Scaling of environment interactions with horizon length at fixed performance levels