

Transfer reactions: the DWBA method

A.M.Moro

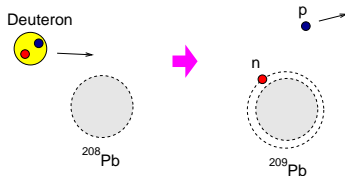


Universidad de Sevilla, Spain

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Material available at: <https://github.com/ammoro/padova>

Outline

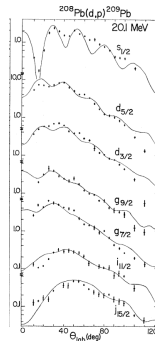
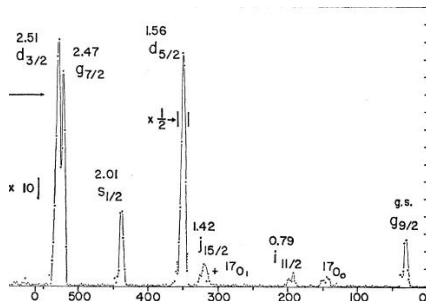


- ## 2 What information can we infer from a transfer reaction?

What do we measure in a transfer reaction?

Example: $d + {}^{208}\text{Pb} \rightarrow p + {}^{209}\text{Pb}$

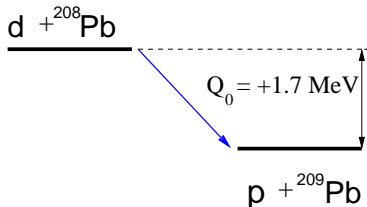
Phys. Rev. 159 (1967) 1039



- The proton energy spectrum shows some peaks which reflect the **energy spectrum** of the residual nucleus (${}^{209}\text{Pb}$).
- Each peak has a characteristic **angular distribution**, which depends on the structure of the associated state.
- The population probability will depend on the **reaction dynamics** and on the **structure** properties of these states.

Transfer reactions: Q -value considerations

Example: $d + {}^{208}\text{Pb} \rightarrow p + {}^{209}\text{Pb}$



$$Q_0 = M_d c^2 + M(^{208}\text{Pb})c^2 - M_p c^2 - M(^{209}\text{Pb})c^2 = +1.7 \text{ MeV}$$

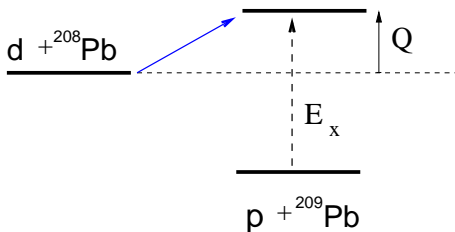
☞ $Q_0 > 0$: the outgoing proton will gain energy with respect to the incident deuteron.

N.b.: For a transfer reaction, the Q value is just the difference in binding energies of the transferred particle/cluster in the initial and final nuclei:

$$Q_0 = \varepsilon_b(f) - \varepsilon_b(i) = 3.936 - 2.224 = +1.7 \text{ MeV}$$

Transfer reactions: Q -value considerations

If the transfer leads to an excited state, the *Q-value* will change accordingly, and hence the kinetic energy of the outgoing nuclei.

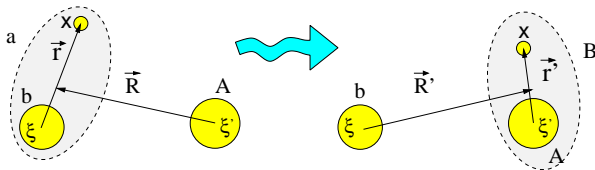


Energy balance:

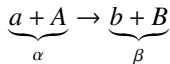
$$E_{\text{cm}}^f = E_{\text{cm}}^i + Q = E_{\text{cm}}^i + Q_0 - E_x$$

👉 If we know Q_0 we can infer the excitation energies (E_x) measuring the final kinetic energy of outgoing fragments.

- Transfer process: $\underbrace{(b+x)}_a + A \rightarrow b + \underbrace{(A+x)}_B$



- Complications arise with respect to inelastic scattering because now we have two different mass partitions involved



Evaluation of scattering amplitude in Born approximation (post form)

- Projectile-target interaction in post representation:

$$V_{\beta}(\mathbf{R}', \mathbf{r}') = V_{xb} + U_{bA} = \underbrace{U_{\beta}(\mathbf{R}')}_{\text{Aux. pot.}} + \underbrace{[V_{xb} + U_{bA} - U_{\beta}(\mathbf{R}')]_{\text{Resid. inter.}}} \equiv U_{\beta}(\mathbf{R}') + \Delta V_{\beta}$$

- In DWBA, the scattering amplitude is $f_{\beta\alpha}(\theta) = -(\mu_{\beta}/2\pi\hbar^2)\mathcal{T}_{\beta,\alpha}$ with

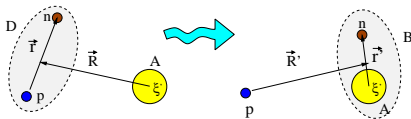
$$\mathcal{T}_{\beta,\alpha}(\theta) = \int \underbrace{\chi_{\beta}^{(-)*}(\mathbf{K}_{\beta}, \mathbf{R}') \Phi_{\beta}^{*}(\xi_{\beta})}_{\text{final state}} \Delta V_{\beta} \underbrace{\chi_{\alpha}^{(+)}(\mathbf{K}_{\alpha}, \mathbf{R}) \Phi_{\alpha}(\xi_{\alpha})}_{\text{initial state}} \underbrace{d\xi_{\beta} d\mathbf{R}'}_{\text{(all coordinates)}}$$

- Initial and final internal states:

$$\text{Initial state: } \Phi_{\alpha}(\xi_{\alpha}) = \varphi_a(\xi, \mathbf{r})\Phi_A(\xi') \quad \xi_{\alpha} \equiv \{\xi, \xi', \mathbf{r}\}$$

$$\text{Final state: } \Phi_{\beta}(\xi_{\beta}) = \varphi_b(\xi)\Phi_B(\xi', \mathbf{r}') \quad \xi_{\beta} \equiv \{\xi, \xi', \mathbf{r}'\}$$

- $\chi_{\alpha,\beta}^{(\pm)}$ are distorted waves for entrance and exit channels, obtained with appropriate optical potentials $U_{\alpha}(\mathbf{R})$, $U_{\beta}(\mathbf{R}')$



- $$\begin{aligned}\Phi_{\alpha}^{(0)}(\xi_{\alpha}) &= \varphi_d(\mathbf{r})\phi_A(\xi') & \xi_{\alpha} &= \{\xi', \mathbf{r}\} \\ \Phi_{\beta}(\xi_{\beta}) &= \Phi_B(\xi', \mathbf{r}') & \xi_{\beta} &= \{\xi', \mathbf{r}'\}\end{aligned}$$

- $$\mathcal{T}_{d,p}^{\text{DWBA}} = \int \int \chi_p^{(-)*}(\mathbf{K}_p, \mathbf{R}') \Phi_B(\xi', \mathbf{r}') (V_{pn} + U_{pA} - U_{pB}) \chi_d^{(+)}(\mathbf{K}_d, \mathbf{R}) \varphi_d(\mathbf{r}) \phi_A(\xi') d\xi_\beta d\mathbf{R}'$$

(d,p) case: parentage decomposition of target nucleus

⇒ We need to evaluate the **overlap integral**

$$\int d\xi' \phi_B^*(\xi', \mathbf{r}') \phi_A(\xi') \equiv \langle \phi_B | \phi_A \rangle$$

⇒ Use the **parentage decomposition** of $B \rightarrow A + n$

$$\Phi_B(\xi', \mathbf{r}') = \mathcal{A}_{BA}^{\ell j} \underbrace{\phi_A(\xi') \varphi_{nA}^{\ell j}(\mathbf{r}')}_{\text{A g.s.}} + \sum_{A' \neq A} \mathcal{A}_{BA'}^{\ell' j'} \phi_{A'}(\xi') \varphi_{nA'}^{\ell' j'}(\mathbf{r}')$$

$$\Rightarrow \langle \phi_B | \phi_A \rangle = \mathcal{A}_{BA}^{\ell j} \varphi_{nA}^{\ell j}(\mathbf{r}')$$

⇒ $\mathcal{A}_{BA}^{\ell j}$ = spectroscopic amplitude

⇒ $|\mathcal{A}_{BA}^{\ell j}|^2 = S_{BA}^{\ell j}$ = spectroscopic factor

⇒ $\varphi_{nA}^{\ell j}(\mathbf{r}')$ = single-particle wavefunction describing motion of n with respect to A .

☞ *The spectroscopic factor quantifies the single-particle content of a given physical state B , when described as $A + n$, with A in some specific state.*

Examples of parentage decomposition

1 Double-magic nucleus plus a single nucleon:

$$|^{209}\text{Bi}(\text{g.s.})\rangle_{9/2^-} \approx \left[|^{208}\text{Pb}(0^+)\rangle \otimes |\pi 1h_{9/2}\rangle \right]_{9/2^-}$$

☞ *almost* single-particle configuration ($S_{IJ}^{\ell sj} \approx 1$).

2 Deformed core plus an extra nucleon:

$$|^{11}\text{Be}(\text{gs})\rangle_{1/2^+} = \alpha \left[|^{10}\text{Be}(0^+)\rangle \otimes |\nu 2s_{1/2}\rangle \right]_{1/2^+} + \beta \left[|^{10}\text{Be}(2^+)\rangle \otimes |\nu 1d_{5/2}\rangle \right]_{1/2^+} + \dots$$

with $|\alpha|^2 + |\beta|^2 + \dots \approx 1$

3 Due to indistinguishability of neutrons (or protons) the SF can be even larger than 1!

Scattering amplitude and cross sections

⇒ In post form:

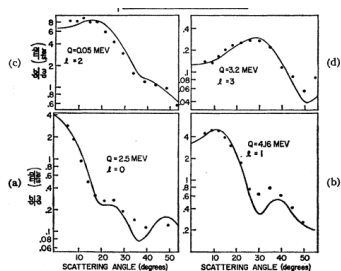
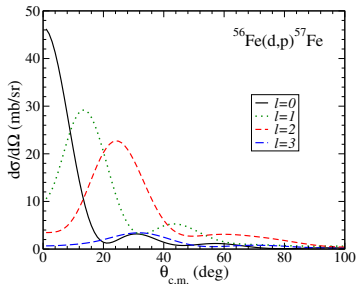
$$\mathcal{T}_{d,p}^{\text{DWBA}} = \mathcal{A}_{BA}^{\ell j} \int \int \chi_p^{(-)*}(\mathbf{K}_p, \mathbf{R}') \varphi_{nA}^{\ell j,*}(\mathbf{r}') V_{pn}(\mathbf{r}) \chi_d^{(+)}(\mathbf{K}_d, \mathbf{R}) \varphi_d(\mathbf{r}) d\mathbf{r}' d\mathbf{R}'$$

$$\left(\frac{d\sigma}{d\Omega} \right)_{(d,p)} = \frac{\mu_\alpha \mu_\beta}{(2\pi\hbar^2)^2} S_{BA}^{\ell j} \left| \int \int \chi_p^{(-)*}(\mathbf{K}_p, \mathbf{R}') \varphi_{nA}^{\ell j,*}(\mathbf{r}') V_{pn}(\mathbf{r}) \chi_d^{(+)}(\mathbf{K}_d, \mathbf{R}) \varphi_d(\mathbf{r}) d\mathbf{r}' d\mathbf{R}' \right|^2$$

$$|\mathcal{A}_{BA}^{\ell j}|^2 = S_{BA}^{\ell j} = \text{spectroscopic factor}$$

📖 In DWBA, the transfer cross section is proportional to the product of the projectile and target spectroscopic factors. Comparing the data with DWBA calculations, one can extract the values of $S_{BA}^{\ell j}$

Orbital angular momentum sensitivity



Angular distributions of transfer cross sections are very sensitive to the single-particle configuration of the transferred nucleon/s. $\Rightarrow \varphi_{nlj}(\mathbf{r})$

From classical arguments, the angle of the first maximum appears at:

$$\theta_{\max} \approx \arcsin \left(\frac{\sqrt{\ell(\ell+1)}\hbar}{pR} \right)$$

1. *Journal of Management Studies*, 1996, 33, 1, 1-14.

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- A vector diagram illustrating the relationship between the incident wave vector \vec{K}_i , the reflected wave vector \vec{K}_f , and the scattering vector \vec{q} . The vector \vec{K}_i is horizontal, \vec{K}_f is at an angle θ to \vec{K}_i , and \vec{q} is the resultant vector from the tip of \vec{K}_i to the tip of \vec{K}_f .

- $$|(\mathbf{P}_i - \mathbf{P}_f) \times \mathbf{R}| = |\mathbf{q}\hbar \times \mathbf{R}| \simeq \ell\hbar$$

Summary: What do we learn from a transfer experiment

1 Excitation energies of residual nucleus

⇒ *The Q -value is related to the masses and excitation energies*

2 Spectroscopic factors (related to occupation numbers)

⇒ In DWBA, $\sigma^{\ell j I} \propto S_{BA}^{\ell j I}$

3 Angular momentum of populated states.

⇒ For heavy targets, the first maximum occurs at:

$$\theta_{\max} \approx \arcsin \left(\frac{\sqrt{\ell(\ell+1)}\hbar}{pR} \right)$$

${}^1\text{H}({}^{11}\text{Be}, {}^{10}\text{Be}){}^2\text{H}$ example

$$|{}^{11}\text{Be}\rangle = \alpha |{}^{10}\text{Be}(0^+) \otimes \nu 2s_{1/2}\rangle + \beta |{}^{10}\text{Be}(2^+) \otimes \nu 1d_{5/2}\rangle + \dots$$

⇒ In DWBA:

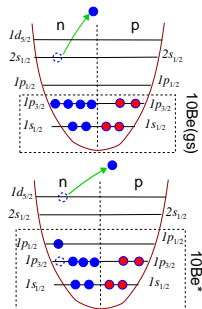
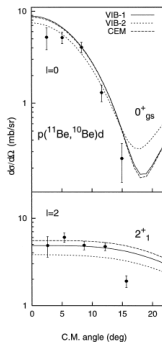
$$\sigma(0^+) \propto |\alpha|^2; \quad \sigma(2^+) \propto |\beta|^2$$

$$|^{11}\text{Be}\rangle = \alpha |^{10}\text{Be}(0^+) \otimes \nu 2s_{1/2}\rangle + \beta |^{10}\text{Be}(2^+) \otimes \nu 1d_{5/2}\rangle + \dots$$
$$\sigma(0^+) \propto |\alpha|^2; \quad \sigma(2^+) \propto |\beta|^2$$

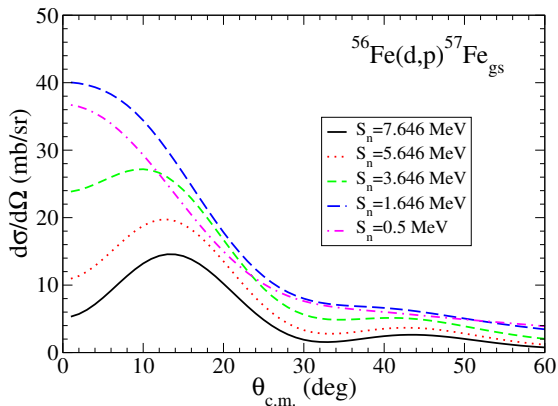
Figure 1 consists of two stacked histograms. The x-axis for both is 'focal plane position (channel)' ranging from 100 to 250. The y-axis for both is 'number of counts'.

The top histogram is labeled 'singles'. It shows a broad peak around 120 channels labeled '6 MeV' with a maximum count of approximately 250. A smaller peak around 160 channels is labeled '3.4 MeV' with a maximum count of approximately 150. To the right of the 3.4 MeV peak, there are two distinct peaks labeled 'GS' (Ground State) and 'C*' (Coulomb excitation) with a maximum count of approximately 100. The label $^1\text{H}(^{11}\text{Be}, ^{10}\text{Be})^2\text{H}$ and $\theta(^{10}\text{Be}) < 1.2^\circ$ are present in the upper right.

The bottom histogram is labeled '(coinc. with ^2H)'. It shows a broad peak around 120 channels labeled '6 MeV' with a maximum count of approximately 60. A smaller peak around 160 channels is labeled '3.4 MeV' with a maximum count of approximately 20. To the right of the 3.4 MeV peak, there are two distinct peaks labeled 'GS' (Ground State) and '0+' (0+ state) with a maximum count of approximately 10.



Dependence with binding energy:



Peripherality of transfer reactions: the ANC

- Recall the overlap function: $\langle \phi_B | \phi_A \rangle = \mathcal{A}_{BA}^{\ell j} \varphi_{nA}^{\ell j}(\mathbf{r}')$
- Outside the range of the nuclear potential:

$$\varphi_{nA}^{\ell j}(\mathbf{r}') \rightarrow b_{\ell j} \frac{W_{-\eta, \ell+1/2}(2kr)}{r} \approx b_{\ell j} e^{-kr} \quad k = \sqrt{2\mu\epsilon_b}/\hbar$$

where $b_{\ell j}$ is the **single-particle asymptotic normalization coefficient**.

- Then, outside the range of the nuclear potential:

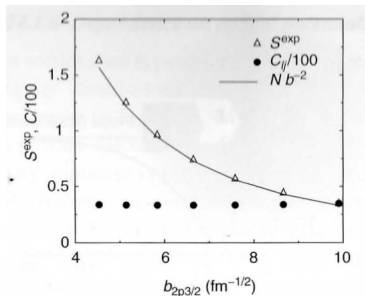
$$\langle \phi_B | \phi_A \rangle = \mathcal{A}_{BA}^{\ell j} b_{\ell j} \frac{W_{-\eta, \ell+1/2}(2kr)}{r} \equiv C_{BA}^{\ell j} \frac{W_{-\eta, \ell+1/2}(2kr)}{r}$$

where $C_{BA}^{\ell j} = \mathcal{A}_{BA}^{\ell j} b_{\ell j}$ is the **asymptotic normalization coefficient** of the $\langle \phi_B | \phi_A \rangle$ overlap.

☞ Thus, outside the range of the nuclear potential, the overlap function is sensitive to the ANC $C_{BA}^{\ell j}$ rather than to the spectroscopic amplitude $\mathcal{A}_{BA}^{\ell j}$

Peripherality of transfer reactions: the ANC

- For a peripheral transfer reaction, $d\sigma/d\Omega \propto |C_{BA}^{\ell j}|^2$.
- In DWBA, the ratio of the experimental and calculated cross sections will provide the quantity $|C_{BA}^{\ell j}|^2$.
- Since $|C_{BA}^{\ell j}|^2 = S_{BA}^{\ell j} b_{\ell j}^2$, varying the parameters of the single-particle potential used to generate $\varphi_{nA}^{\ell j}(\mathbf{r}')$, will modify $b_{\ell j}$ and also $S_{BA}^{\ell j}$ but their product ($|C_{BA}^{\ell j}|^2$) will remain roughly constant.

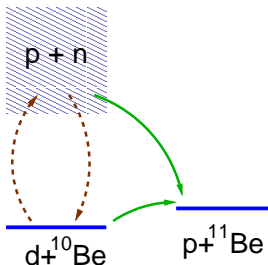


Quoted from Fig. 14.4 of Thompson and Nunes book

Transfer reactions with weakly bound nuclei

Transfer reactions with weakly bound nuclei

- DWBA approximates the total WF by the elastic channel and assumes that the transfer occurs in one step (Born approximation).
- For weakly bound projectiles (eg. deuterons), breakup is an important channel and can influence the transfer process.



- $\Psi_{\mathbf{K}_d}^{(+)}(\mathbf{R}, \mathbf{r})$ includes breakup components, but these are lost when we make the DWBA approximation ($\Psi^{(+)} \approx \chi_d^{(+)}(\mathbf{K}_d, \mathbf{R})\varphi_d(\mathbf{r}) \Rightarrow$ need to go beyond DWBA

Adiabatic distorted wave approximation (ADWA)

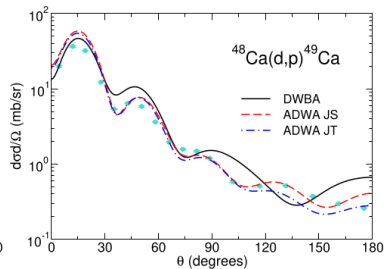
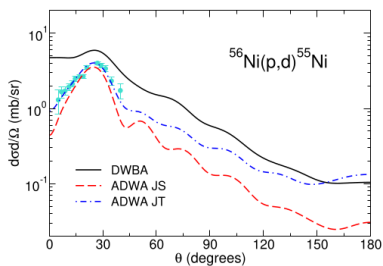
- $\chi_d^{(+)}(\mathbf{K}_d, \mathbf{R})$ describes deuteron elastic scattering but, for the (d, p) transfer matrix element, we need only $\Psi_{\mathbf{K}_d}^{(+)}(\mathbf{R}, \mathbf{r})$ for small $|\mathbf{r}|$
- R.C. Johnson and col. have derived an approximation of $\Psi_{\mathbf{K}_d}^{(+)}(\mathbf{R}, \mathbf{r})$ valid for $r \approx 0$, which includes the effect of deuteron breakup effectively (**adiabatic approx.**):
 - 1 **Zero-range** approximation (Johnson-Soper): [(Johnson, Soper, PRC1, 976 (1970))]

$$U^{JS}(R) = U_{pA}(R) + U_{nA}(R) \quad \Rightarrow \chi_d^{JS}(\mathbf{R})$$

- 2 **Finite-range** version (Johnson-Tandy): [Johnson & Tandy, NPA235 (1974) 56]

$$U^{JT}(R) = \frac{\langle \varphi_{pn}(\mathbf{r}) | V_{pn}(U_{nA} + U_{pA}) | \varphi_{pn}(\mathbf{r}) \rangle}{\langle \phi_{pn}(\mathbf{r}) | V_{pn} | \phi_{pn}(\mathbf{r}) \rangle}$$

DWBA vs ADWA



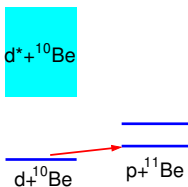
From Timofeyuk and Johnson, Progress in Particle and Nuclear Physics 111 (2020) 103738

- Use CDCC approximation for $\Psi_{\mathbf{K}_\alpha}^{(+)}$.

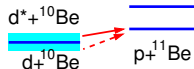
$$\Psi_{\mathbf{K}_\alpha}^{(+)} \approx \Psi^{\text{CDCC}} = \underbrace{\chi_0(\mathbf{R})\phi_0(\mathbf{r})}_{\text{elastic}} + \sum_{n',j,\pi} \underbrace{\phi_{n'}^{j\pi}(k_{n'}, \mathbf{r})\chi_{n',j,\pi}(\mathbf{R})}_{\text{breakup}}$$

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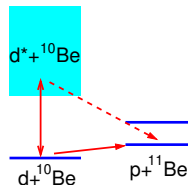
DWBA, ADWA and CDCC-BA compared



DWBA



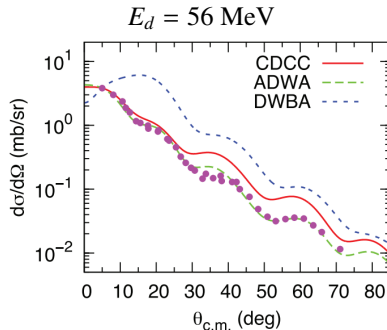
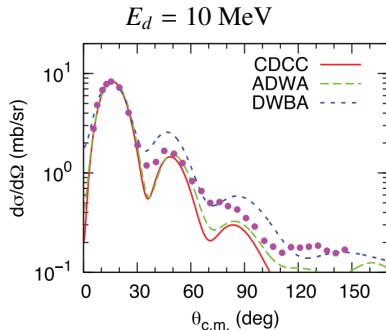
ADWA



CDCC-BA

Gómez-Camacho and A.M.M., *A Pedestrian Approach to the Theory of Transfer Reactions: Application to Weakly-Bound and Unbound Exotic Nuclei*, Lecture Notes in Physics, vol 879.

DWBA vs ADWA vs CDCC

Example: $^{58}\text{Ni}(d,p)^{59}\text{Ni}$ 

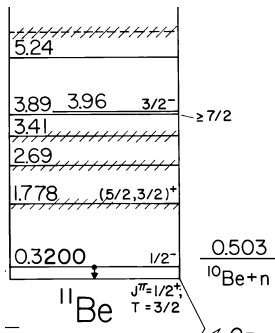
☞ *CDCC and ADWA provide better description of the data and lead also to more realistic spectroscopic information (e.g. spectroscopic factors)*

Pang *et al*, PRC 90, 044611 (2014)

Transfer reactions populating unbound states: resonances

Continuum resonances

The continuum spectrum is not “homogeneous”; it contains in general energy regions with special structures, such as resonances and virtual states

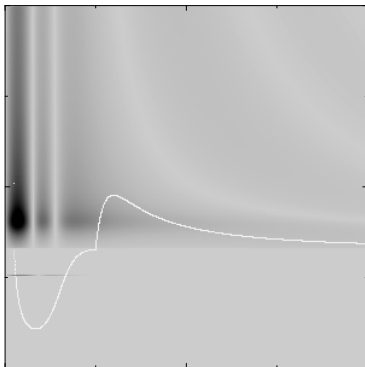


What is a resonance?

- It is a **pole** of the S-matrix in the complex energy plane.
- It is a structure on the continuum which may, or may not, produce a **maximum in the cross section**, depending on the reaction mechanism and the phase space available.
- The resonance occurs in the range of energies for which the **phase shift is close to $\pi/2$** .
- In this range of energies, continuum wavefunctions have a **large probability of being in the radial range of the potential**.
- The continuum wavefunctions are **not square normalizable**. For practical applications, a normalized wavepacket (or “bin”) can be constructed to represent the resonance.

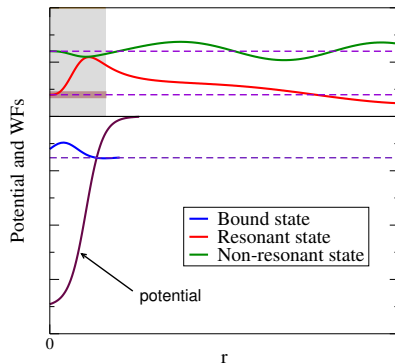
Distinctive features of a resonance

In the energy range of the resonance, the continuum wavefunctions have a large probability of being within the range of the potential.



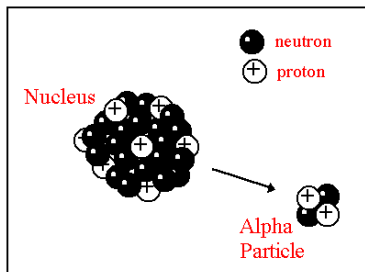
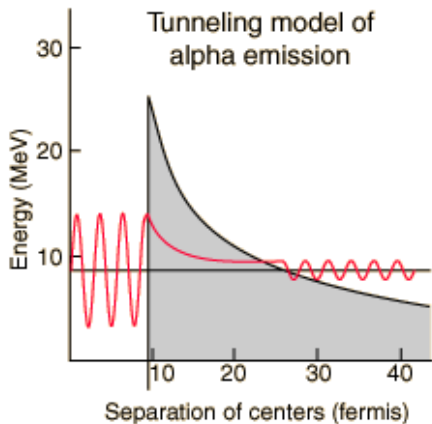
Cuts and areas ordered by size

(Courtesy of C. Dasso)

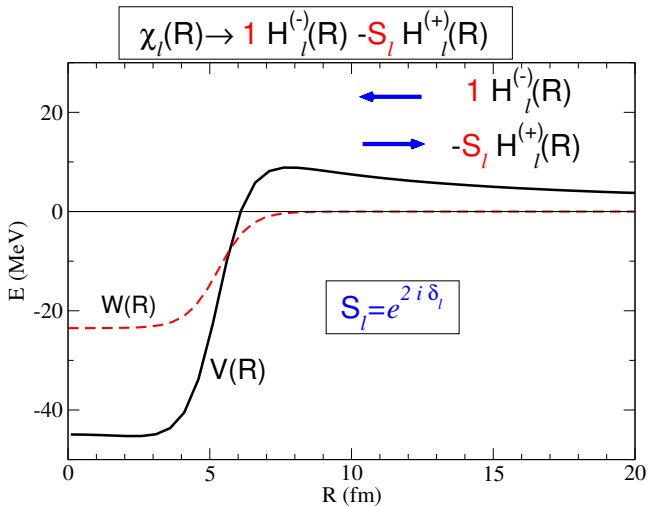


Distinctive features of a resonance

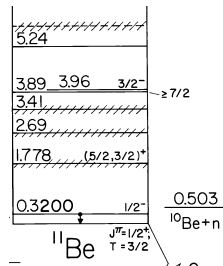
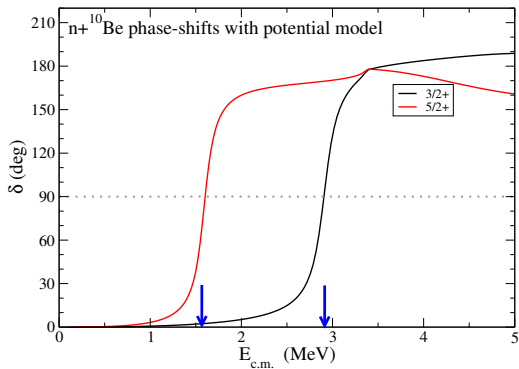
The decay of the resonance is also behind the α -decay phenomenon:



Resonances and phase-shifts

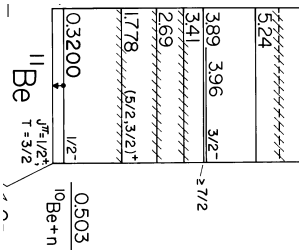
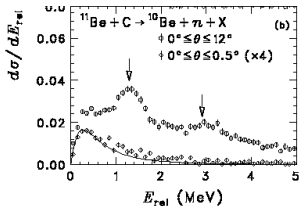


Resonances and phase-shifts

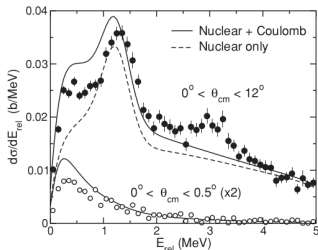
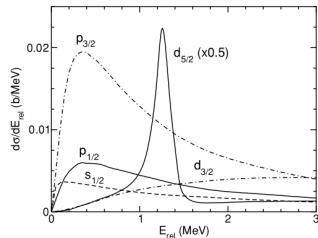


Studying resonances in nuclear breakup experiments

RIKEN data



CDCC analysis



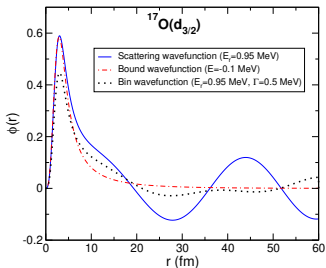
Fukuda *et al.*, PRC70 (2004) 054606

Howell *et al.*, JPG31 (2005) S1881

Exploring resonances from transfer reactions

- Calculation of transfer to unbound states in DWBA and ADWA poses numerical problems due to the oscillatory behaviour of unbound wavefunctions.
- A regularization method must be applied:
 - Representing the resonance by a weakly bound state with the same quantum numbers
 - Vincent & Fortune contour integration in the complex radius plane (PRC2 (1970) 782)
 - Representing the resonance by a continuum *bin*

E.g.: $d_{3/2}$ resonance in ^{17}O resonance at $E_r = 0.95$ MeV



Exploring resonances from transfer reactions

- Inclusion of continuum states in DWBA poses numerical problems due to the oscillatory behaviour of unbound wavefunctions
- Regularization method must be applied, such as representing the resonance by a wavepacket (continuum *bin*, as in the CDCC method)

E.g.: ^{11}Be resonance at $E_x = 1.78 \text{ MeV}$ from $^{10}\text{Be}(d,p)^{11}\text{Be}$

Schmitt et al, PRC88, 064612 (2013)

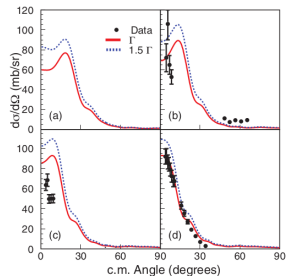
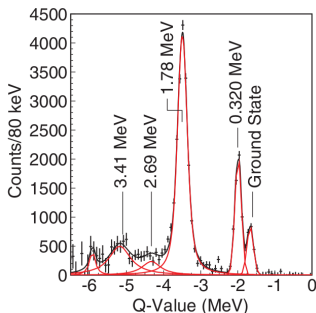
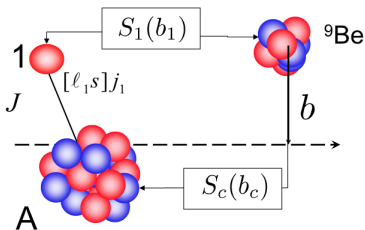


FIG. 8. (Color online) Differential cross sections are presented for transfer to the first resonance in ^{11}Be at 1.78 MeV via the $^{10}\text{Be}(d,p)$ reaction in inverse kinematics at deuteron energies of (a) 12 MeV, (b) 15 MeV, (c) 18 MeV, and (d) 21.4 MeV. The curves are from FR-ADWA calculations using (solid line) an energy bin that is the same width as for the resonance used in the calculation and (dotted line) with a width 1.5 times that value. At 12 MeV the protons were too low in energy to extract an angular distribution.

Knock-out reactions

Spectroscopic from momentum distributions

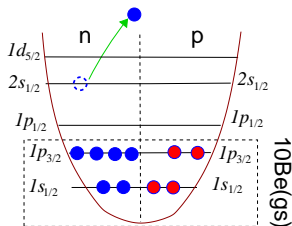
- Fast-moving projectile on a (typically) light target.
- One nucleon suddenly removed (absorbed) due to its interaction with the target.
- The remaining residue remains unchanged and is detected.
- The momentum of the core is related to that of the removed nucleon because, in the rest frame of the projectile, $\vec{P} = 0$



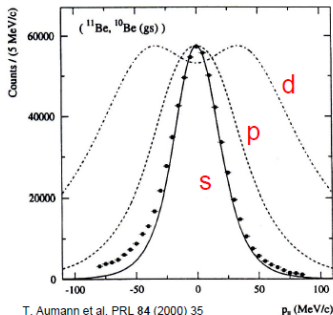
$$\vec{P} = \vec{p}_c + \vec{p}_1 = 0$$

Angular momentum sensitivity of momentum distributions

- The shape is determined by the orbital angular momentum ℓ .
- The magnitude is determined by the amount of $s_{1/2}$ (spectroscopic factor)

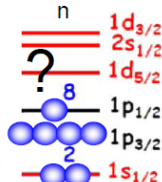


Residue momentum $^{11}\text{Be} \rightarrow ^{10}\text{Be}$ – halo case



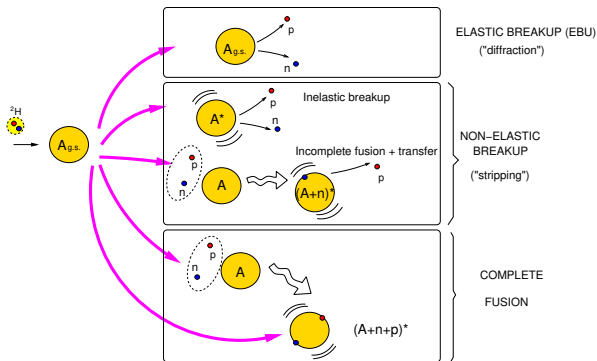
T. Aumann et al. PRL 84 (2000) 35

$Z = 4, N = 7$



^{11}Be

Stripping and diffraction contributions to inclusive breakup cross sections



☞ *The singles (inclusive) cross section of a given fragment will contain in general diffraction and stripping components*

Stripping cross section within a semiclassical (eikonal) theory

At high energies, one can use the sudden, eikonal approximations to obtain simple formulas for the stripping and diffraction parts of the inclusive breakup cross section for a inclusive reaction of the form $a + B \rightarrow b + X$, with $a = b + x$:

Stripping:

$$\sigma_{\text{sp}}^{\text{str}} = 2\pi \int b db \int d\mathbf{r} |\varphi_{bx}(\mathbf{r})|^2 (1 - |S_x(b_x)|)^2 |S_{bA}(b_b)|^2$$

Diffraction:

$$\sigma_{\text{sp}}^{\text{diff}} = 2\pi \int b db \left[\langle \varphi_{bx} | |S_b S_x|^2 | \varphi_{bx} \rangle - |\langle \varphi_{bx} | S_b S_x | \varphi_{bx} \rangle|^2 \right].$$

- $|S_b(b_b)|^2$ = probability of survival of the core.
- $1 - |S_x(b_x)|^2$ = probability of absorption of the valence particle.

Extraction of SFs from knockout reactions

- Agreement theory vs experiment quantified with the **reduction factor**:

$$R_s = \frac{\sigma_{\text{theor}}}{\sigma_{\text{exp}}}$$

with

$$\sigma_{\text{theor}} = \sum_{n\ell j} S_{bx}^a(I; n\ell j) \sigma_{\text{sp}}(I; n\ell j)$$

$$\sigma_{\text{sp}}(I; n\ell j) = \sigma_{\text{sp}}^{\text{EBU}} + \sigma_{\text{sp}}^{\text{NEB}}$$

- $R_s < 1 \Rightarrow$ possible correlations (long-range, short-range, tensor, ...) not included in σ_{theor} ?
- R_s strongly dependent on $\Delta S = S_p - S_n$.

Extraction of SFs from knockout reactions

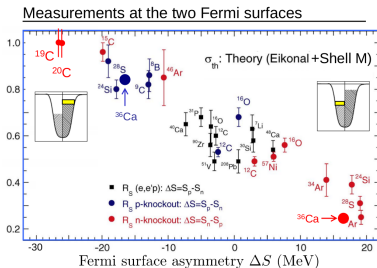
- Agreement theory vs experiment quantified with the **reduction factor**:

$$R_s = \frac{\sigma_{\text{theor}}}{\sigma_{\text{exp}}}$$

with

$$\sigma_{\text{theor}} = \sum_{nlj} S_{bx}^a(I; nlj) \sigma_{\text{sp}}(I; nlj)$$

$$\sigma_{\text{sp}}(I; nlj) = \sigma_{\text{sp}}^{\text{EBU}} + \sigma_{\text{sp}}^{\text{NEB}}$$



-Gade et al, PRC 77, 044306 (2008)
Tostevin, PRC90,057602(2014)

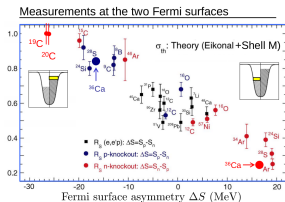
- $R_s < 1 \Rightarrow$ possible correlations (long-range, short-range, tensor, ...) not included in σ_{theor} ?
- R_s strongly dependent on $\Delta S = S_p - S_n$.

Extraction of SFs from knockout reactions

...however, this behaviour has not been corroborated by other probes, such as transfer or proton-induced knockout reactions (p, pN)

HI knockout (~ 100 MeV/u)

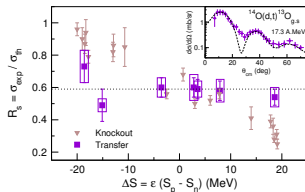
Tostevin, PRC90,057602(2014)



- Reaction model: eikonal + adiabatic
- R_s strongly dependent on $S_p - S_n$.

Low-energy transfer

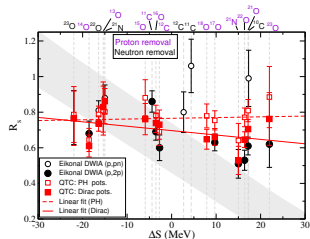
Flavigny, PRL110, 122503(2013)



- Reaction model: ADWA, DWBA, CRC
- $R_s \sim \text{constant}$.

 (p, pN) @ 200-400 MeV/u

Aumann, PPNP118,103847(2021)



- Reaction models: DWIA, TC
- $R_s \sim \text{constant}$.

Similar results from RIKEN
Wakase, PTEP 021D01 (2018)

R_s from knockout disagree with those from transfer and $(p, pN) \Rightarrow$ description of reaction mechanism?