

AP® Computer Science A Elevens Lab Student Guide

The AP Program wishes to acknowledge and thank the following individuals for their contributions in developing this lab and the accompanying documentation.

Michael Clancy: University of California at Berkeley

Robert Glen Martin: School for the Talented and Gifted in Dallas, TX

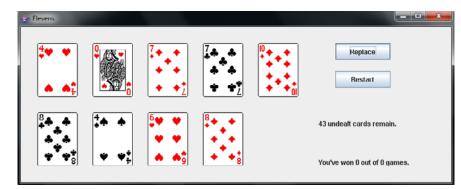
Judith Hromcik: School for the Talented and Gifted in Dallas, TX



Elevens Lab Student Guide

Introduction

The following activities are related to a simple solitaire game called Elevens. You will learn the rules of Elevens, and will be able to play it by using the supplied Graphical User Interface (GUI) shown at the right. You will learn about the design and the Object Oriented Principles that



suggested that design. You will also implement much of the code.

Table of Contents

Introduction	1
Activity 1: Design and Create a Card Class	3
Activity 2: Initial Design of a Deck Class	5
Activity 3: Shuffling the Cards in a Deck	7
Activity 4: Adding a Shuffle Method to the Deck Class	11
Activity 5: Testing with Assertions (Optional)	
Activity 6: Playing Elevens	19
Activity 7: Elevens Board Class Design	21
Activity 8: Using an Abstract Board Class	25
Activity 9: Implementing the Elevens Board	29
Activity 10: ThirteensBoard (Optional)	
Activity 11: Simulation of Elevens (Optional)	35
Glossary	39
References	40

Activity 1: Design and Create a Card Class

Introduction:

In this activity, you will complete a Card class that will be used to create card objects.

Think about card games you've played. What kinds of information do these games require a card object to "know"? What kinds of operations do these games require a card object to provide?

Exploration:

Now think about implementing a class to represent a playing card. What instance variables should it have? What methods should it provide? Discuss your ideas for this Card class with classmates.

Read the partial implementation of the Card class available in the Activity1 Starter Code folder. As you read through this class, you will notice the use of the @Override annotation before the toString method. The Java @Override annotation can be used to indicate that a method is intended to override a method in a superclass. In this example, the Object class's toString method is being overridden in the Card class. If the indicated method doesn't override a method, then the Java compiler will give an error message.

Here's a situation where this facility comes in handy. Programmers new to Java often encounter problems matching headings of overridden methods to the superclass's original method heading. For example, in the Weight class below, the tostring method is intended to be invoked when tostring is called for a Weight object.

```
public class Weight {
   private int pounds;
   private int ounces;
        ...

public String tostring(String str) {
    return this.pounds + " lb. " + this.ounces + " oz.";
   }
   ...
}
```

Unfortunately, this doesn't work; the tostring method given above has a different name and a different signature from the Object class's toString method. The correct version below has the correct name toString and no parameter:

```
public String toString() {
   return this.pounds + " lb. " + this.ounces + " oz.";
}
```

The @Override annotation would cause an error message for the first tostring version to alert the programmer of the errors.

Exercises:

- 1. Complete the implementation of the provided Card class. You will be required to complete:
 - a. a constructor that takes two String parameters that represent the card's rank and suit, and an int parameter that represents the point value of the card;
 - b. accessor methods for the card's rank, suit, and point value;
 - c. a method to test equality between two card objects; and
 - d. the toString method to create a String that contains the rank, suit, and point value of the card object. The string should be in the following format:

```
rank of suit (point value = pointValue)
```

2. Once you have completed the Card class, find the CardTester.java file in the Activity1 Starter Code folder. Create three Card objects and test each method for each Card object.

Activity 2: Initial Design of a Deck Class

Introduction:

Think about a deck of cards. How would you describe a deck of cards? When you play card games, what kinds of operations do these games require a deck to provide?

Exploration:

Now consider implementing a class to represent a deck of cards. Describe its instance variables and methods, and discuss your design with a classmate.

Read the partial implementation of the Deck class available in the Activity2 Starter Code folder. This file contains the instance variables, constructor header, and method headers for a Deck class general enough to be useful for a variety of card games. Discuss the Deck class with your classmates; in particular, make sure you understand the role of each of the parameters to the Deck constructor, and of each of the private instance variables in the Deck class.

Exercises:

- 1. Complete the implementation of the Deck class by coding each of the following:

```
For example, if ranks = {"A", "B", "C"}, suits = {"Giraffes", "Lions"}, and values = {2,1,6}, the constructor would create the following cards:
```

```
["A", "Giraffes", 2], ["B", "Giraffes", 1], ["C", "Giraffes", 6],
["A", "Lions", 2], ["B", "Lions", 1], ["C", "Lions", 6]
```

and would add each of them to cards. The parameter size would then be set to the size of cards, which in this example is 6.

Finally, the constructor should shuffle the deck by calling the shuffle method. Note that you will not be implementing the shuffle method until Activity 4.

- isEmpty This method should return true when the size of the deck is 0; false otherwise.
- size This method returns the number of cards in the deck that are left to be dealt.

• deal — This method "deals" a card by removing a card from the deck and returning it, if there are any cards in the deck left to be dealt. It returns <code>null</code> if the deck is empty. There are several ways of accomplishing this task. Here are two possible algorithms:

Algorithm 1: Because the cards are being held in an ArrayList, it would be easy to simply call the List method that removes an object at a specified index, and return that object. Removing the object from the end of the list would be more efficient than removing it from the beginning of the list. Note that the use of this algorithm also requires a separate "discard" list to keep track of the dealt cards. This is necessary so that the dealt cards can be reshuffled and dealt again.

Algorithm 2: It would be more efficient to leave the cards in the list. Instead of removing the card, simply decrement the size instance variable and then return the card at size. In this algorithm, the size instance variable does double duty; it determines which card to "deal" and it also represents how many cards in the deck are left to be dealt. This is the algorithm that you should implement.

2. Once you have completed the Deck class, find DeckTester.java file in the Activity2 Starter Code folder. Add code in the main method to create three Deck objects and test each method for each Deck object.

Questions:

- 1. Explain in your own words the relationship between a deck and a card.
- 2. Consider the deck initialized with the statements below. How many cards does the deck contain?

```
String[] ranks = {"jack", "queen", "king"};
String[] suits = {"blue", "red"};
int[] pointValues = {11, 12, 13};
Deck d = new Deck(ranks, suits, pointValues);
```

3. The game of Twenty-One is played with a deck of 52 cards. Ranks run from ace (highest) down to 2 (lowest). Suits are spades, hearts, diamonds, and clubs as in many other games. A face card has point value 10; an ace has point value 11; point values for 2, ..., 10 are 2, ..., 10, respectively. Specify the contents of the ranks, suits, and pointValues arrays so that the statement

```
Deck d = new Deck(ranks, suits, pointValues);
```

initializes a deck for a Twenty-One game.

4. Does the order of elements of the ranks, suits, and pointValues arrays matter?

Activity 3: Shuffling the Cards in a Deck

Introduction:

Think about how you shuffle a deck of cards by hand. How well do you think it randomizes the cards in the deck?

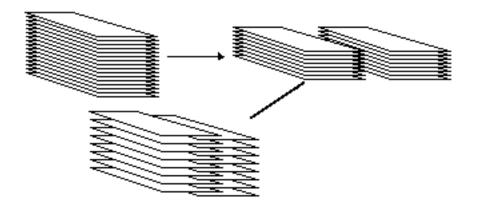
Exploration:

We now consider the *shuffling* of a deck, that is, the *permutation* of its cards into a random-looking sequence. A requirement of the shuffling procedure is that any particular permutation has just as much chance of occurring as any other. We will be using the Math.random method to generate random numbers to produce these permutations.

Several ideas for designing a shuffling method come to mind. We will consider two:

Perfect Shuffle

Card players often shuffle by splitting the deck in half and then interleaving the two half-decks, as shown below.



This procedure is called a *perfect shuffle* if the interleaving alternates between the two half-decks. Unfortunately, the perfect shuffle comes nowhere near generating all possible deck permutations. In fact, eight shuffles of a 52-card deck return the deck to its original state!

Consider the following "perfect shuffle" algorithm that starts with an array named cards that contains 52 cards and creates an array named shuffled.

This approach moves the first half of cards to the even index positions of shuffled, and it moves the second half of cards to the odd index positions of shuffled.

The above algorithm shuffles 52 cards. If an odd number of cards is shuffled, the array shuffled has one more even-indexed position than odd-indexed positions. Therefore, the first loop must copy one more card than the second loop does. This requires rounding up when calculating the index of the middle of the deck. In other words, in the first loop j must go up to (cards.length + 1) / 2, exclusive, and in the second loop j most begin at (cards.length + 1) / 2.

Selection Shuffle

Consider the following algorithm that starts with an array named cards that contains 52 cards and creates an array named shuffled. We will call this algorithm the "selection shuffle."

This approach finds a suitable card for the k^{th} position of the deck. Unsuitable candidates are any cards that have already been placed in the deck.

While this is a more promising approach than the perfect shuffle, its big defect is that it runs too slowly. Every time an empty element is selected, it has to loop again. To determine the last element of shuffled requires an average of 52 calls to the random number generator.

A better version, the "efficient selection shuffle," works as follows:

```
For k = 51 down to 1,
Generate a random integer r between 0 and k, inclusive;
Exchange cards[k] and cards[r].
```

This has the same structure as selection sort:

The selection shuffle algorithm does not require to a loop to find the largest (or smallest) value to swap, so it works quickly.

Exercises:

- 1. Use the file Shuffler.java, found in the **Activity3 Starter Code**, to implement the perfect shuffle and the efficient selection shuffle methods as described in the **Exploration** section of this activity. You will be shuffling arrays of integers.
- 2. Shuffler.java also provides a main method that calls the shuffling methods. Execute the main method and inspect the output to see how well each shuffle method actually randomizes the array elements. You should execute main with different values of SHUFFLE_COUNT and VALUE COUNT.

Questions:

- 1. Write a static method named flip that simulates a flip of a weighted coin by returning either "heads" or "tails" each time it is called. The coin is twice as likely to turn up heads as tails. Thus, flip should return "heads" about twice as often as it returns "tails."
- 2. Write a static method named are Permutations that, given two int arrays of the same length but with no duplicate elements, returns true if one array is a permutation of the other (i.e., the arrays differ only in how their contents are arranged). Otherwise, it should return false.
- 3. Suppose that the initial contents of the values array in Shuffler.java are {1, 2, 3, 4}. For what sequence of random integers would the efficient selection shuffle change values to contain {4, 3, 2, 1}?

Activity 4: Adding a Shuffle Method to the Deck Class

Introduction:

You implemented a Deck class in Activity 2. This class should be complete except for the shuffle method. You also implemented a DeckTester class that you used to test your incomplete Deck class.

In Activity 3, you implemented methods in the Shuffler class, which shuffled integers.

Now you will use what you learned about shuffling in Activity 3 to implement the Deck shuffle method.

Exercises:

- 1. The file Deck.java, found in the **Activity4 Starter Code** folder, is a correct solution from Activity 2. Complete the Deck class by implementing the shuffle method. Use the efficient selection shuffle algorithm from Activity 3.
 - Note that the Deck constructor creates the deck and then calls the shuffle method. The shuffle method also needs to reset the value of size to indicate that all of the cards can be dealt again.
- 2. The DeckTester.java file, found in the Activity4 Starter Code folder, provides a basic set of Deck tests. It is similar to the DeckTester class you might have written in Activity 2. Add additional code at the bottom of the main method to create a standard deck of 52 cards and test the shuffle method. You can use the Deck toString method to "see" the cards after every shuffle.

Activity 5: Testing with Assertions (Optional)

Introduction:

In the previous activities, you were asked to design and implement the Card and Deck classes. Upon completion of those tasks, you were instructed to test those classes by creating objects and testing each of the class' methods. In this activity, we will take a more formal approach to testing and introduce the Java assert statement.

Exploration:

What is the purpose of testing? Programmers make mistakes. These range from misunderstanding an algorithm or a problem specification (the most serious), to simple typing errors. The purpose of program testing is to find as many of those mistakes as possible. Let's consider some aspects of testing.

Efficient and organized testing

How should we test a program? Clearly, we need to run the program and see whether its behavior matches what is intended. There's more to it than that, though. Good testing is *systematic*. A programmer should pick test cases not at random but in a way more likely to find errors. For example, one should choose test runs that collectively exercise all parts of a program. Code that isn't executed may contain bugs. Good testing is also *programmer-efficient*. Tests should be easy to run. Test cases should be chosen to be as simple as possible while still being complex enough to expose errors. Simple test cases can also make it easier to see what a program is doing wrong.

For this activity, we will focus on finding two kinds of errors:

- Inconsistencies, where two parts of the program have different expectations about a variable's value, for example; and
- Common "typos of the brain," such as off-by-one errors and substitution of one operator for another (such as using > instead of <).

Our tests will all involve *assertions*, boolean expressions that should be true if the program is running correctly. We will incorporate our tests in a "tester" class whose main method executes the tests.

Assertions in Java

Our testing code will use the Java assert statement. This statement has the following form:

```
assert booleanExpression : StringExpression;
```

If the value of boolean Expression is true, the program continues with the next statement. If the value of boolean Expression is false, the program throws an Assertion Error exception and prints String Expression. It also prints a Stack Trace (more on that later). Here's an example using assert.

```
Card c1 = new Card("ace", "hearts", 1);
Card c2 = new Card("ace", "hearts", 1);
assert c1.matches(c2) : "Duplicate cards do not match.";
```

This code creates two new Card objects, and then checks that they contain the same information. If cl.matches(c2) returns true, then execution continues with the next statement. However, if the program has an error which results in cl.matches(c2) returning false, an AssertionError is thrown and the message "Duplicate cards do not match." is output.

Assertions are *disabled* by default. To use them, the command-line option -ea (Enable Assertions) is used. For example, the following would run the main method in CardTester with assertions enabled:

```
java -ea CardTester
```

Organizing tests of the Card class

We move on to test the Card class. Cards have a constructor and several methods (suit, rank, pointValue, matches, and toString). Our tests must cover all of these methods.

First, we create a file named CardTester.java. This name was chosen to describe its purpose. Its main method will start by creating some Card objects that will be used to do the testing:

```
Card c1 = new Card("ace", "hearts", 1);
Card c2 = new Card("ace", "hearts", 1);
Card c3 = new Card("ace", "hearts", 2);
Card c4 = new Card("ace", "spades", 1);
Card c5 = new Card("king", "hearts", 1);
Card c6 = new Card("queen", "clubs", 3);
```

The first two cards are identical. Cards c3, c4, and c5 each differ from c1 in only one of the instance variable values. These "one difference" cards will help us find copy/paste errors; for example, if the body of suit was copied from rank and pasted without change. The last card is different from the others in all of the values.

We start by testing the Card accessor methods. These tests merely check, using cards with completely different information, that what's stored is what was provided in the constructor. Note the inclusion in the String message of information about which value was involved in each assertion.

Next, we test the Card method matches. Two cards match if and only if they have the same rank, suit, and point values. A likely implementation of matches will involve some comparisons and some uses of &&. Common bugs are the copy/paste error mentioned above and the substitution of || for &&. Comparing c1 to all the others should reveal these kinds of errors.

```
assert c1.matches(c1) : "Card doesn't match itself: " + c1;
assert c1.matches(c2) : "Duplicate cards aren't equal: " + c1;
assert !c1.matches(c3)
    : "Different cards are equal: " + c1 + ", " + c3;
assert !c1.matches(c4)
    : "Different cards are equal: " + c1 + ", " + c4;
assert !c1.matches(c5)
    : "Different cards are equal: " + c1 + ", " + c5;
assert !c1.matches(c6)
    : "Different cards are equal: " + c1 + ", " + c6;
```

Finally, we test toString, again on two completely different objects.

```
assert c1.toString().equals("ace of hearts (point value = 1)")
   : "Wrong toString: " + c1;
assert c6.toString().equals("queen of clubs (point value = 3)")
   : "Wrong toString: " + c6;
```

If all of the tests pass, we provide a message that says so:

```
System.out.println("All tests passed!");
```

Systematic testing

Cards didn't involve any data structures more complicated than strings. When testing a class with more complex structures, it makes sense to start small. With a Deck class, for example, it might make sense to first provide tests that use a 1-card deck, and then a 2-card deck with different cards.

But, would all these tests get out of control? Just as in other programming you've done, it makes sense to split a long sequence of statements into "helper" methods. The result may be a smaller test program, and some of the assertion sequences might be easier to reuse. The main method in a DeckTester class might be the following:

```
public static void main(String[] args) {
   test1CardDeck();
   test2CardDeck();
   testShuffle();
   System.out.println("All tests passed!");
}
```

Exercises:

1. The folder Activity5 Starter Code contains the four subfolders Buggy1, Buggy2, Buggy3, and Buggy4. Each of these contains a different buggy version of the Deck class. These buggy decks have been precompiled; only the Deck.class bytecode file is included. These buggy versions each contain one error caused by either moving a statement, or substituting one symbol for another, e.g., 1 for 0 or > for <. Test each of them with the DeckTester application provided in each folder:

```
java -ea DeckTester
```

If you are using a Windows-based system, you can just execute the provided **DeckTester.bat** file.

Each of the four different <code>DeckTester</code> runs will produce an <code>AssertionError</code> exception, along with information about why the error occurred. For each error that occurs, write down which method or constructor of the buggy <code>Deck</code> class could contain the bug, and make an educated guess about the cause of the error. You might find it helpful to refer to your completed <code>Deck</code> class from Activity 4.

Note: The Buggy1 test will produce output similar to the following:

```
... >java -ea DeckTester
Exception in thread "main" java.lang.AssertionError: isEmpty is
false for an empty deck.
   at DeckTester.testEmpty(DeckTester.java:98)
   at DeckTester.test1CardDeck(DeckTester.java:28)
   at DeckTester.main(DeckTester.java:12)
```

The last three lines of output are a stack trace that tells you that the

- AssertionError occurred in the testEmpty method at line 98.
- testEmpty method was called from the test1CardDeck method at line 28.
- test1CardDeck method was called from the main method at line 12.

Record your conclusions below: **Buggy1:** Constructor or Method (write method name): Describe a Possible Code Error: **Buggy2:** Constructor or Method (write method name): Describe a Possible Code Error: **Buggy3:** Constructor or Method (write method name): Describe a Possible Code Error:

Buggy4:	
Constructor or Method (write method name):	
Describe a Possible Code Error:	

2. Now, examine the Buggy5 folder. This folder contains a Deck.java file with multiple errors. Use DeckTester to help you find the errors. Correct each error until the Deck class has passed all of its tests.

Note that you may receive a runtime error other than AssertionError when running DeckTester. If so, you may find it helpful to switch the order of 1-card deck and 2-card deck tests as follows:

```
public static void main(String[] args) {
   test2CardDeck();  // order swapped
   test1CardDeck();  // order swapped
   testShuffle();
   System.out.println("All tests passed!");
}
```

Activity 6: Playing Elevens

Introduction:

In this activity, the game Elevens will be explained, and you will play an interactive version of the game.

Exploration:

The solitaire game of Elevens uses a deck of 52 cards, with ranks A (ace), 2, 3, 4, 5, 6, 7, 8, 9, 10, J (jack), Q (queen), and K (king), and suits \clubsuit (clubs), \blacklozenge (diamonds), \blacktriangledown (hearts), and \spadesuit (spades). Here is how it is played.

- 1. The deck is shuffled, and nine cards are dealt "face up" from the deck to the board.
- 2. Then the following sequence of steps is repeated:
 - a. The player removes each pair of cards (A, 2, ..., 10) that total 11, e.g., an 8 and a 3, or a 10 and an A. An ace is worth 1, and suits are ignored when determining cards to remove.
 - b. Any triplet consisting of a J, a Q, and a K is also removed by the player. Suits are also ignored when determining which cards to remove.
 - c. Cards are dealt from the deck if possible to replace the cards just removed.

The game is won when the deck is empty and no cards remain on the table. Here's a sample game, in which underlined cards are replacements from the deck.

Card	s on th	e Tabl	le						Explanation
K♠	10♦	J .	2.	2♥	9♦	3♥	5♠	5♦	initial deal
K♠	10♦	J .	<u>7♦</u>	2♥	<u>Q</u> ♠	3♥	5♠	5♦	remove 2♣ (either 2 would work) and 9♦
<u>A</u> ♠	10♦	<u>9*</u>	7♦	2♥	<u>7♣</u>	3♥	5♠	5♦	remove J♣ Q♠ K♠
A.	10♦	<u>10♠</u>	7♦	<u>3*</u>	7 .	3♥	5 ^	5♦	remove 9♣ and 2♥ (removing A♠ and 10♦ would have been legal here too)
<u>2♠</u>	10♦	<u>9</u>	7♦	3♣	7 .	3♥	5♠	5♦	remove A♠ and 10♠ (10♠ could have been removed instead)
<u>A♣</u>	10♦	<u>K</u> ♦	7♦	3♣	7 .	3♥	5♠	5♦	remove 2♠ and 9♠
<u>6</u> ♦	<u>K♣</u>	K♦	7♦	3 .	7 .	3♥	5♠	5♦	remove A♣ and 10♦

 $2 \bullet$ K♣ K♦ $7 \bullet$ 3♣ 7 ♣ 3♥ 5♠ $Q \bullet$ remove $6 \bullet$ and one of the 5s; no further plays are possible; game is lost.

An interactive GUI version of Elevens allows one to play by clicking card images and buttons rather than by handling actual cards. When Elevens.jar is run, the cards on the board are displayed in a window. Clicking on an unselected card selects it; clicking on a selected card unselects it. Clicking on the **Replace** button first checks that the selection is legal; if so, it does the removal and deals cards to fill the empty slots. Clicking on the **Restart** button restarts the game.

The folder **Activity6 Starter Code** contains the file Elevens.jar that, when executed, runs a GUI-based implementation. In a Windows environment, you may be able to run it by double-clicking on it. Otherwise you can run it with the command

```
java -jar Elevens.jar
```

Play a few games of Elevens. How many did you win?

Questions:

- 1. List all possible plays for the board 5♠ 4♥ 2♦ 6♣ A♠ J♥ K♦ 5♣ 2♠
- 2. If the deck is empty and the board has three cards left, must they be J, Q, and K? Why or why not?

3. Does the game involve any strategy? That is, when more than one play is possible, does it matter which one is chosen? Briefly explain your answer.

Activity 7: Elevens Board Class Design

Introduction:

Now that the Card and Deck classes are completed, the next class to design is ElevensBoard. This class will contain the state (instance variables) and behavior (methods) necessary to play the game of Elevens.

Questions:

1. What items would be necessary if you were playing a game of Elevens at your desk (not on the computer)? List the private instance variables needed for the ElevensBoard class.

2. Write an algorithm that describes the actions necessary to play the Elevens game.

3. Now examine the partially implemented ElevensBoard.java file found in the Activity7 Starter Code directory. Does the ElevensBoard class contain all the state and behavior necessary to play the game?

- 4. ElevensBoard.java contains three helper methods. These helper methods are private because they are only called from the ElevensBoard class.
 - a. Where is the dealMyCards method called in ElevensBoard?

b. Which public methods should call the contains Pair Sum 11 and contains JQK methods?

c. It's important to understand how the <code>cardIndexes</code> method works, and how the list that it returns is used. Suppose that <code>cards</code> contains the elements shown below. Trace the execution of the <code>cardIndexes</code> method to determine what list will be returned. Complete the diagram below by filling in the elements of the returned list, and by showing how those values index <code>cards</code>. Note that the returned list may have less than 9 elements.

	•	_	2	_	-	•	•	,	O
cards ->	J♥	6 .	null	2♠	null	null	A 🌲	4♥	null

1 >	0	1	2	3	4	5	6	7	8
returned ->							i		: :
list				ļ	ļ	ļ	ļ	į	; ;

d. Complete the following printCards method to print all of the elements of cards that are indexed by cIndexes.

```
public static printCards(ElevensBoard board) {
   List<Integer> cIndexes = board.cardIndexes();

/* Your code goes here. */
```

e. Which one of the methods that you identified in question 4b above needs to call the cardIndexes method before calling the containsPairSum11 and containsJQK methods? Why?

Activity 8: Using an Abstract Board Class

Introduction:

The Elevens game belongs to a set of related solitaire games. In this activity you will learn about some of these related games. Then you will see how inheritance can be used to reuse the code that is common to all of these games without rewriting it.

Exploration: Related Games

Thirteens

A game related to Elevens, called *Thirteens*, uses a 10-card board. Ace, 2, ..., 10, jack, queen correspond to the point values of 1, 2, ..., 10, 11, 12. Pairs of cards whose point values add up to 13 are selected and removed. Kings are selected and removed singly. Chances of winning are claimed to be about 1 out of 2.

Tens

Another relative of Elevens, called *Tens*, uses a 13-card board. Pairs of cards whose point values add to 10 are selected and removed, as are quartets of kings, queens, jacks, and tens, all of the same rank (for example, $K \spadesuit$, $K \heartsuit$, $K \diamondsuit$, and $K \clubsuit$). Chances of winning are claimed to be about 1 in 8 games.

Exploration: Abstract Classes

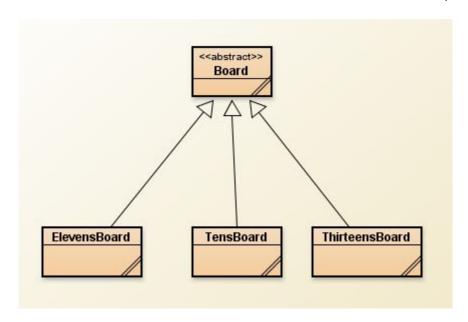
In reading the descriptions of Elevens and its related games, it is evident that these games share common state and behaviors. Each game requires:

- State (instance variables) a deck of cards and the cards "on the" board.
- Behavior (methods) to deal the cards, to remove and replace selected cards, to check for a win, to check if selected cards satisfy the rules of the game, to see if there are more legal selections available, and so on.

With all of this state and behavior in common, it would seem that inheritance could allow us to write code once and reuse it, instead of having to copy it for each different game.

But how? If we use the "IS-A" test, a ThirteensBoard "IS-A" ElevensBoard is not true. They have a lot in common, but an inheritance relationship between the two does not exist. So how do we create an inheritance hierarchy to take advantage of the commonalities between these two related boards?

The answer is to use a common superclass. Take all the state and behavior that these boards have in common and put them into a new Board class. Then have ElevensBoard, TensBoard, and ThirteensBoard inherit from the Board class. This makes sense because each of them is just a different kind of board. An ElevensBoard "IS-A" Board, a ThirteensBoard "IS-A" Board, and a TensBoard "IS-A" Board. A diagram that shows the inheritance relationships of these classes is included below. Note that Board is shown as abstract. We'll discuss why later.



Let's see how this works out for dividing up our original ElevensBoard code from Activity 7. Because all these games need a deck and the cards on the board, all of the instance variables can go into Board. Some methods, like deal, will work the same for every game, so they should be in Board too. Methods like containsJQK are Elevens-specific and should be in ElevensBoard. So far, so good.

But what should we do with the <code>isLegal</code> and <code>anotherPlayIsPossible</code> methods? Every Elevens-related game will have both of these methods, but they need to work differently for each different game. That's exactly why Java has <code>abstract</code> methods. Because each of these games needs <code>isLegal</code> and <code>anotherPlayIsPossible</code> methods, we include those methods in <code>Board</code>. However, because the implementation of these methods depends on the specific game, we make them <code>abstract</code> in <code>Board</code> and don't include their implementations there. Also, because <code>Board</code> now contains <code>abstract</code> methods, it must also be specified as <code>abstract</code>. Finally, we override each of these <code>abstract</code> methods in the subclasses to implement their specific behavior for that game.

But if we have to implement <code>isLegal</code> and <code>anotherPlayIsPossible</code> in each game-specific board class, why do we need to have the <code>abstract</code> methods in <code>Board</code>? Consider a class the uses a board, such as the GUI program you used in Activity 6. Such a class is called a <code>client</code> of the <code>Board</code> class.

Activity 8 - 26 - Elevens Student Lab Guide

The GUI program does not actually need to know what kind of a game it is displaying! It only knows that

the board that was provided "IS-A" Board, and it only "knows" about the methods in the Board class. The GUI program is only able to call <code>isLegal</code> and <code>anotherPlayIsPossible</code> because they are included in <code>Board</code>.

Finally, we need to understand how the GUI program is able to execute the correct <code>isLegal</code> and <code>anotherPlayIsPossible</code> methods. When the GUI program starts, it is provided an object of a class that inherits from <code>Board</code>. If you want to play Elevens, you provide an <code>ElevensBoard</code> object. If you want to play Tens, you provide a <code>TensBoard</code> object. So, when the GUI program uses that object to call <code>isLegal</code> or <code>anotherPlayIsPossible</code>, it automatically uses the method implementation included in that particular object. This is known as <code>polymorphism</code>.

Questions:

1.	Discuss t	he simi	larities a	nd differences	between <i>Ei</i>	levens, '	Thirteens,	and <i>Tens</i> .
----	-----------	---------	------------	----------------	-------------------	-----------	------------	-------------------

2. As discussed previously, all of the instance variables are declared in the Board class. But it is the ElevensBoard class that "knows" the board size, and the ranks, suits, and point values of the cards in the deck. How do the Board instance variables get initialized with the ElevensBoard values? What is the exact mechanism?

3. Now examine the files Board.java, and ElevensBoard.java, found in the Activity8

Starter Code directory. Identify the abstract methods in Board.java. See how these methods are implemented in ElevensBoard. Do they cover all the differences between *Elevens*, *Thirteens*, and *Tens* as discussed in question 1? Why or why not?

Activity 9: Implementing the Elevens Board

Introduction:

In Activity 8, we refactored (reorganized) the original ElevensBoard class into a new Board class and a much smaller ElevensBoard class. The purpose of this change was to allow code reuse in new games such as Tens and Thirteens. Now you will complete the implementation of the methods in the refactored ElevensBoard class.

Exercises:

1. Complete the ElevensBoard class in the Activity9 Starter Code folder, implementing the following methods.

Abstract methods from the Board class:

a. isLegal — This method is described in the method heading and related comments below. The implementation should check the number of cards selected and utilize the ElevensBoard helper methods.

```
/**
 * Determines if the selected cards form a valid group for removal.
 * In Elevens, the legal groups are (1) a pair of non-face cards
 * whose values add to 11, and (2) a group of three cards consisting of
 * a jack, a queen, and a king in some order.
 * @param selectedCards the list of the indexes of the selected cards.
 * @return true if the selected cards form a valid group for removal;
 * false otherwise.
 */
@Override
public boolean isLegal(List<Integer> selectedCards)
```

b. anotherPlayIsPossible — This method should also utilize the helper methods. It should be very short.

```
/**
 * Determine if there are any legal plays left on the board.
 * In Elevens, there is a legal play if the board contains
 * (1) a pair of non-face cards whose values add to 11, or (2) a group
 * of three cards consisting of a jack, a queen, and a king in some order.
 * @return true if there is a legal play left on the board;
 * false otherwise.
 */
@Override
public boolean anotherPlayIsPossible()
```

ElevensBoard helper methods:

c. containsPairSum11 — This method determines if the selected elements of cards contain a pair of cards whose point values add to 11.

d. contains JQK — This method determines if the selected elements of cards contains a jack, a queen, and a king in some order.

When you have completed these methods, run the main method found in ElevensGUIRunner.java. Make sure that the Elevens game works correctly. Note that the cards directory must be in the same directory with your .class files.

Questions:

- 1. The size of the board is one of the differences between *Elevens* and *Thirteens*. Why is size not an abstract method?
- 2. Why are there no abstract methods dealing with the selection of the cards to be removed or replaced in the array cards?

3. Another way to create "IS-A" relationships is by implementing interfaces. Suppose that instead of creating an abstract Board class, we created the following Board interface, and had ElevensBoard implement it. Would this new scheme allow the Elevens GUI to call isLegal and anotherPlayIsPossible polymorphically? Would this alternate design work as well as the abstract Board class design? Why or why not?

```
public interface Board
{
   boolean isLegal(List<Integer> selectedCards);
   boolean anotherPlayIsPossible();
}
```

Activity 10: ThirteensBoard (Optional)

Introduction:

The purpose of this activity is to create the Thirteens game using the knowledge gained from implementing the Elevens game.

Exploration:

The rules for the Thirteens game are repeated below:

Thirteens

A game related to Elevens, called Thirteens, uses a 10-card board. Ace, 2, ..., 10, jack, queen correspond to the point values of 1, 2, ..., 10, 11, 12. Pairs of cards whose point values add up to 13 are selected and removed. Kings are selected and removed singly. Chances of winning are claimed to be about 1 out of 2.

Exercises:

- 1. The Activity10 Starter Code folder contains all the code for a complete working Elevens game. Review the code in the ElevensBoard class. Identify the changes that would be necessary to implement the Thirteens game.
- 2. Copy and paste the ElevensBoard.java file into a new file, ThirteensBoard.java. Make the necessary changes to this file to implement the Thirteens game.
- 3. The Activity10 Starter Code folder also contains the ElevensGUIRunner.java file that is shown below. This program creates the board (an ElevensBoard object). Then it creates the GUI (a CardGameGUI object). Finally, it displays the GUI by calling its displayGame method. Review the code in the ElevensGUIRunner class as shown below. Identify the changes that would be necessary to implement the Thirteens game.

```
/**
  * This is a class that plays the GUI version of the Elevens game.
  * See accompanying documents for a description of how Elevens is played.
  */
public class ElevensGUIRunner {
    /**
    * Plays the GUI version of Elevens.
    * @param args is not used.
```

```
*/
public static void main(String[] args) {
    Board board = new ElevensBoard();
    CardGameGUI gui = new CardGameGUI(board);
    gui.displayGame();
}
```

- 4. Copy and paste the ElevensGUIRunner.java file into a new file,
 ThirteensGUIRunner.java. Make the necessary changes to this file to implement the
 Thirteens game.
- 5. Run the ThirteensGUIRunner program and test your new Thirteens game.

Activity 11: Simulation of Elevens (Optional)

Introduction:

We have implemented two different solitaire games that we can play, Elevens and Thirteens. That is perfect if we want to entertain ourselves playing them. But what if we want to answer questions about the games? For example, what percentage of Elevens games can be won? You probably already have some idea about the answer to this question, but you might have to play thousands of games to have any real confidence in your answer. That's where *simulation* comes in.

Exploration:

A common computing application is the *simulation* of some process; in other words, writing a program that imitates the process in some way. The behaviors and state in the program represent key features of, and are said to provide a *model* for, the process. An example is a simulation of a household robot vacuum cleaner. Internally, the simulation program is keeping track of its environment, the battery level, and the amount of dust in its dust container, and is perhaps displaying them on a computer console. Program methods plot the robot's course through rooms in the "house" and determine when it is finished.

A simulation is useful when the process being simulated is too complicated, too slow, too dangerous, or too expensive to observe in the real world. Also, understanding the program helps one understand the process being simulated. For example, the producers of the robot vacuum cleaner would have used a simulation to debug its algorithms before starting to manufacture the actual robots.

A program is called *probabilistic* when its state change is affected by chance. One example is a traffic simulation, which has to account for cars unpredictably entering the traffic zone and driving at varying speeds. A more obvious example is a simulation of a game based on dice or spinners. In Elevens, the probabilistic element is the shuffling of the deck of cards.

To model random events, we use a *pseudo-random number generator* (the "pseudo" is usually omitted). In the <code>Deck shuffle</code> method, we used the <code>Math.random</code> method to generate our random numbers. This reliance on chance significantly complicates the task of verifying that a simulation is behaving correctly. The programmer needs to have a good idea of what output to expect. Also, a small number of outcomes of the chance events may produce misleading behavior. For example, four flips of a coin may produce all heads, but it would be a mistake to assume that this behavior would happen often. Ten thousand flips would produce the more reasonable outcome of around 50 percent heads and 50 percent tails. The typical probabilistic simulation involves a large number of calls to the random number generator to increase the likelihood that the output reflects expected behavior.

To simulate Elevens, we will need to model the "playing" of the game using program state and behavior. Let's see how the real world relates to the code:

STATE:

Real-world "data"	Program data
The deck of cards	A List of Card objects
The cards on the board	An array of Card objects

BEHAVIOR:

Real-world operations	Program operations
Locating cards to remove	Searching for specific groups of Card objects in the board (an 11-pair or a JQK-triplet)
Removing cards and replacing them	Removing Card objects from the board and replacing them with Card objects from the deck
Dealing a card	Removing a Card object from the deck

We have most of this code already written. We have already taken care of all the state requirements. The deck of cards is modeled by the cards list in the Deck class. And the cards on the board are represented by the cards array in the Board class. We have also written methods for most of the necessary behaviors. In fact, we only need to model the additional things you do when you are playing the game yourself!

In the exercises, you will use an ElevensSimulation class, which will play games of Elevens. It will need access to methods that mimic the actions you make when you play the game. What do you do when you play the game and why do you do it? Answer these questions:

- What do you do repeatedly to play a game?
- As you are scanning the cards on the board, what are you trying to find?
- Why do you decide to click on a group of cards?
- What happens when you click the **Replace** button?

We will model these behaviors with three new methods in the ElevensBoard class:

- playIfPossible Looks for a legal play and makes the play (if found). This is the only new method that ElevensSimulation needs to call directly. We could put all of our new code into this method, but it's helpful to divide it up using two new private helper methods.
- playPairSum11IfPossible Looks for an 11-pair and replaces it (if found).
- playJQKIfPossible Looks for a JQK-triplet and replaces it (if found).

Next we consider the implementation of playPairSum11IfPossible. This method needs to first determine if the board contains an 11-pair. Then, if it finds one, it needs to remove it. Of course, playPairSum11IfPossible could call containsPairSum11 to see if there is an 11-pair on the board. But containsPairSum11 doesn't return any information about the indexes of the two cards that make up the 11-pair. So, playPairSum11IfPossible would have to find the pair again before removing it. To avoid having to find the pair twice, we would need to copy the code from containsPairSum11 into playPairSum11IfPossible. Thankfully, there's a better way.

What if we change the containsPairSum11 method into a findPairSum11 method? In other words, instead of having a "contains" method that returns a boolean value, we have a "find" method that returns a list of the indexes of the two cards in the pair. If there is no 11-pair on the board, it will return an empty list. Now, playPairSum11IfPossible will be able to call findPairSum11, and if there is an 11-pair, it will already have the list of indexes needed to call the replaceSelectedCards method. This design eliminates both the duplicated code and the double work! We will need to make a similar modification to change the containsJQK method into a findJQK method for the playJQKIfPossible method to call.

Note that it's usually not possible to foresee everything during the initial design of a program. For example, in the GUI version of Elevens, there was no need for "find" methods. The person playing the game had that task. However, the "find" methods became useful when we got into the details of the simulation. So, program designs can and do change.

Of course, when we do an initial program design, we try to accommodate all the needs of the problem as we understand them. But we also try to keep the design flexible, so that we can accommodate future needs. One rule of program design is that methods should be private, unless there is a good reason for another class to call those methods. Because we initially made containsPairSum11 private, we know that no other class uses it. Therefore, it's safe to rename and change it.

Exercises:

- 1. First, examine the completed ElevensSimulation class in the Activity11 Starter Code folder. This simulation creates an ElevensBoard object, and uses it to play GAMES_TO_PLAY games of Elevens. Note that the only new ElevensBoard method used is playIfPossible.
- 2. Now make the necessary changes to the ElevensBoard class. Change containsPairSum11 into findPairSum11. You will need to change both the method heading and the method body. Note that the method's comment block has already been changed for you.

- 3. Change the isLegal and anotherPlayIsPossible methods to use findPairSum11 instead of containsPairSum11. Note that the board contains an 11-pair if and only if findPairSum11 (cIndexes).size() > 0.
- 4. Change containsJQK to findJQK in a similar fashion to the containsPairSum11 to findPairSum11 conversion you did in exercise 2 above. Again, the method's comment block has already been changed for you.
- 5. Change the isLegal and anotherPlayIsPossible methods to use findJQK instead of containsJQK. At this point, the Elevens GUI program should work just as it did before.
- 6. It's time to complete the ElevensBoard methods required by the ElevensSimulation class. First complete the public playIfPossible method, which is called from the ElevensSimulation class. This method will use the private playPairSum11IfPossible and playJQKIfPossible helper methods. Note that you will have to replace the return statement in the stubbed out method.
- 7. Complete the private playPairSum11IfPossible and playJQKIfPossible helper methods. Note that you will have to replace the return statements in the stubbed out methods.
- 8. Now it's time to test your simulation-related changes. Make sure that GAMES_TO_PLAY and I_AM_DEBUGGING are initialized to 1 and true respectively in ElevensSimulation. Also make sure that I_AM_DEBUGGING is initialized to true in ElevensBoard. Run the ElevensSimulation program a few times and examine the output. You should be able to see both 11-pairs and JQK-triplets being correctly identified and removed.

Questions:

- 1. Set the I_AM_DEBUGGING flags to false and GAMES_TO_PLAY to 10. Run the ElevensSimulation program a few times and record the percentage of games won for each run. What is the range of win percentages that you saw? Were the percentages fairly consistent, or did they vary quite a bit?
- 2. Increase the number of games to play to 100. Are the win percentages more consistent from run to run?
- 3. Experiment with simulating different numbers of games. How many games do you need to play in order to get consistent results from run to run?
- 4. Optional Repeat the above steps for the Thirteens game.

Glossary

- **assertion:** Boolean expressions that should be true if the program is running correctly. The Java assert statement can be used to check assertions in a program.
- **class invariant:** A logical statement relating to the values of the instance variables of a class that is always true between calls to the class's methods (also referred to as a "data invariant"). ("Invariant" means "not varying" or "not changing.")
- client class: A class that uses another class (e.g., The Deck class is a client of the Card class.).
- **helper method:** A method, usually private, that is called by another method. Helper methods are used to simplify the calling method. They also facilitate code reuse when they provide a function that can be used by more than one calling method.
- **loop invariant:** A logical statement that is always true when execution reaches a loop's termination test.
- **model:** A class with behaviors and state that represent key features of some "real-world" object or process. We say that a class models the "real-world" object. For example, the Deck class models a real deck of cards.
- **perfect shuffle:** A card-shuffling method that starts with dividing the deck into two stacks, then interleaving the cards, first a card from stack 1, then a card from stack 2, then another card from stack 1, another from stack 2, and so on.
- **permutation:** A rearrangement of a given sequence of values. There are six permutations of the sequence [1,2,3], namely [1,2,3] (the "identity" permutation), [1,3,2], [2,1,3], [2,3,1], [3,1,2], and [3,2,1]. If the given sequence contains duplicate values, so will its permutations. For example, the permutations of [1,1,2] are [1,1,2], [1,2,1], and [2,1,1].
- polymorphism: A process that Java uses where the method to execute is based on the object executing the method. For example, if board.anotherPlayIsPossible() is executed, and board references an ElevensBoard object, then the ElevensBoard anotherPlayIsPossible method will be called.
- **probabilistic:** Based on chance or involving the use of randomness.
- **pseudo-random number generator:** A procedure that produces a sequence of values that passes various statistical tests for randomness (e.g., any value is just as likely to occur in a given position in the sequence as any other).

random number generator: See pseudo-random number generator.

refactor: Reorganizing code. One example of refactoring is creating helper methods to simplify code or eliminate duplicate code. Another is splitting a class into a superclass and a subclass, putting the code that would be common to other subclasses into the new superclass.

selection shuffle: A card-shuffling method that works similarly to the selection sort. It randomly selects a card for each position in the deck from the remaining unselected cards.

shuffle: A method of permuting (mixing up) the cards in a deck. See **perfect shuffle** and **selection shuffle**.

simulation: Imitation, using a computer program, of some real-world process. The "actors" in the process correspond to objects and variables in the simulation, while the interactions between the actors correspond to program methods.

systematic: Performed using a logical step-by-step process.

truncation: Removal of the fractional part of a real or double value, producing an integer.

References

The Complete Book of Solitaire and Patience Games, by Albert H. Morehead and Geoffrey Mott-Smith, Bantam Books (1977).