

Class 08: Breast Cancer Analysis Mini Project

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Background

The goal of this mini-project is for you to explore a complete analysis using the unsupervised learning techniques covered in class. You'll extend what you've learned by combining PCA as a preprocessing step to clustering using data that consist of measurements of cell nuclei of human breast masses. This expands on our RNA-Seq analysis from last day.

The data itself comes from the Wisconsin Breast Cancer Diagnostic Data Set first reported by K. P. Benne and O. L. Mangasarian: "Robust Linear Programming Discrimination of Two Linearly Inseparable Sets".

Values in this data set describe characteristics of the cell nuclei present in digitized images of a fine needle aspiration (FNA) of a breast mass.

Data Import

Input data file is saved into my Project directory as a CSV

```
wisc.df <- read.csv("WisconsinCancer.csv", row.names = 1)
head(wisc.df)
```

	diagnosis	radius_mean	texture_mean	perimeter_mean	area_mean
842302	M	17.99	10.38	122.80	1001.0
842517	M	20.57	17.77	132.90	1326.0
84300903	M	19.69	21.25	130.00	1203.0
84348301	M	11.42	20.38	77.58	386.1
84358402	M	20.29	14.34	135.10	1297.0
843786	M	12.45	15.70	82.57	477.1
	smoothness_mean	compactness_mean	concavity_mean	concave.points_mean	
842302	0.11840	0.27760	0.3001		0.14710
842517	0.08474	0.07864	0.0869		0.07017
84300903	0.10960	0.15990	0.1974		0.12790
84348301	0.14250	0.28390	0.2414		0.10520
84358402	0.10030	0.13280	0.1980		0.10430
843786	0.12780	0.17000	0.1578		0.08089
	symmetry_mean	fractal_dimension_mean	radius_se	texture_se	perimeter_se
842302	0.2419		0.07871	1.0950	0.9053
842517	0.1812		0.05667	0.5435	0.7339
84300903	0.2069		0.05999	0.7456	0.7869
84348301	0.2597		0.09744	0.4956	1.1560
84358402	0.1809		0.05883	0.7572	0.7813
843786	0.2087		0.07613	0.3345	0.8902
	area_se	smoothness_se	compactness_se	concavity_se	concave.points_se
842302	153.40	0.006399	0.04904	0.05373	0.01587
842517	74.08	0.005225	0.01308	0.01860	0.01340
84300903	94.03	0.006150	0.04006	0.03832	0.02058
84348301	27.23	0.009110	0.07458	0.05661	0.01867
84358402	94.44	0.011490	0.02461	0.05688	0.01885
843786	27.19	0.007510	0.03345	0.03672	0.01137
	symmetry_se	fractal_dimension_se	radius_worst	texture_worst	
842302	0.03003		0.006193	25.38	17.33
842517	0.01389		0.003532	24.99	23.41
84300903	0.02250		0.004571	23.57	25.53
84348301	0.05963		0.009208	14.91	26.50
84358402	0.01756		0.005115	22.54	16.67
843786	0.02165		0.005082	15.47	23.75
	perimeter_worst	area_worst	smoothness_worst	compactness_worst	
842302	184.60	2019.0	0.1622		0.6656
842517	158.80	1956.0	0.1238		0.1866
84300903	152.50	1709.0	0.1444		0.4245

84348301	98.87	567.7	0.2098	0.8663
84358402	152.20	1575.0	0.1374	0.2050
843786	103.40	741.6	0.1791	0.5249
	concavity_worst	concave.points_worst	symmetry_worst	
842302	0.7119	0.2654	0.4601	
842517	0.2416	0.1860	0.2750	
84300903	0.4504	0.2430	0.3613	
84348301	0.6869	0.2575	0.6638	
84358402	0.4000	0.1625	0.2364	
843786	0.5355	0.1741	0.3985	
	fractal_dimension_worst			
842302	0.11890			
842517	0.08902			
84300903	0.08758			
84348301	0.17300			
84358402	0.07678			
843786	0.12440			

The first column **diagnosis** is the expert opinion on the sample (i.e. patient FNA)

```
wisc.df$diagnosis
```

```
[1] "M" "M"
[19] "M" "B" "B" "B" "M" "M"
[37] "M" "B" "M" "M" "M" "M" "M" "M" "M" "M" "B" "M" "B" "B" "B" "B" "B" "M"
[55] "M" "B" "M" "M" "B" "B" "B" "M" "B" "M" "B" "M" "B" "B" "B" "B" "B" "M" "B"
[73] "M" "M" "B" "M" "B" "M" "B" "B" "B" "M" "B" "M" "B" "M" "B" "M" "B" "B" "B"
[91] "B" "M" "B" "B" "M" "M" "B" "B" "B" "M" "M" "B" "B" "B" "B" "M" "B" "B" "B"
[109] "M" "B" "B" "B" "B" "B" "B" "B" "B" "M" "M" "B" "M" "M" "B" "M" "B" "B" "B" "B"
[127] "M" "M" "B" "B" "M" "B"
[145] "B" "B" "M" "B" "M" "B" "B" "B" "B" "M"
[163] "M" "B" "M" "B" "M" "M" "B" "B" "B" "M" "M" "B" "B" "B" "B" "B" "B" "M" "B" "B"
[181] "M" "M" "M" "B" "M" "B" "M" "B" "B" "B" "M" "B" "B" "M" "M" "B" "M" "B" "M" "M"
[199] "M" "M" "B" "M" "M" "M" "B" "M" "B" "M" "B" "B" "M" "B" "M" "B" "M" "M" "M" "M"
[217] "B" "B" "M" "M" "B" "B" "B" "M" "B" "B" "B" "B" "B" "B" "M" "B" "B" "B" "B" "M" "B"
[235] "B" "B" "M" "M" "B" "M" "B" "M" "B"
[253] "M" "B" "B" "B" "B"
[271] "B" "B" "M" "B" "M" "B" "B" "M" "B" "B" "B" "M" "B" "M" "B" "M" "B" "B" "B" "B" "B"
[289] "B" "M" "B" "B" "M" "B" "B" "M" "B" "B" "B" "B"
[307] "B" "M" "B" "B" "B" "M" "B" "M"
[325] "B" "B" "B" "B" "M" "M" "B" "B" "B" "B" "B" "B" "B" "M" "B" "M" "B" "B" "M" "B" "B" "B"
[343] "B" "M" "B" "M" "M" "B" "B" "B" "B" "B" "B" "B"
```

```
[361] "B" "B" "B" "B" "B" "M" "M" "B" "M" "M" "M" "B" "M" "M" "B" "B" "B" "B"
[379] "B" "M" "B" "B" "B" "B" "B" "M" "B" "B" "B" "B" "M" "B" "B" "M" "B" "B"
[397] "B" "B" "B" "B" "M" "B" "B" "B" "B" "B" "B" "B" "M" "B" "B" "B" "B" "B"
[415] "M" "B" "B" "M" "B" "M" "B"
[433] "M" "M" "B" "M" "B" "B" "B" "B" "B" "M" "B" "B" "M" "B" "M" "B" "B" "M"
[451] "B" "M" "B" "B" "B" "B" "B" "B" "B" "B" "M" "M" "B" "B" "B" "B" "B" "B"
[469] "M" "B" "B" "B" "B" "B" "B" "B" "B" "B" "M" "B" "B" "B" "B" "B" "B" "B"
[487] "B" "M" "B" "M" "B" "B" "M" "B" "B" "B" "B" "B" "M" "M" "B" "M" "B" "M"
[505] "B" "B" "B" "B" "B" "M" "B" "B" "M" "B" "M" "B" "M" "B" "M" "B" "B" "B" "M"
[523] "B" "M" "B" "M" "B" "B" "B" "B"
[541] "B" "B"
[559] "B" "B" "B" "B" "M" "M" "M" "M" "M" "M" "M" "B"
```

-1 is used to remove the diagnosis column, which is not needed right now, but needed later as a vector

```
wisc.data <- wisc.df[,-1]
diagnosis <- wisc.df[,1]
```

Lastly, explore and get familiar

Q1. Q1. How many observations are in this dataset?

There are 569 observations/patients in the dataset.

Q2. How many of the observations have a malignant diagnosis?

There are 212 observations that have a malignant diagnosis.

```
table(wisc.df$diagnosis)
```

```
   B    M
357 212
```

Q3. How many variables/features in the data are suffixed with _mean?

```
colnames(wisc.data)
```

```

[1] "radius_mean"                  "texture_mean"
[3] "perimeter_mean"               "area_mean"
[5] "smoothness_mean"              "compactness_mean"
[7] "concavity_mean"                "concave.points_mean"
[9] "symmetry_mean"                 "fractal_dimension_mean"
[11] "radius_se"                     "texture_se"
[13] "perimeter_se"                  "area_se"
[15] "smoothness_se"                  "compactness_se"
[17] "concavity_se"                   "concave.points_se"
[19] "symmetry_se"                    "fractal_dimension_se"
[21] "radius_worst"                   "texture_worst"
[23] "perimeter_worst"                 "area_worst"
[25] "smoothness_worst"                "compactness_worst"
[27] "concavity_worst"                  "concave.points_worst"
[29] "symmetry_worst"                  "fractal_dimension_worst"

```

```
length(grep("_mean", colnames(wisc.data)))
```

```
[1] 10
```

Principal Coordinate Analysis

The `prcomp()` function to do PCA has a `scale=FALSE` default. In general we nearly always want to set this to TRUE so our analysis is not dominated by columns/variables in our data set that have high standard deviation and mean when compared to others just because the units of measurement are on different scales

```
wisc.pr <- prcomp( wisc.data, scale=TRUE)
summary(wisc.pr)
```

Importance of components:

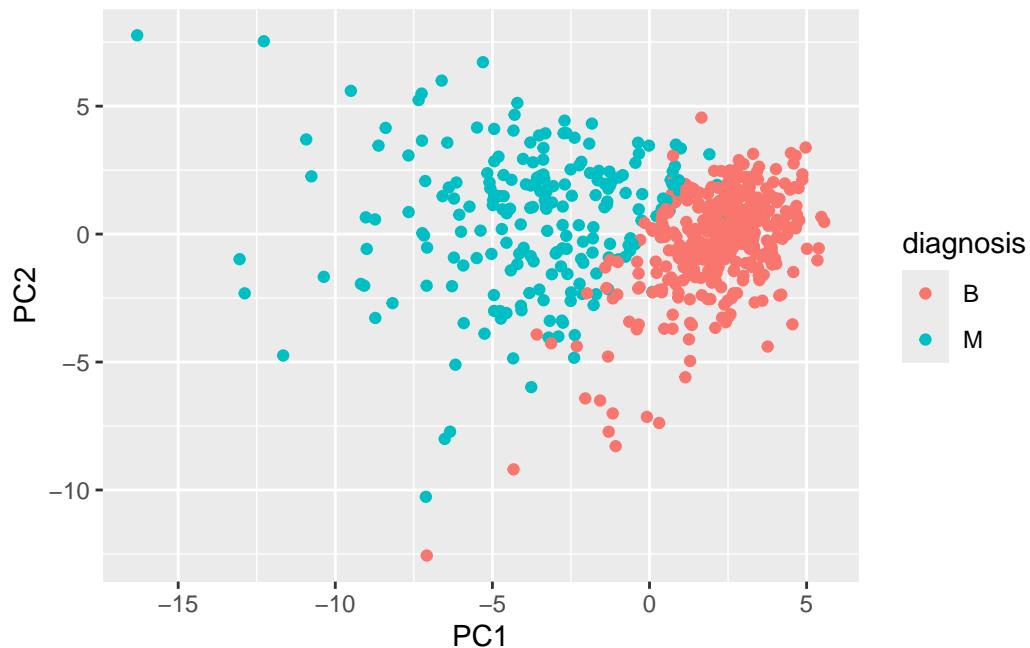
	PC1	PC2	PC3	PC4	PC5	PC6	PC7
Standard deviation	3.6444	2.3857	1.67867	1.40735	1.28403	1.09880	0.82172
Proportion of Variance	0.4427	0.1897	0.09393	0.06602	0.05496	0.04025	0.02251
Cumulative Proportion	0.4427	0.6324	0.72636	0.79239	0.84734	0.88759	0.91010
	PC8	PC9	PC10	PC11	PC12	PC13	PC14
Standard deviation	0.69037	0.6457	0.59219	0.5421	0.51104	0.49128	0.39624
Proportion of Variance	0.01589	0.0139	0.01169	0.0098	0.00871	0.00805	0.00523
Cumulative Proportion	0.92598	0.9399	0.95157	0.9614	0.97007	0.97812	0.98335
	PC15	PC16	PC17	PC18	PC19	PC20	PC21

	PC22	PC23	PC24	PC25	PC26	PC27	PC28
Standard deviation	0.30681	0.28260	0.24372	0.22939	0.22244	0.17652	0.1731
Proportion of Variance	0.00314	0.00266	0.00198	0.00175	0.00165	0.00104	0.0010
Cumulative Proportion	0.98649	0.98915	0.99113	0.99288	0.99453	0.99557	0.9966
	PC29	PC30					
Standard deviation	0.16565	0.15602	0.1344	0.12442	0.09043	0.08307	0.03987
Proportion of Variance	0.00091	0.00081	0.0006	0.00052	0.00027	0.00023	0.00005
Cumulative Proportion	0.99749	0.99830	0.9989	0.99942	0.99969	0.99992	0.99997
	PC29	PC30					
Standard deviation	0.02736	0.01153					
Proportion of Variance	0.00002	0.00000					
Cumulative Proportion	1.00000	1.00000					

The main PC result figure is called a “score plot” or a “PC plot” or “ordination plot”...

```
library(ggplot2)

ggplot(wisc.pr$x)+
  aes(PC1, PC2, col=diagnosis) +
  geom_point()
```



Q4. From your results, what proportion of the original variance is captured by the first principal components (PC1)?

44.27% of the original variance is captured by PC1

```
summary(wisc.pr)
```

Importance of components:

	PC1	PC2	PC3	PC4	PC5	PC6	PC7
Standard deviation	3.6444	2.3857	1.67867	1.40735	1.28403	1.09880	0.82172
Proportion of Variance	0.4427	0.1897	0.09393	0.06602	0.05496	0.04025	0.02251
Cumulative Proportion	0.4427	0.6324	0.72636	0.79239	0.84734	0.88759	0.91010
	PC8	PC9	PC10	PC11	PC12	PC13	PC14
Standard deviation	0.69037	0.6457	0.59219	0.5421	0.51104	0.49128	0.39624
Proportion of Variance	0.01589	0.0139	0.01169	0.0098	0.00871	0.00805	0.00523
Cumulative Proportion	0.92598	0.9399	0.95157	0.9614	0.97007	0.97812	0.98335
	PC15	PC16	PC17	PC18	PC19	PC20	PC21
Standard deviation	0.30681	0.28260	0.24372	0.22939	0.22244	0.17652	0.1731
Proportion of Variance	0.00314	0.00266	0.00198	0.00175	0.00165	0.00104	0.0010
Cumulative Proportion	0.98649	0.98915	0.99113	0.99288	0.99453	0.99557	0.9966
	PC22	PC23	PC24	PC25	PC26	PC27	PC28
Standard deviation	0.16565	0.15602	0.1344	0.12442	0.09043	0.08307	0.03987
Proportion of Variance	0.00091	0.00081	0.0006	0.00052	0.00027	0.00023	0.00005
Cumulative Proportion	0.99749	0.99830	0.9989	0.99942	0.99969	0.99992	0.99997
	PC29	PC30					
Standard deviation	0.02736	0.01153					
Proportion of Variance	0.00002	0.00000					
Cumulative Proportion	1.00000	1.00000					

Q5. How many principal components (PCs) are required to describe at least 70% of the original variance in the data?

3 principal components are required to describe at least 70% of the data

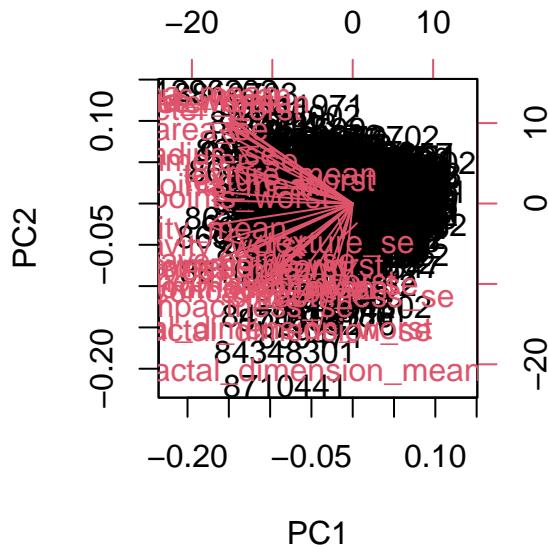
Q6. How many principal components (PCs) are required to describe at least 90% of the original variance in the data?

About 8 principal components are required to describe at least 90% of the original variance in the data

Interpreting PCA Results

Create a biplot of the `wisc.pr` using the `biplot()` function

```
biplot(wisc.pr)
```



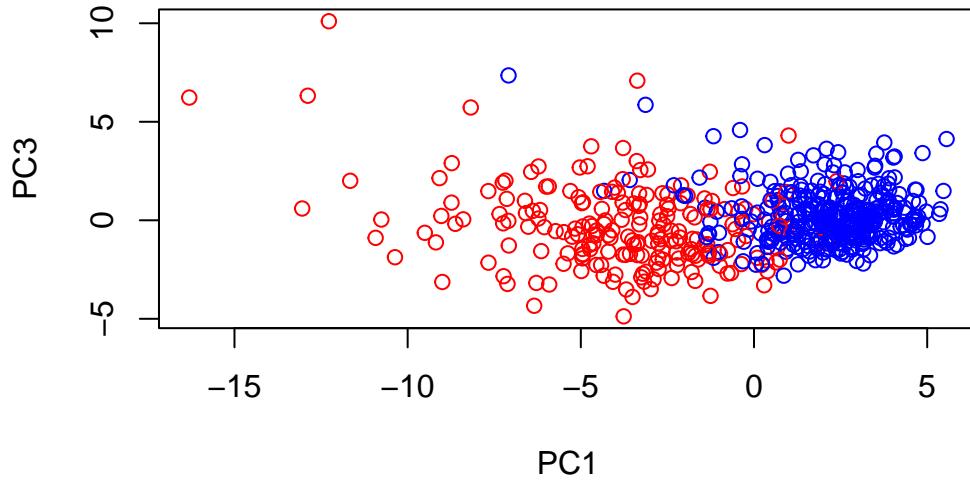
Q7. What stand out to you about this plot? Is it easy or difficult to understand and why?

There are too many plots on this plot, there is no scaling of values to remove this noise.

Q8. Generate a similar plot for principal components 1 and 3. What do you notice about these plots?

These plots show a distinct difference in clustering between the two colors.

```
col <- ifelse(diagnosis == "M", "red", "blue")
plot(wisc.pr$x[,c(1,3)], col = col ,
      xlab = "PC1", ylab = "PC3")
```



PCA Scree-plot

A plot of how much variance each PC captures. We can get this from `wisc.pr$sdev` or from the output of `summary(wisc.pr)`

```
var.tbl <- summary(wisc.pr)
head(var.tbl$importance)
```

	PC1	PC2	PC3	PC4	PC5	PC6
Standard deviation	3.644394	2.385656	1.678675	1.407352	1.284029	1.098798
Proportion of Variance	0.442720	0.189710	0.093930	0.066020	0.054960	0.040250
Cumulative Proportion	0.442720	0.632430	0.726360	0.792390	0.847340	0.887590
	PC7	PC8	PC9	PC10	PC11	
Standard deviation	0.8217178	0.6903746	0.6456739	0.5921938	0.5421399	
Proportion of Variance	0.0225100	0.0158900	0.0139000	0.0116900	0.0098000	
Cumulative Proportion	0.9101000	0.9259800	0.9398800	0.9515700	0.9613700	
	PC12	PC13	PC14	PC15	PC16	
Standard deviation	0.5110395	0.4912815	0.3962445	0.3068142	0.2826001	
Proportion of Variance	0.0087100	0.0080500	0.0052300	0.0031400	0.0026600	
Cumulative Proportion	0.9700700	0.9781200	0.9833500	0.9864900	0.9891500	
	PC17	PC18	PC19	PC20	PC21	
Standard deviation	0.2437192	0.2293878	0.2224356	0.1765203	0.1731268	

```

Proportion of Variance 0.0019800 0.0017500 0.0016500 0.0010400 0.0010000
Cumulative Proportion 0.9911300 0.9928800 0.9945300 0.9955700 0.9965700
PC22 PC23 PC24 PC25 PC26
Standard deviation 0.1656484 0.1560155 0.1343689 0.1244238 0.0904303
Proportion of Variance 0.0009100 0.0008100 0.0006000 0.0005200 0.0002700
Cumulative Proportion 0.9974900 0.9983000 0.9989000 0.9994200 0.9996900
PC27 PC28 PC29 PC30
Standard deviation 0.08306903 0.0398665 0.02736427 0.01153451
Proportion of Variance 0.00023000 0.0000500 0.00002000 0.00000000
Cumulative Proportion 0.99992000 0.9999700 1.00000000 1.00000000

```

```

pr.var <- wisc.pr$sdev^2
head(pr.var)

```

```
[1] 13.281608 5.691355 2.817949 1.980640 1.648731 1.207357
```

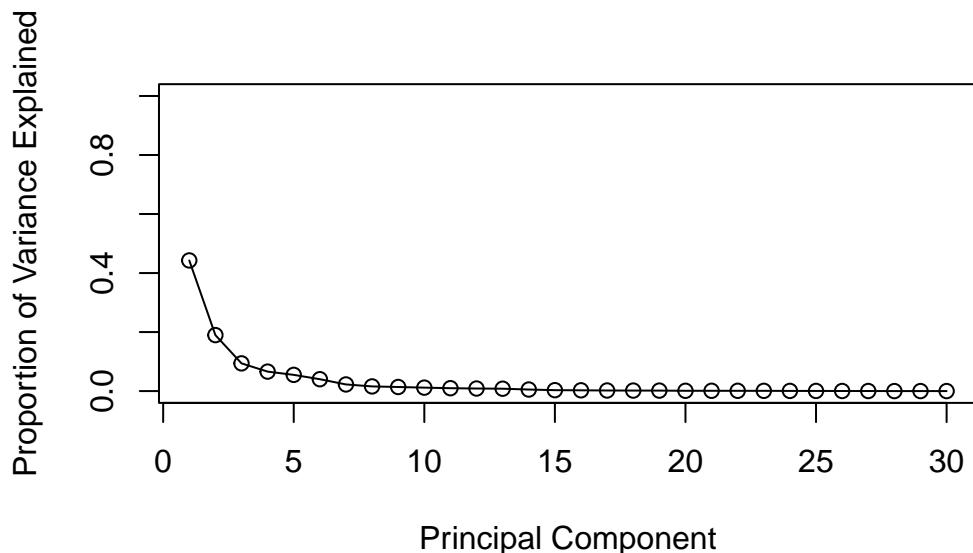
Variance explained by each principal component: pve

```
pve <- pr.var / sum(pr.var)
```

```

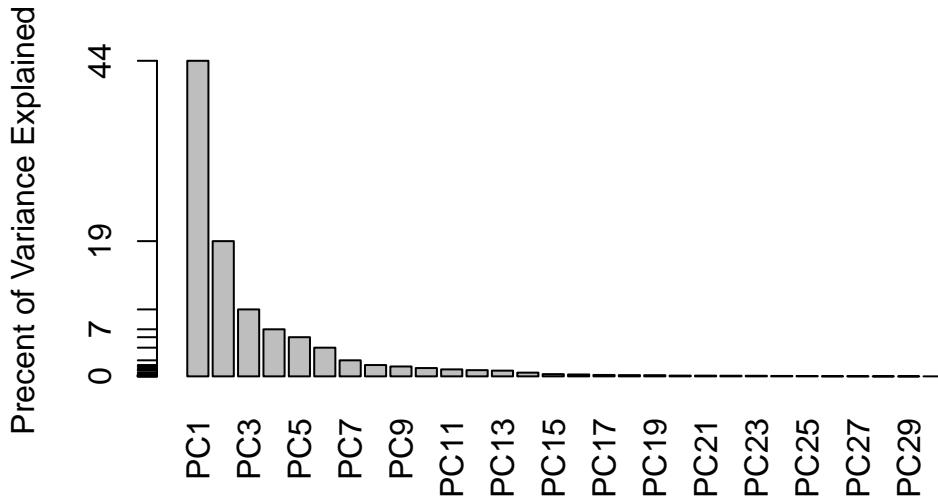
plot(pve, xlab = "Principal Component",
      ylab = "Proportion of Variance Explained",
      ylim = c(0, 1), type = "o")

```



An alternative scree plot can be made

```
screeplot <- barplot(pve, ylab = "Percent of Variance Explained",
                      names.arg=paste0("PC",1:length(pve)), las=2, axes = FALSE)
axis(2, at=pve, labels=round(pve,2)*100 )
```



Q9. For the first principal component, what is the component of the loading vector (i.e. `wisc.pr$rotation[, 1]`) for the feature `concave.points_mean`?

```
wisc.pr$rotation["concave.points_mean", 1]
```

[1] -0.2608538

Q10. What is the minimum number of principal components required to explain 80% of the variance of the data?

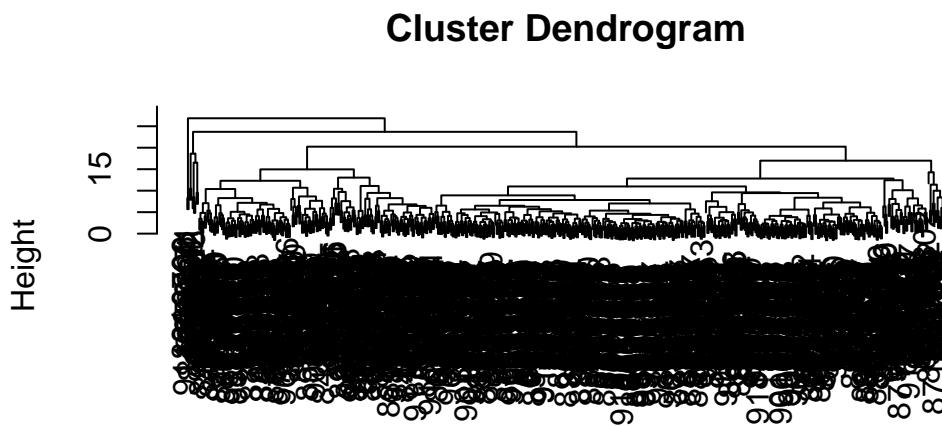
5 principal components are required to explain 80% of the variance of the data

Hierarchical clustering

Just clustering the original data is not very informative or helpful

```
data.scaled <- scale(wisc.data)
data.dist <- dist(data.scaled)
wisc.hclust <- hclust (data.dist)
```

```
plot(wisc.hclust)
```



```
    data.dist  
hclust (*, "complete")
```

```
wisc.hclust.clusters <- cutree(wisc.hclust, k=4)  
table(cutree(wisc.hclust, k=4))
```

1	2	3	4
177	7	383	2

```
table(wisc.hclust.clusters,diagnosis)
```

```

diagnosis
wisc.hclust.clusters   B    M
                           1 12 165
                           2 2  5
                           3 343 40
                           4 0  2

```

Combining methods (PCA and Clustering)

Clustering the original data was not very productive. The PCA results looked promising. Here we combined these methods by clustering from our PCA results. In other words “clustering in PC space”

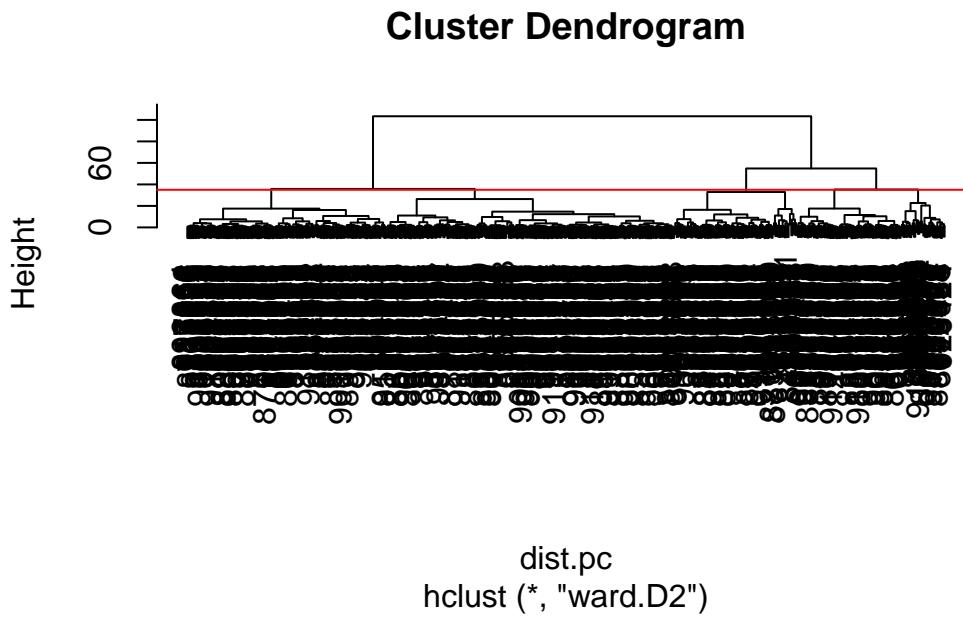
```
dist.pc <- dist(wisc.pr$x[,1:3])
wisc.pr.hclust <- hclust(dist.pc, method = "ward.D2")
```

Q11. Using the `plot()` and `abline()` functions, what is the height at which the clustering model has four clusters?

height=35 is when the clustering model of `wisc.pr.hclust` has four clusters.

View the tree...

```
plot(wisc.pr.hclust)
abline(h=35, col="red")
```



To get out clustering membership vector (i.e. out main clustering result) we “cut” the tree at a desired height or to yield a desired number of “k”

```
grps <- cutree(wisc.pr.hclust, h=70)
table(grps)
```

```
grps
 1   2
203 366
```

How does this clustering grps compare to the expert diagnosis

```
table(grps, diagnosis)
```

grps	B	M
1	24	179
2	333	33

Q12. Can you find a better cluster vs diagnoses match by cutting into a different number of clusters between 2 and 10?

Yes, because there is less split of the data. When there is two clusters there is a split in data where there is a majority of M in one and B in the other.

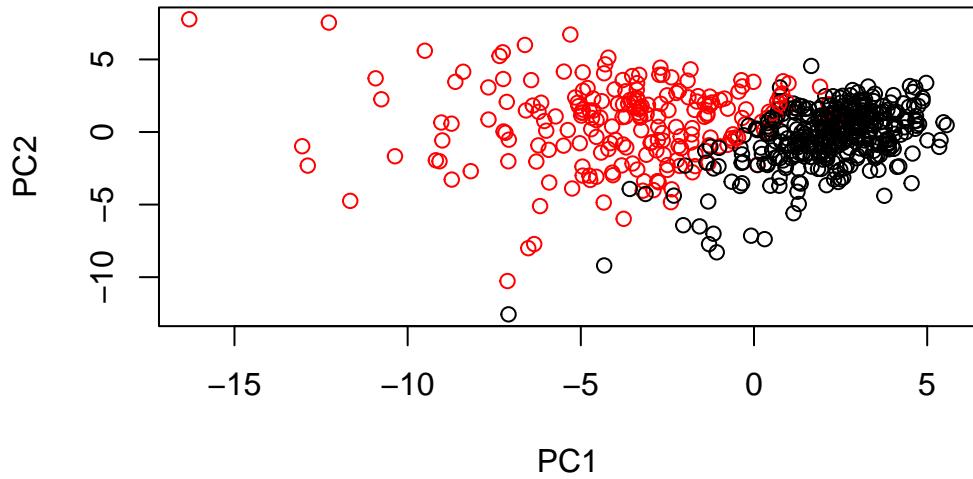
Q13. Which method gives your favorite results for the same data.dist dataset?
Explain your reasoning.

Using `ward.D2` provides a clear separation between M and B samples that were both balanced. Overall, M and B were accurately grouped and a strong alignment in each cluster can be observed.

Combining Methods

Create a graph of PC1 and PC2

```
col <- ifelse(diagnosis == "M", "red", "black")
plot(wisc.pr$x[,1:2], col=col)
```



Re-order the factor and re plot

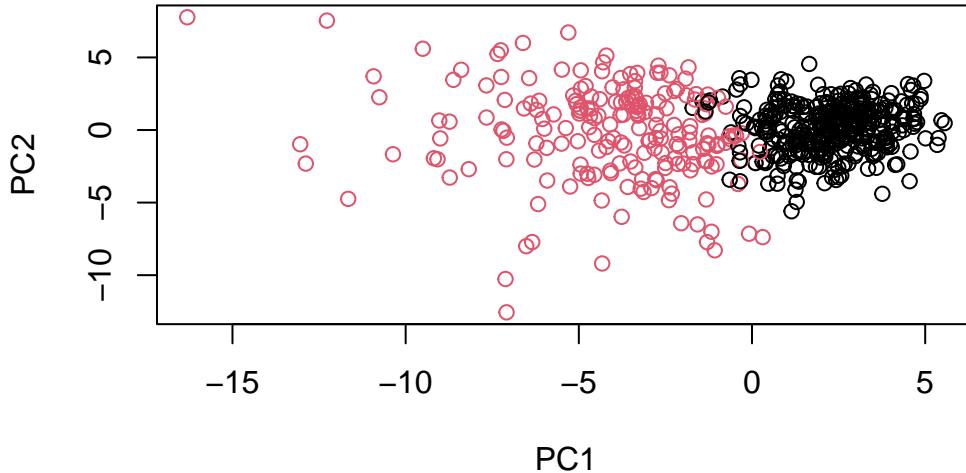
```
g <- as.factor(grps)
levels(g)
```

```
[1] "1" "2"
```

```
g <- relevel(g,2)
levels(g)
```

```
[1] "2" "1"
```

```
plot(wisc.pr$x[,1:2], col=g)
```



Cut this model into two clusters and assign to `wisc.pr.hclust.clusters`

```
wisc.pr.hclust.clusters <- cutree(wisc.pr.hclust, k=2)
table(wisc.pr.hclust.clusters, diagnosis)
```

		diagnosis	
		B	M
wisc.pr.hclust.clusters	1	24	179
	2	333	33

Q15. How well does the newly created model with four clusters separate out the two diagnoses?

There is a distinct and balanced separation of the four clusters. Cluster 1 consists of majority M samples and cluster 2 consists of majority B samples.

Q16. How well do the k-means and hierarchical clustering models you created in previous sections (i.e. before PCA) do in terms of separating the diagnoses? Again, use the `table()` function to compare the output of each model (`wisc.km$cluster` and `wisc.hclust.clusters`) with the vector containing the actual diagnoses.

The k-means model separates the diagnoses well however there is some overlap. The hierarchical model shows a distinct separation but with four clusters instead of 2, thus fragmenting the separation.

Q17. Which of your analysis procedures resulted in a clustering model with the best specificity?
How about sensitivity?

Hierarchical clustering is both higher in sensitivity and specificity than the k means model.
This was concluded as there were greater benign and malignant samples that were correctly grouped.

Sensitivity: $TP/(TP+FN)$ Specificity: $TN/(TN+FN)$

7. Prediction

We can use our PCA model for prediction with new input patient samples.

```
#url <- "new_samples.csv"  
url <- "https://tinyurl.com/new-samples-CSV"  
new <- read.csv(url)  
npc <- predict(wisc.pr, newdata=new)  
npc
```

	PC1	PC2	PC3	PC4	PC5	PC6	PC7
[1,]	2.576616	-3.135913	1.3990492	-0.7631950	2.781648	-0.8150185	-0.3959098
[2,]	-4.754928	-3.009033	-0.1660946	-0.6052952	-1.140698	-1.2189945	0.8193031
	PC8	PC9	PC10	PC11	PC12	PC13	PC14
[1,]	-0.2307350	0.1029569	-0.9272861	0.3411457	0.375921	0.1610764	1.187882
[2,]	-0.3307423	0.5281896	-0.4855301	0.7173233	-1.185917	0.5893856	0.303029
	PC15	PC16	PC17	PC18	PC19	PC20	
[1,]	0.3216974	-0.1743616	-0.07875393	-0.11207028	-0.08802955	-0.2495216	
[2,]	0.1299153	0.1448061	-0.40509706	0.06565549	0.25591230	-0.4289500	
	PC21	PC22	PC23	PC24	PC25	PC26	
[1,]	0.1228233	0.09358453	0.08347651	0.1223396	0.02124121	0.078884581	
[2,]	-0.1224776	0.01732146	0.06316631	-0.2338618	-0.20755948	-0.009833238	
	PC27	PC28	PC29	PC30			
[1,]	0.220199544	-0.02946023	-0.015620933	0.005269029			
[2,]	-0.001134152	0.09638361	0.002795349	-0.019015820			

Q18. Which of these new patients should we prioritize for follow up based on your results?

We should prioritize patient 2 due to closer clustering associated with a malignant disease diagnosis. They are a higher risk group for malignant disease.