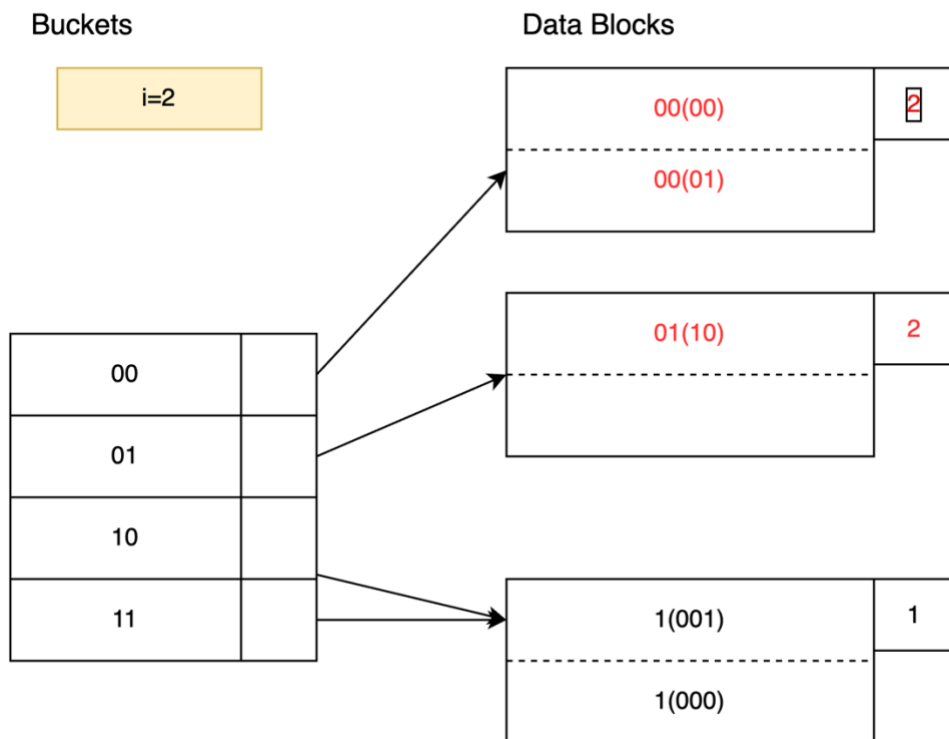


4. Extensible Hash Table

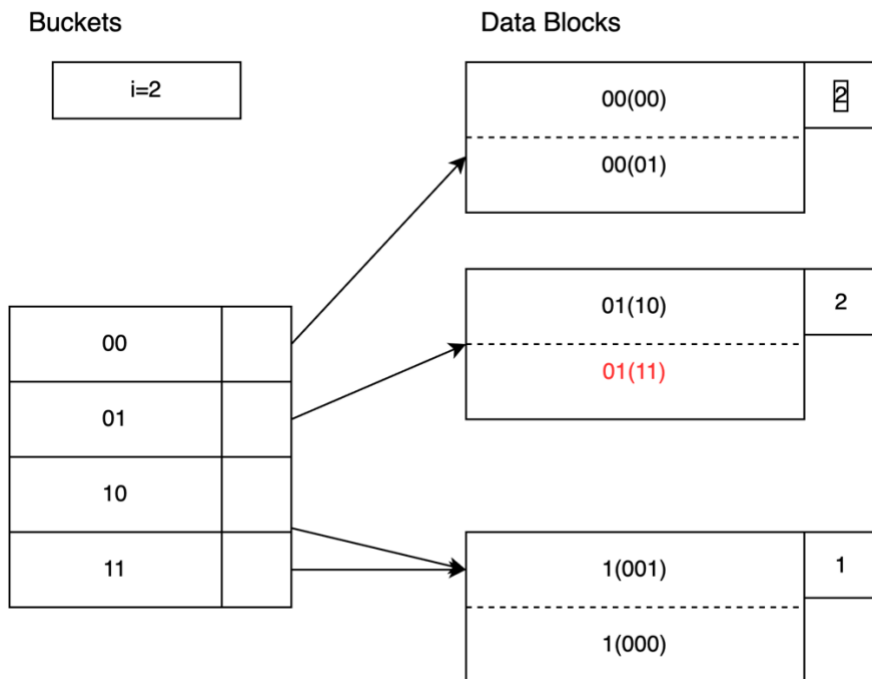
4.1. Insert 0001 – Step 1: increase buckets i=2



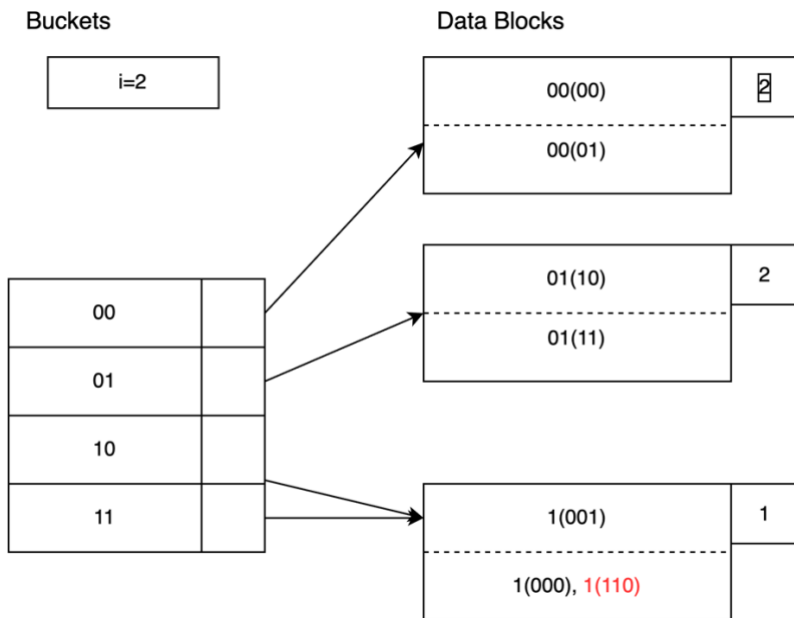
Step 2: Insert 0001



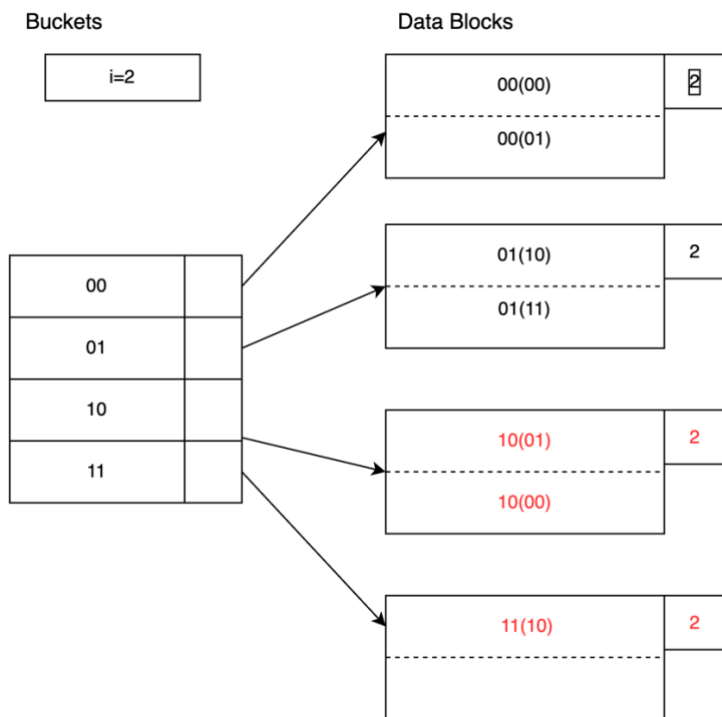
4.2. Insert 0111



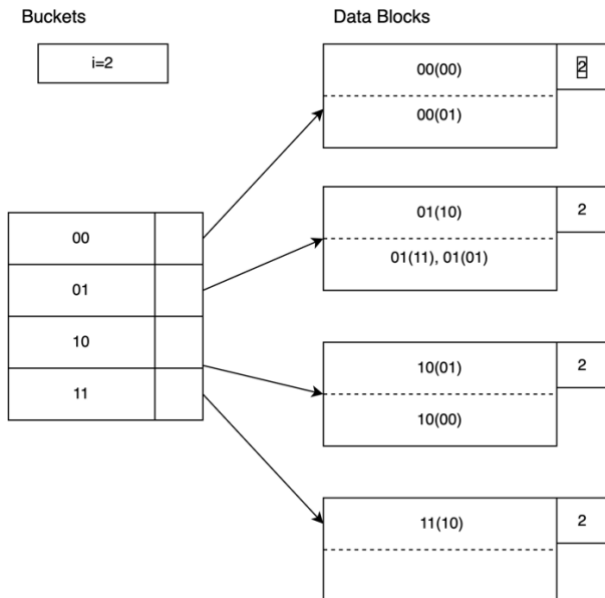
4.3. Insert 1110



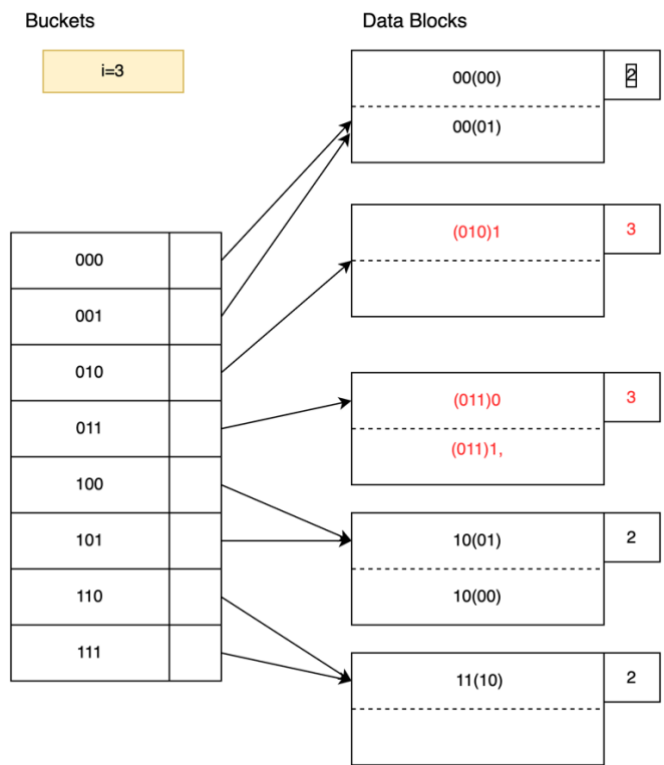
Need to add a new block



4.4. Insert 0101



Need to extend the buckets as block is full, make i=3

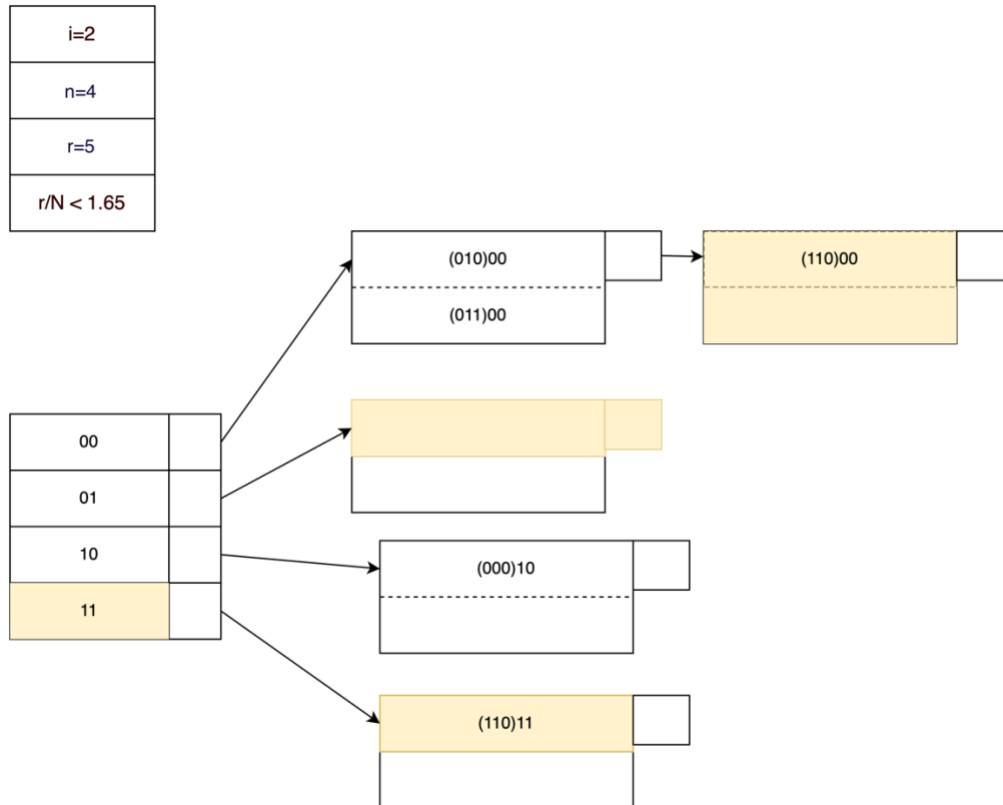


5. Linear HashTable

- **Insert 11000**

$r = 5$ $n=3$; $r/n = 5/3 = 1.67 > 1.65$

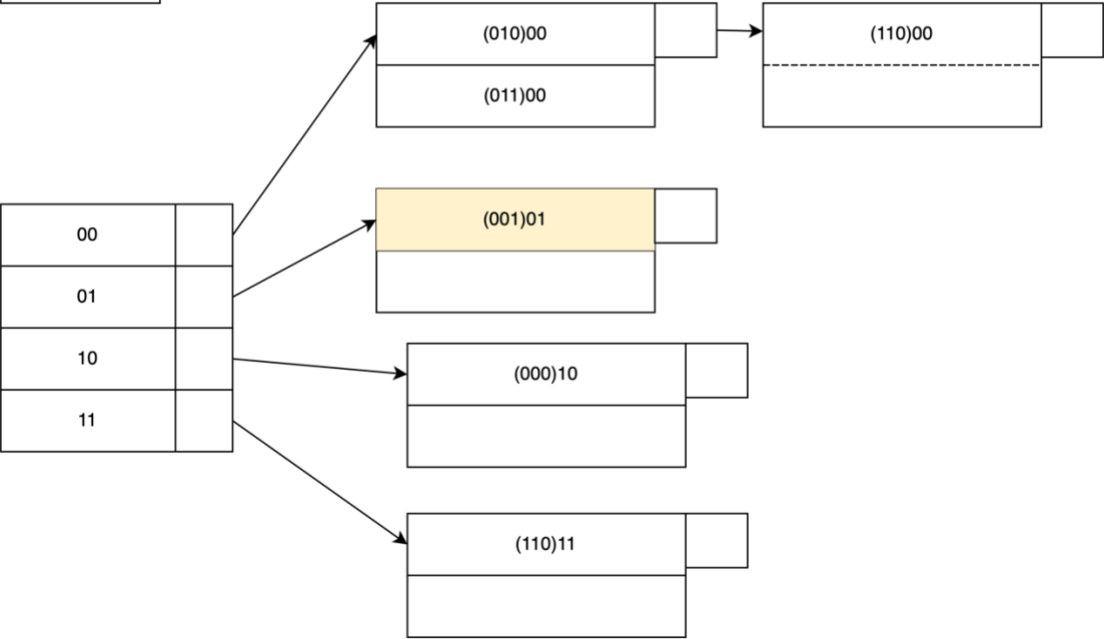
Hence introduce a new bucket 11 . Rearrange the entries from MSB flipped bucket (01) and add the new entry 11000 in 00 bucket as overflow block .



- **Insert 00101**

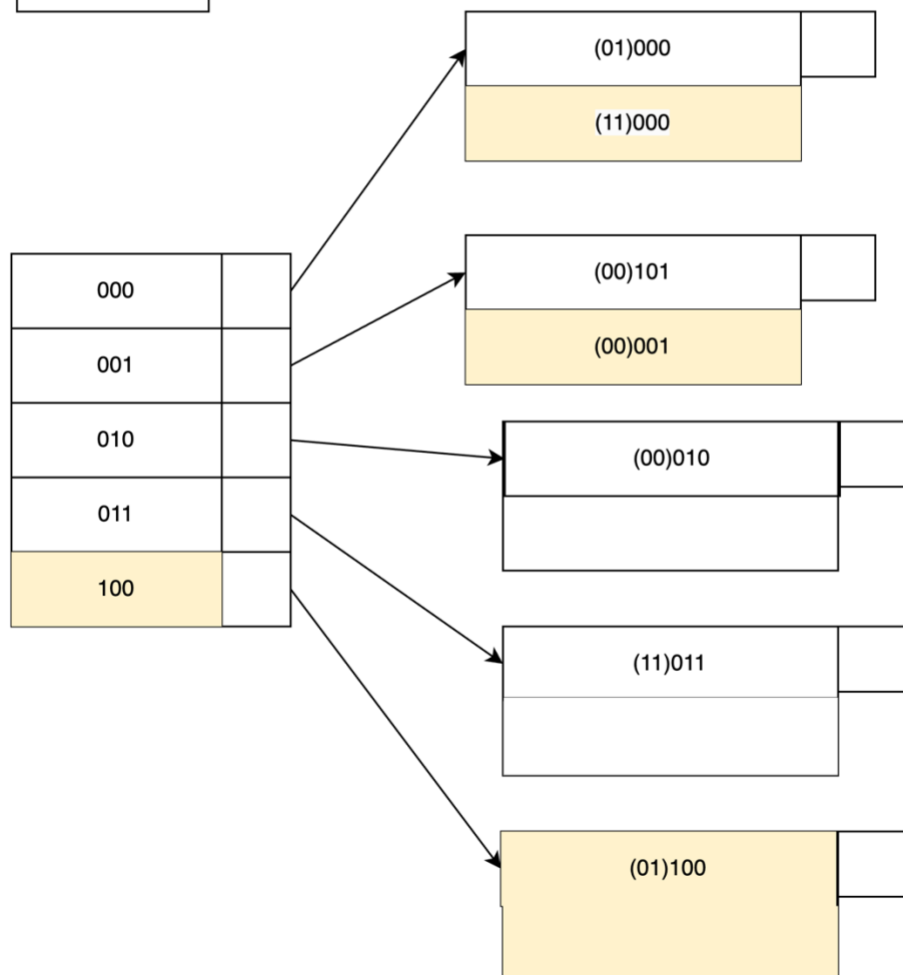
$r=6$ $n=4$; $r/n = 6/4 = 1.5 < 1.65$. Hence directly insert in 01 bucket

i=2
n=4
r=6
$r/N < 1.65$



- Insert 00001
 $r=7$; $n=4$; $r/n = 7/4 = 1.75 > 1.65$
 hence need to extend bucket array to add a new bucket 100. Rearrange entries from 000 - move 00100 from 000 to 100 bucket.
 Now insert 00001 to bucket 001

$i=3$
$n=5$
$r=7$
$r/N < 1.65$



- Insert 01111
 $r=8$ $n=5$; $r/n = 8/5 = 1.6 < 1.65$
 As bucket 111 isn't present, flip MSB to get 011 and now insert it in bucket 011

