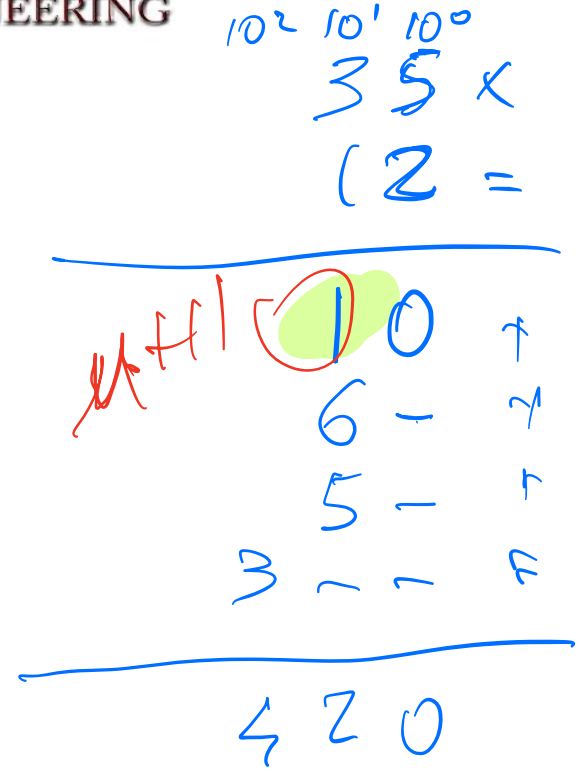
EE382A – Spring 2025

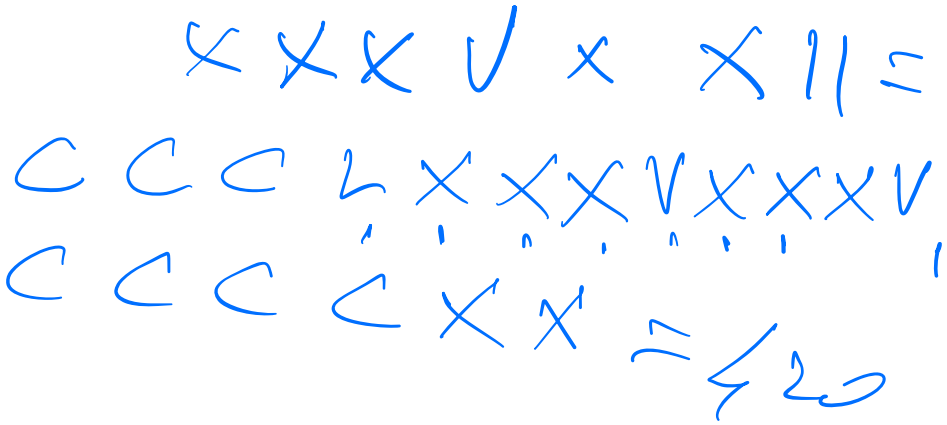
Chapter 7: Kestrel's Instruction Set Architecture (4 of 5)

Kestrel's ISA, fourth part

- Single-precision multiplication
- Multi-precision multiplication
- Optional programming assignment: fixed-point multiplication
- Bit-shifting
- Deeply nested conditionals

How does multiplication work?





AL-QUARITHMI

LIBER ABACI

G.B. FIBONACCI

0 1 2 3 5 8

Single-precision multiplication

MULT Returns low byte of product of two unsigned bytes

```
mult    Rdest, OpA, OpB
```

MULTSA Returns low byte of product of a signed byte (first operand, OpA) and an unsigned byte (second operand, OpB)

```
multsa  Rdest, OpA, OpB
```

MULTSB Returns low byte of product of an unsigned byte (first operand, OpA) and a signed byte (second operand, OpB)

```
multsb  Rdest, OpA, OpB
```

MULTSAB Returns low byte of product of a signed byte (first operand, OpA) and a signed byte (second operand, OpB)

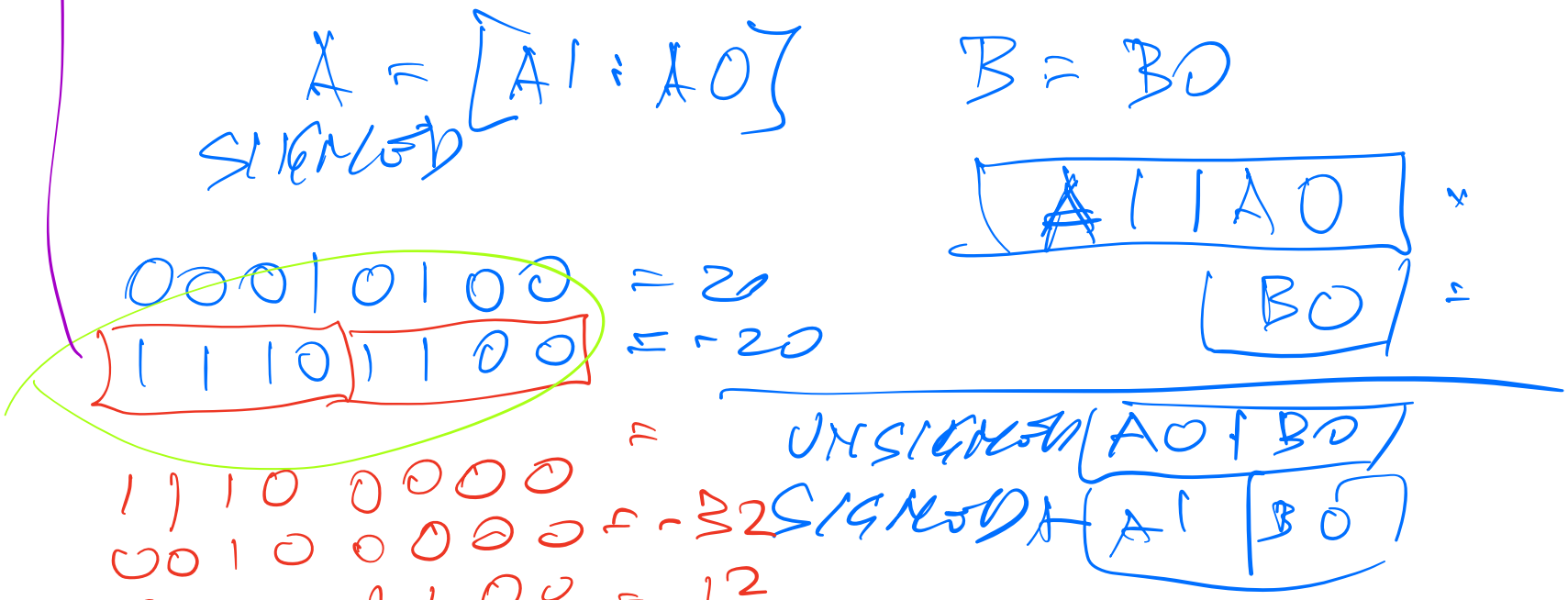
```
multsab  Rdest, OpA, OpB
```

The **MHI** register contains the product's high byte.

Single-precision multiplication (cont.)

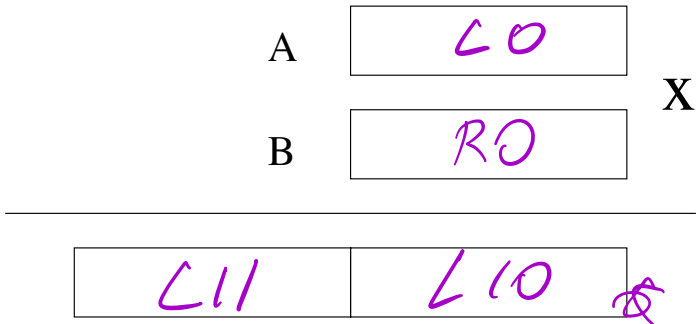
NOTE: the signed operations are only performed when they involve the most-significant byte (MSB) of a signed operand, NOT on all the bytes of a signed operand!

SMHI is the sign extension of the multiplier high byte, **`mhi`**



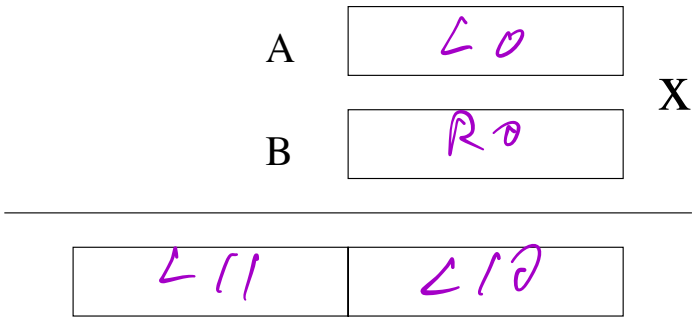
Single-precision multiplication: examples

Example 1: both operands unsigned




```
mult    f10, f0, f0
move    f11, multi
```

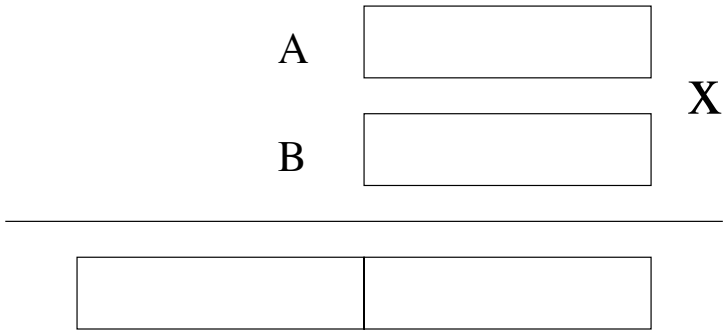
Example 2: A signed, B unsigned

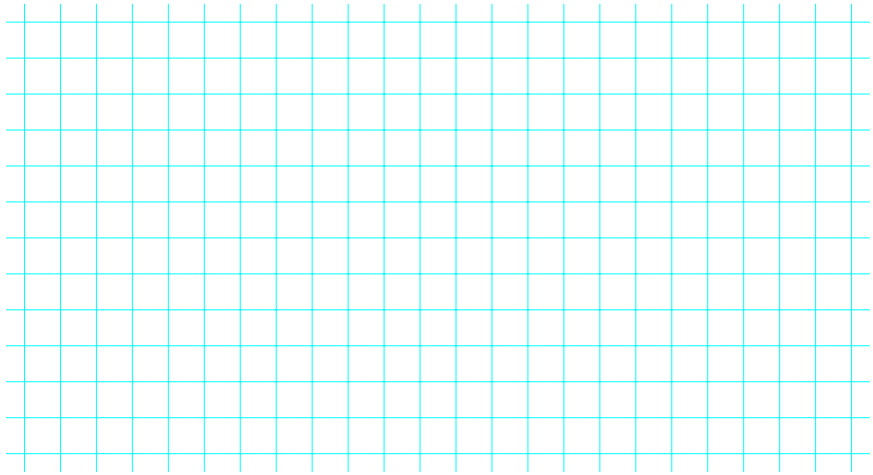



```
multsd  f10, f0, f0
move    f11, multi
```

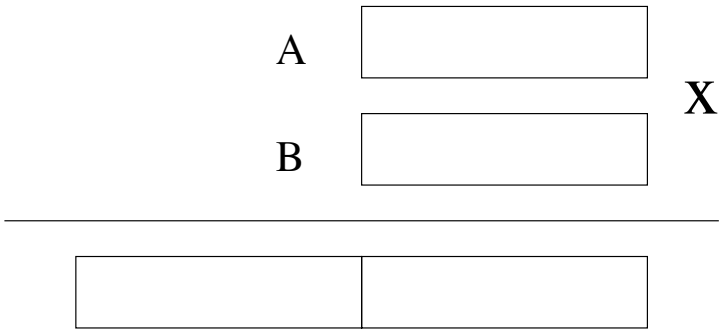
Single-precision multiplication: more examples

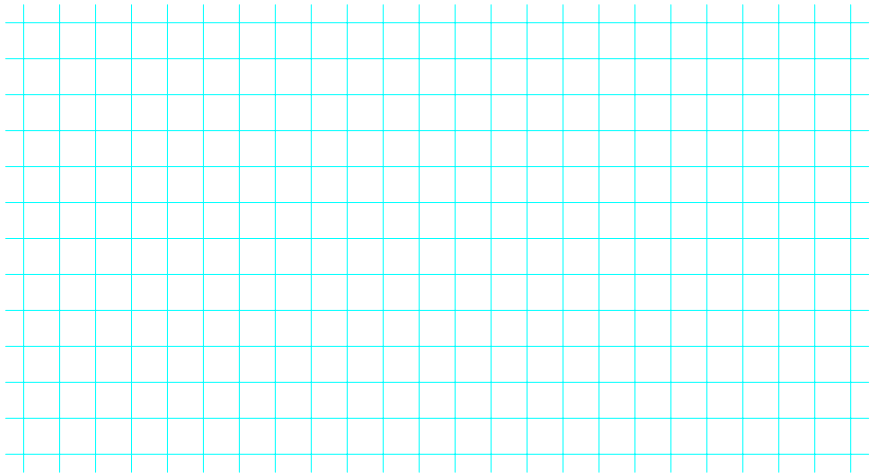
Example 3: A unsigned, B signed





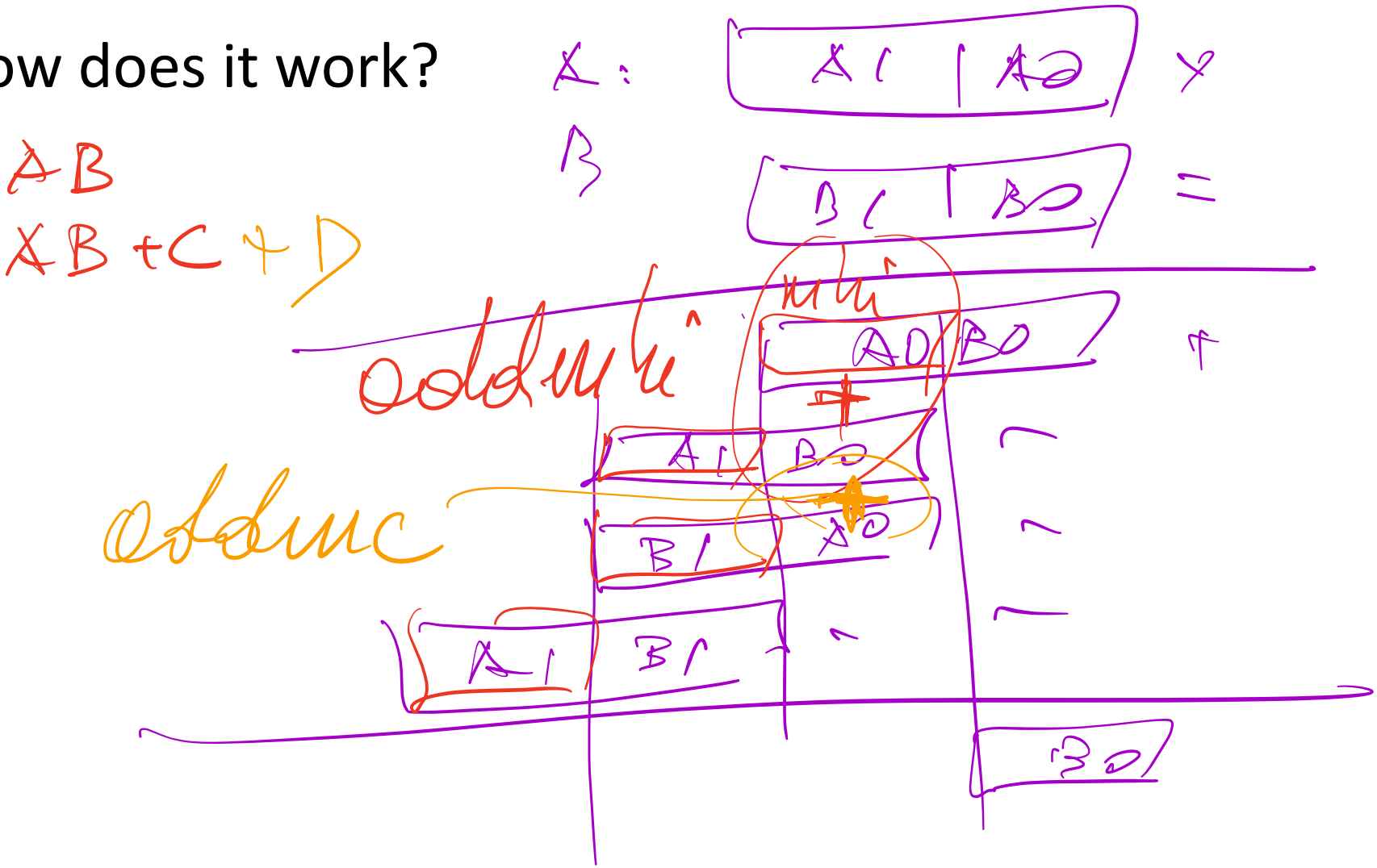
Example 4: both A and B signed





Multi-precision multiplication

- How does it work?



Multi-precision multiplication

With MULT-type instructions, use the modifiers

ADDMC to add the unsigned OpC to the product

```
addmc   OpC
```

ADDMHI to add unsigned register **`mhi`** to the product

```
addmhi
```

Note that they can both be used in the same instruction.

Multiply-accumulate: operands

Kestrel can perform a fused multiply-add in one clock cycle, using the instruction:

```
addmc   OpC
```

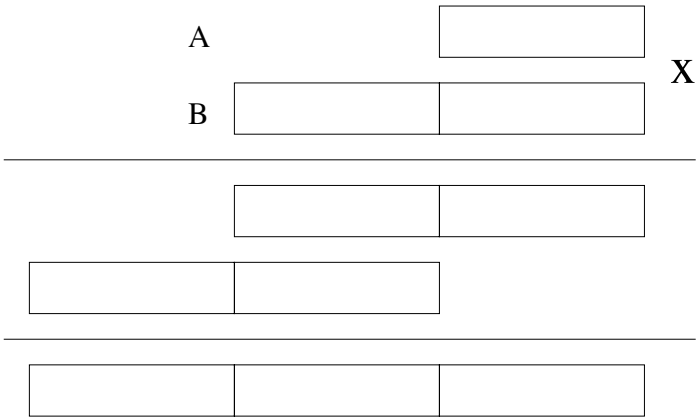
The accumulator for the addition must be a register, so the second source operand (OpB) cannot come from the SSR. The strategy is to read the multiplier from memory. Example:

```
mult  L10, L0, mdr, addmc L20
```

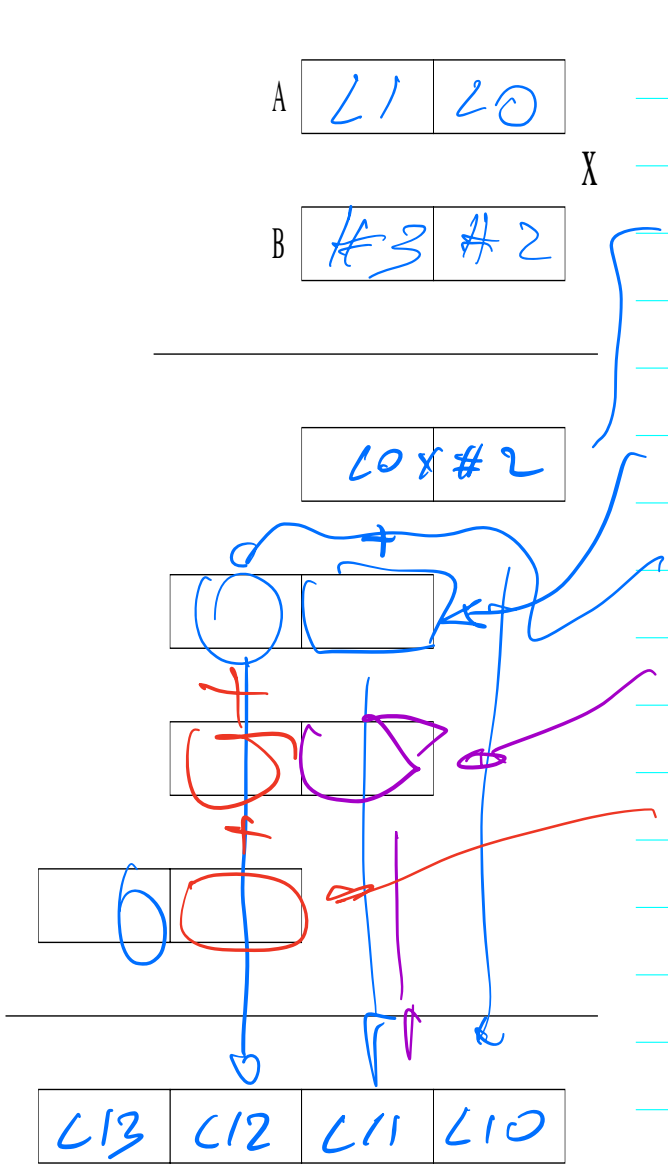
multiplies register **L0** by the **mdr**, adds register **L20** to the product, and stores the sum into register **L10**.

Multi-precision multiplication examples

Both operands unsigned



Multi-precision multiplication: unsigned




```
read #3
mulf      L10, L0, mdr
multaddhi L11, L1, mdr
move      L12, mhi, read(#3)
multu     L11, L0, mdr addu L11
multaddhi L12, L1, mdr, addc L12
move      L13, mhi
```

Multiply-accumulate

Note that neither **`addmc`** nor **`addmhi`** set or use the **`mp`** flag:

- the **`mp`** flag is local to the ALU;
- such a flag is not needed in the multiplier. Why?

$$A \cdot B + C + D \leq (2^8 - 1)(2^8 - 1) + 2^8 - 1 + 2^8 - 1$$

$$= 2^{16} - 2^8 - 2^8 + 1 + 2^8 - 1 + 2^8 - 1 =$$

$$= 2^{16} - 1 = 65535$$

Multiplication's actual operands

When we write, for example:

```
mult  L10, L0, mdr, addmc L20
```

register **L0** is OpA and the **mdr** is OpB.

However, it would be the same even if we swapped them, as in:

```
mult  L10, mdr, L0, addmc L20
```

since the **mdr** can only be OpB the assembler swaps them automatically. In this case it would not make any difference, but it would with signed multiplication. In this instruction:

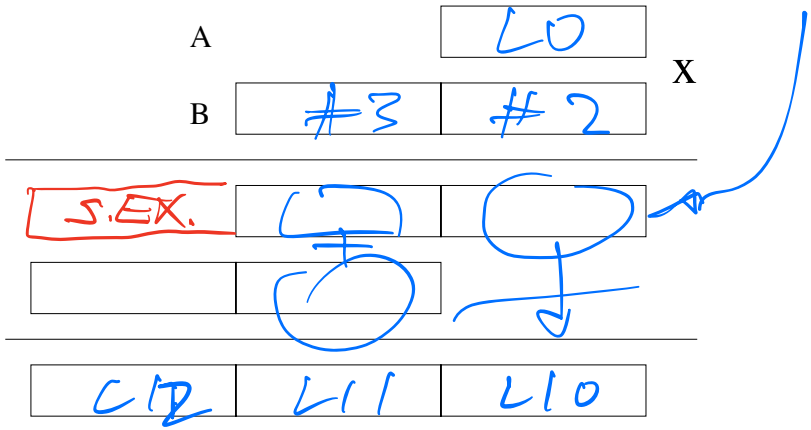
```
multsb  L4, mdr, L10, addmc L20
```

it is **L10** that is considered signed, not the **mdr.**

Always write the operands as OpA, OpB to avoid confusion!

Signed Multi-precision multiplication

A signed, B unsigned




```
read (#2)
multsa      L10, L0, mdh
more        L12, sumhi, read(#3)
multsa      L11, L0, mdh
add         L12, L12, mlo
```

Use the signed operations only on the MSB of each signed operand.

When using signed operations, sign-extend the partial product.

Signed multiplication: sign extensions

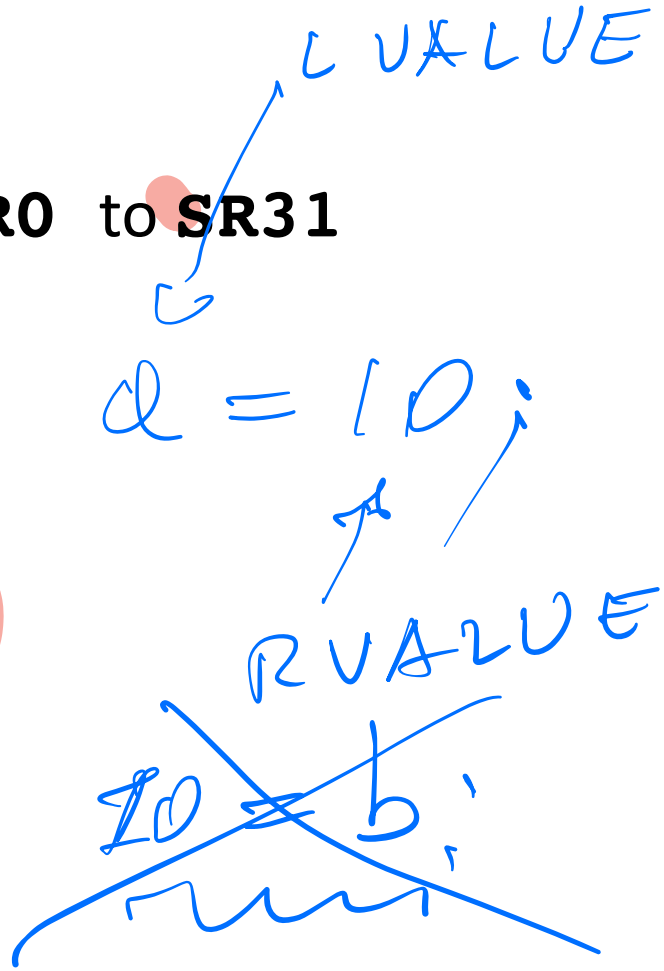
In most cases (excluding some operand conflicts) the sign extensions of all registers is available by just **pre-pending the letter `S` to the register name.**

SSR registers: **`SL0`** to **`SL31`**, and **`SR0`** to **`SR31`**

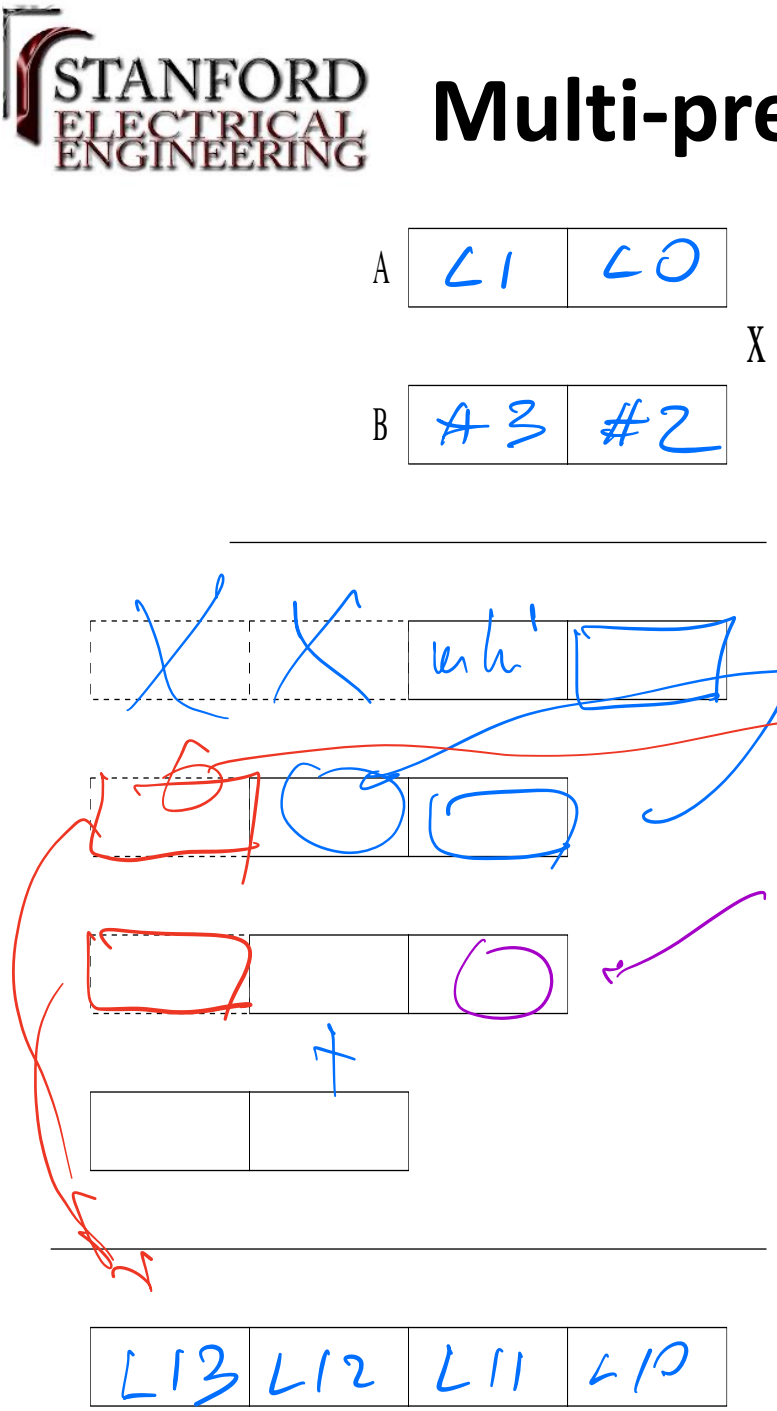
MHI register: **`smhi`**

MDR register: **`smdr`**

The sign extensions are *rvalues* only.



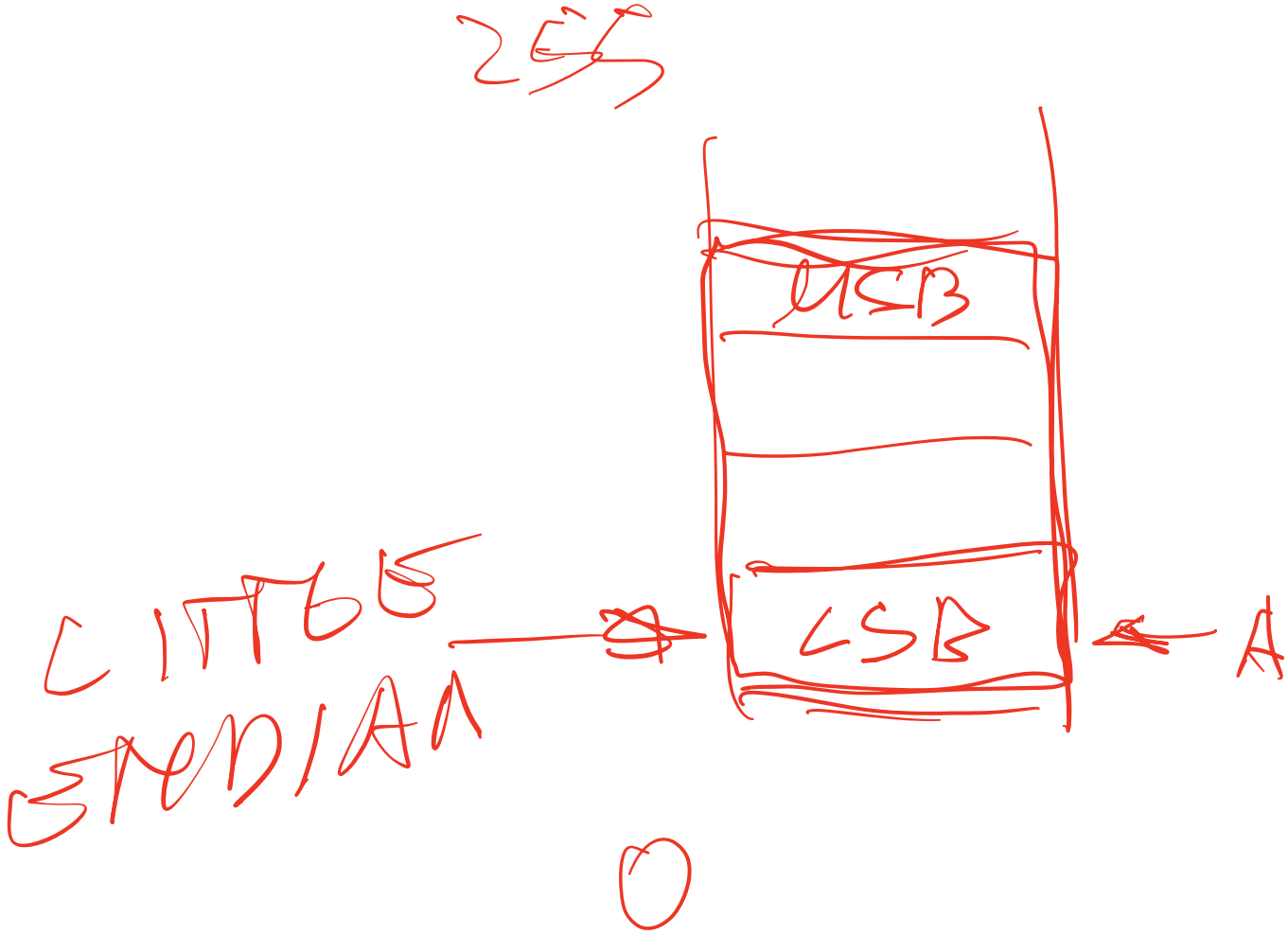
Multi-precision multiplication: signed




```
read (#2)
mult      L10, L0, mdr
multsa    oddmdr L11, L1, mdr , read (#3)
move      L12, mdr
move      L13, smdr
mults6    L11, L0, mdr, oddmac L11
add       L13, L13, smdr
multsab   oddmdr L12, L1, mdr, oddmac L12
add       L13, L13, mdr
```

Signed multi-precision multiplication

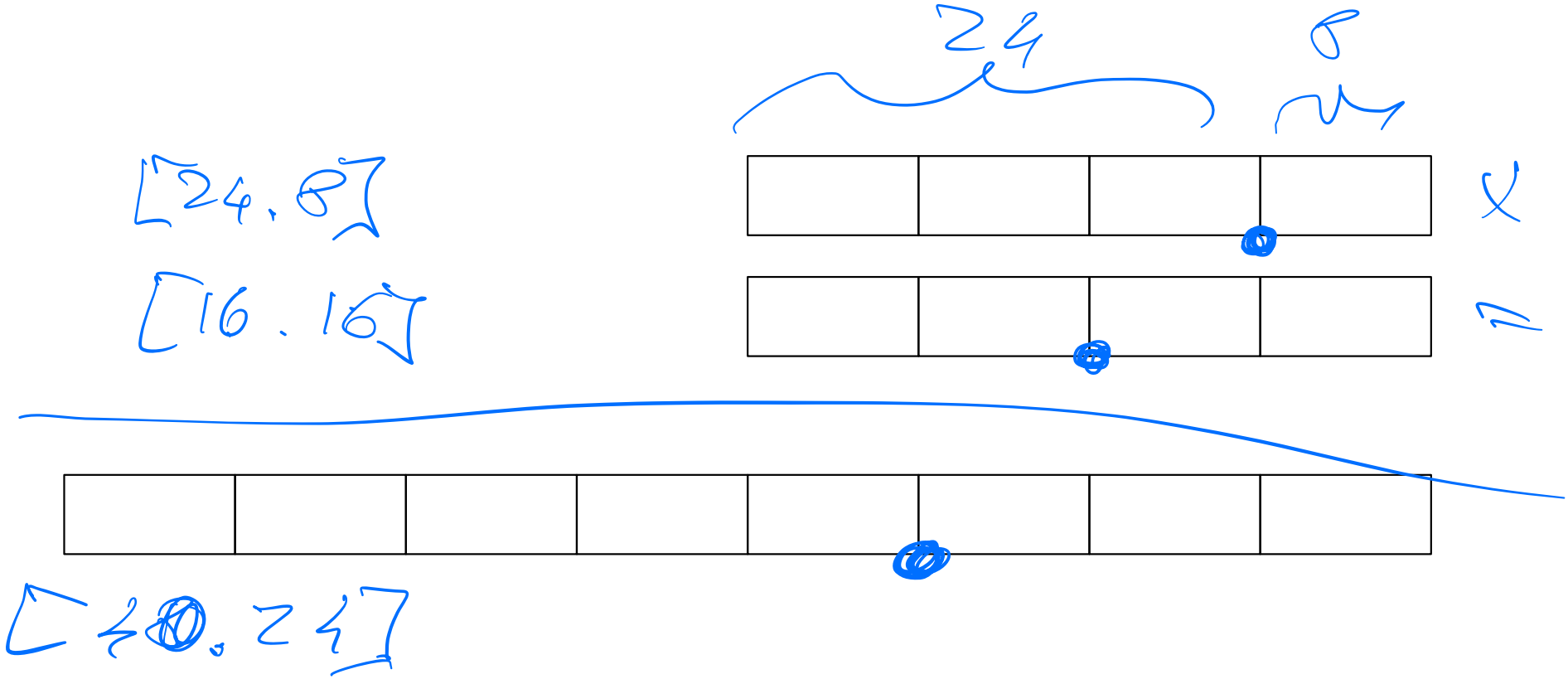
Why use the signed operations only on the MSB of each operand?



Fixed-point representation

Used extensively in image processing and in machine learning.

Also used in our last SIMD assignment, Mandelbrot, like this:

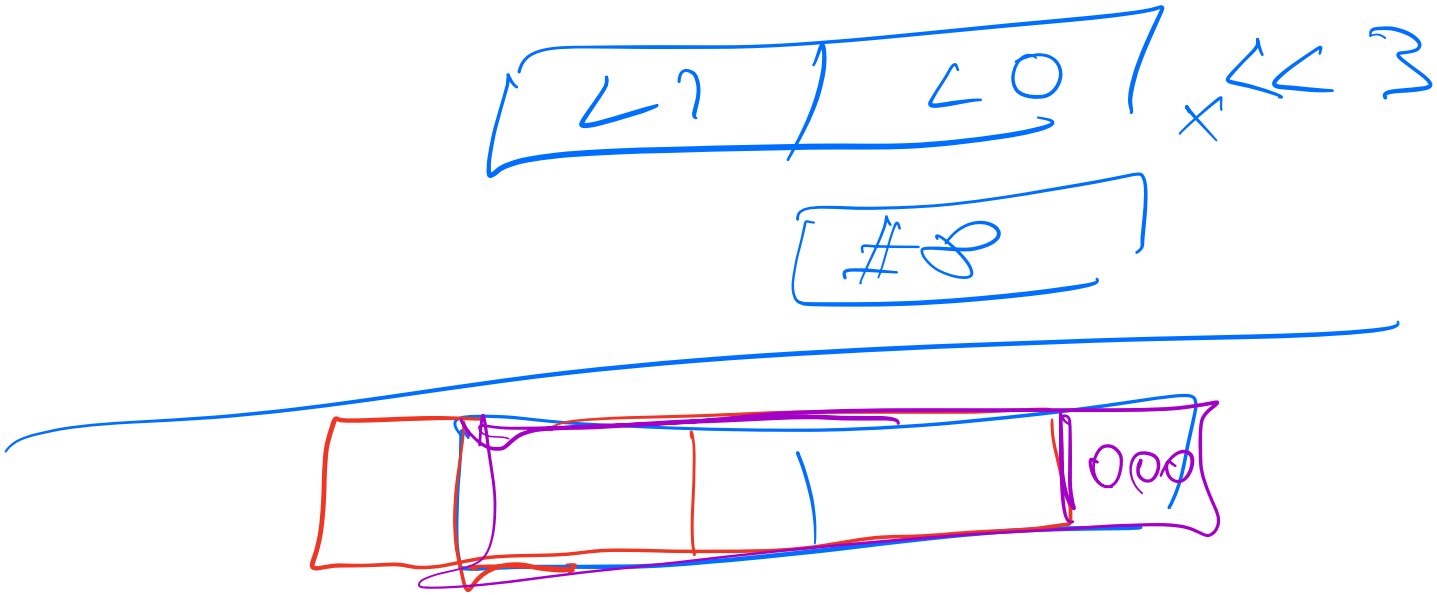


Optional programming assignment: fixed-point multiplication

Multiply two 2-byte numbers that represent fixed-point values in the format 4.12 (4-bit integer part and 12-bit fractional part), and produce a product *in the same format*, on two bytes.

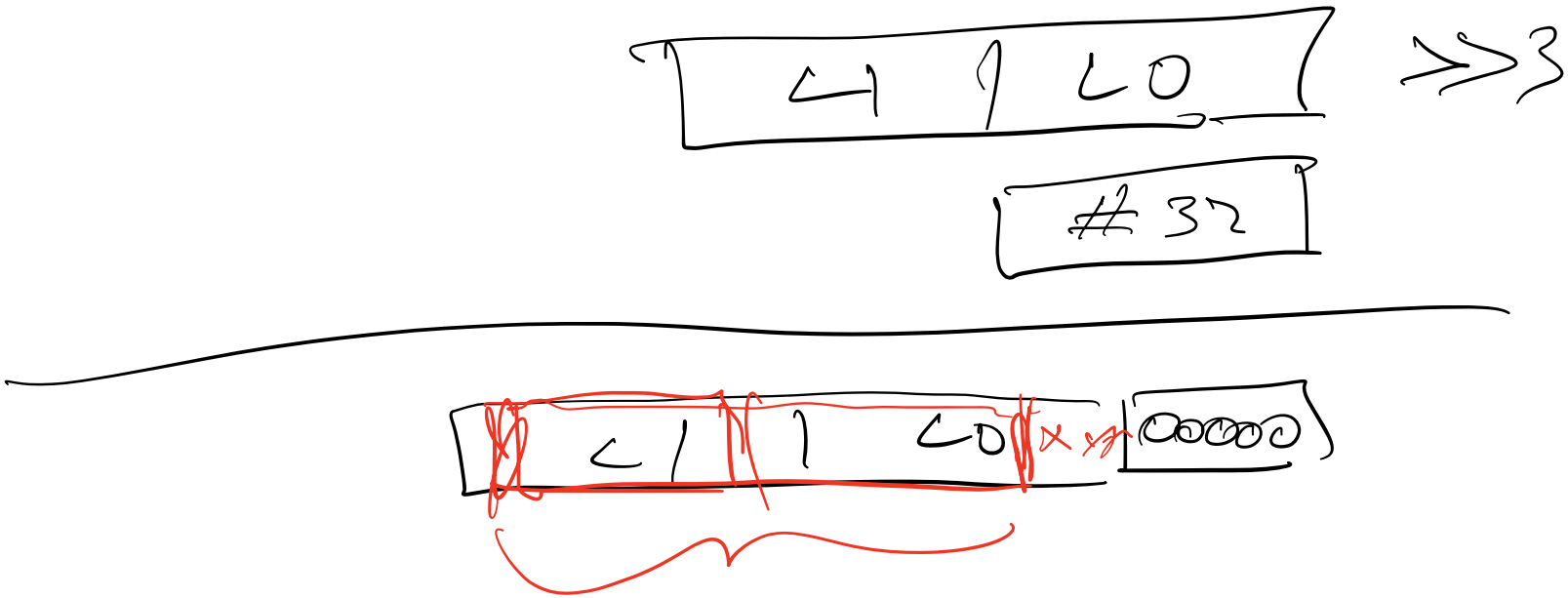
Actual shift operations in Kestrel (1/2)

In Kestrel, shifting is done with the multiplier, NOT with the bit-shifter. Example of **left shift**: [L1:L0] << 3



Actual shift operations in Kestrel (2/2)

Example of **right shift**: [L1:L0] >> 3.



How to differentiate between logic and arithmetic right shift?

Deeply nested conditionals

The bit shifter can't control nested conditionals deeper than 8 levels, so:

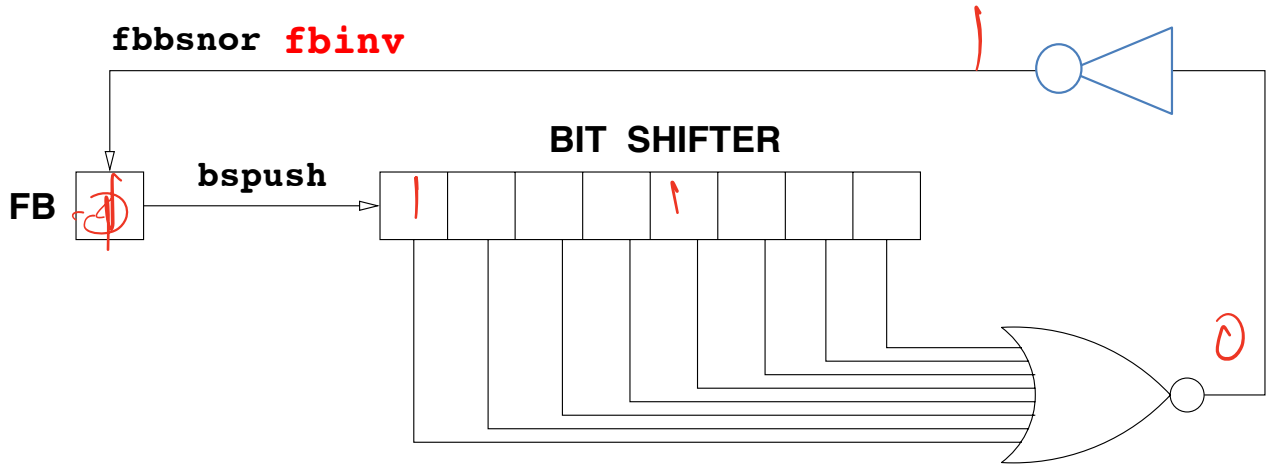
1) Save the bit shifter in a register or in memory

```
move  L29, bs
```

2) Push onto the bit shifter a bit to summarize the on/off state of the PE with **`fbbsnor fbinv`**, which writes the flag bus with the OR of all bits in the bit shifter.

```
fbbsnor fbinv bspush
```

Note that there is no need to clear the bit shifter before pushing it.



Deeply nested conditionals (cont.)

3) Restore the bit shifter when returning:

```
move   L29, L29 bslatch
```

that executes in all PEs regardless of the mask, and sets the mask.

NOTE that:

```
move   L29, L29, bscondlatch
```

only executes in active PEs and does *not* set the mask, therefore do not use it for conditional stack execution. We'll see its use later.