

A large, faint, circular watermark of the Stanford University seal is centered in the background. The seal features a redwood tree in the center, surrounded by the text "STANFORD JUNIOR UNIVERSITY" at the top and "DIE LUFT DER FREIHEIT WEHT" at the bottom. The year "1891" is at the very bottom. The seal is bordered by a diamond pattern.

**EE382A – Spring 2025**

**Chapter 7:  
Kestrel's Instruction Set  
Architecture (4 of 5)**

# Kestrel's ISA, fourth part

- Single-precision multiplication
- Multi-precision multiplication
- Optional programming assignment: fixed-point multiplication
- Bit-shifting
- Deeply nested conditionals



# How does multiplication work?



# Single-precision multiplication

**MULT** Returns low byte of product of two unsigned bytes

**mult Rdest, OpA, OpB**

**MULTSA** Returns low byte of product of a signed byte (first operand, OpA) and an unsigned byte (second operand, OpB)

**multsa Rdest, OpA, OpB**

**MULTSB** Returns low byte of product of an unsigned byte (first operand, OpA) and a signed byte (second operand, OpB)

**multsb Rdest, OpA, OpB**

**MULTSAB** Returns low byte of product of a signed byte (first operand, OpA) and a signed byte (second operand, OpB)

**multsab Rdest, OpA, OpB**

The **MHI** register contains the product's high byte.

# Single-precision multiplication (cont.)

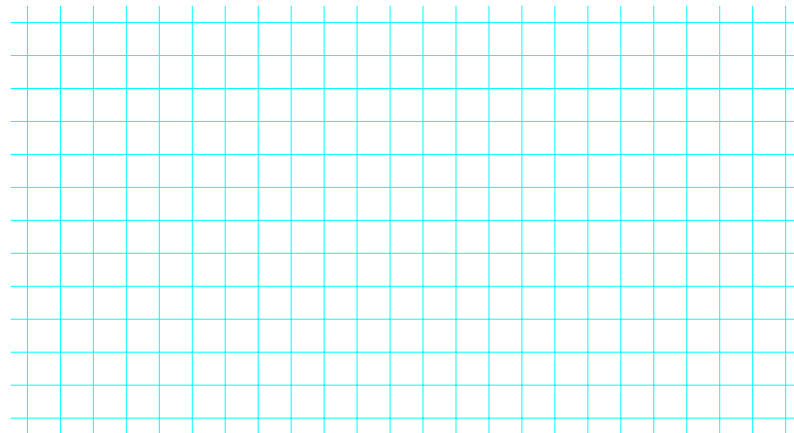
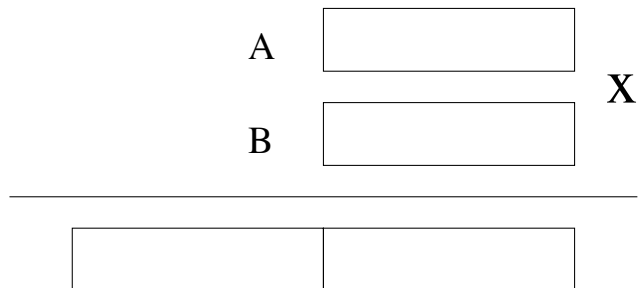
**NOTE:** the signed operations are only performed when they involve the most-significant byte (MSB) of a signed operand, NOT on all the bytes of a signed operand!

**SMHI** is the sign extension of the multiplier high byte, **mhi**

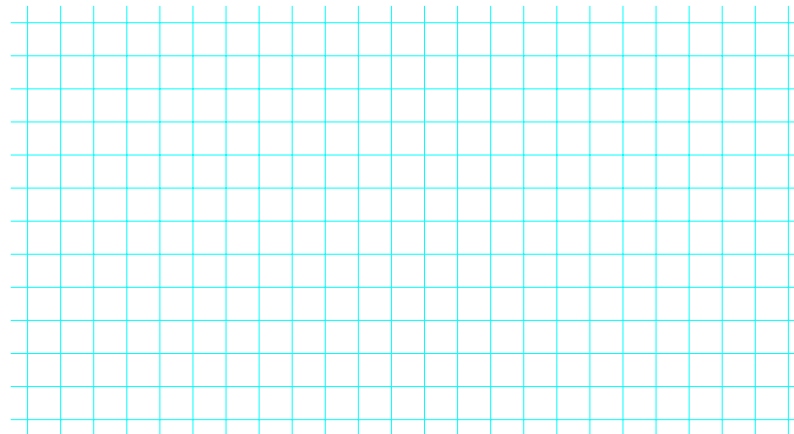
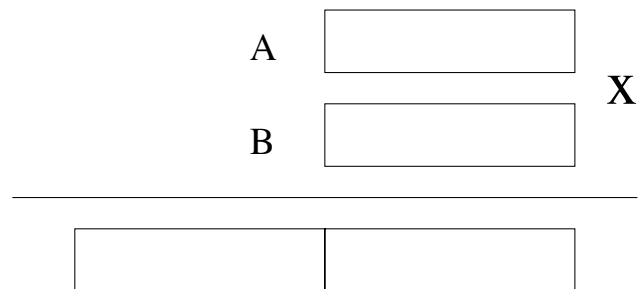


# Single-precision multiplication: examples

Example 1: both operands unsigned

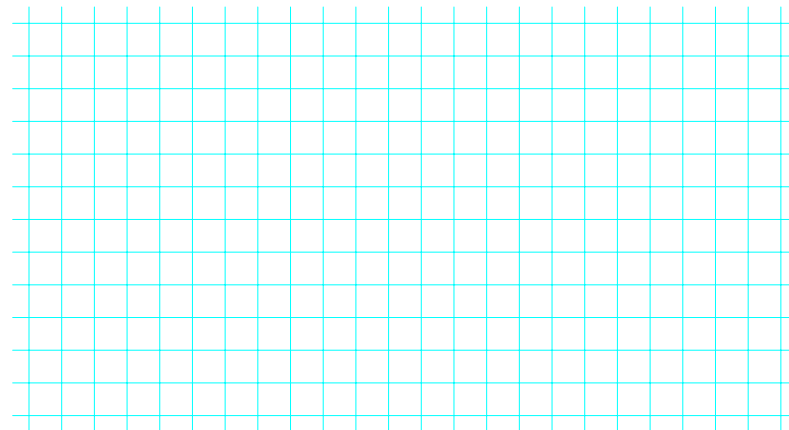
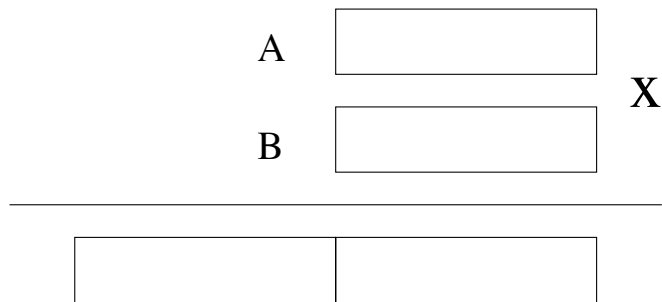


Example 2: A signed, B unsigned

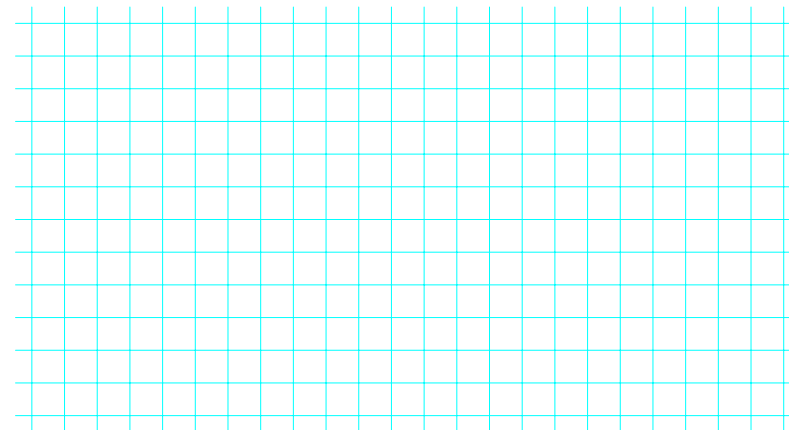
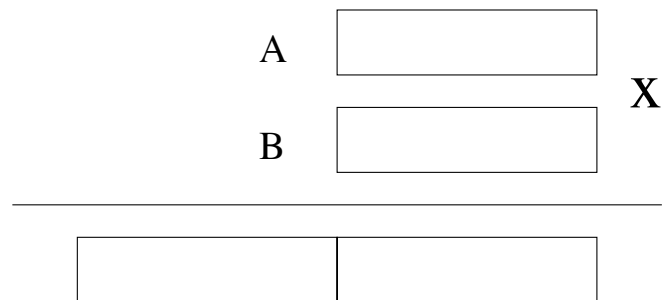


# Single-precision multiplication: more examples

Example 3: A unsigned, B signed



Example 4: both A and B signed



# Multi-precision multiplication

- How does it work?





# Multi-precision multiplication

With MULT-type instructions, use the modifiers

**ADDMC**            to add the unsigned OpC to the product

**addmc    OpC**

**ADDMHI**            to add unsigned register **mhi** to the product

**addmhi**

Note that they can both be used in the same instruction.

## Multiply-accumulate: operands

Kestrel can perform a fused multiply-add in one clock cycle, using the instruction:

**addmc OpC**

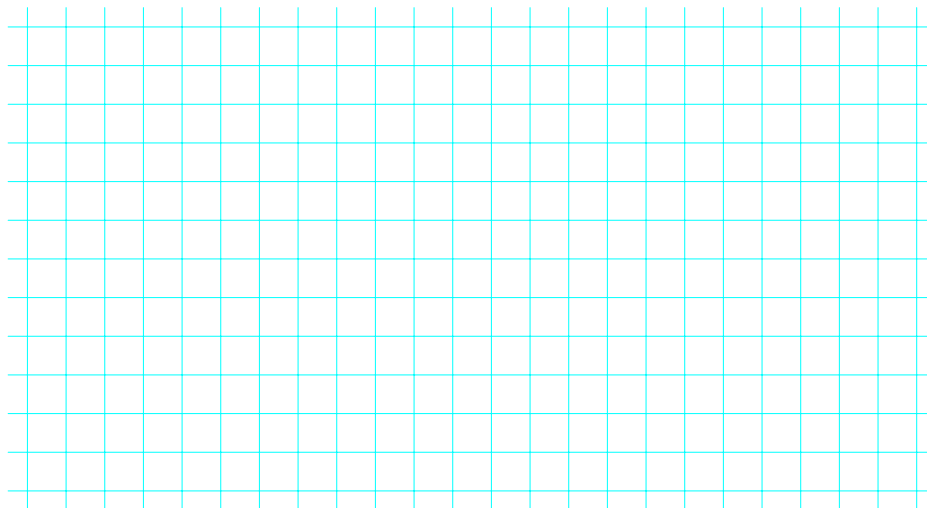
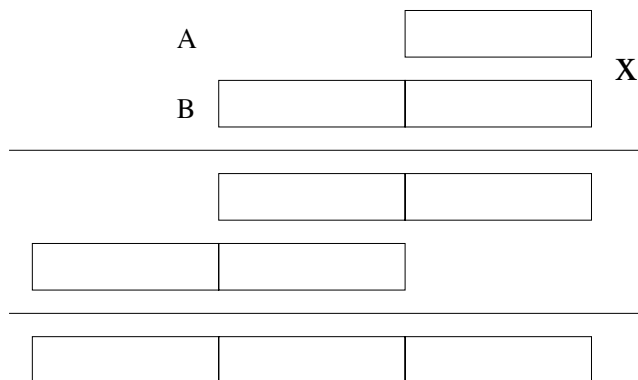
The accumulator for the addition must be a register, so the second source operand (OpB) cannot come from the SSR. The strategy is to read the multiplier from memory. Example:

**mult L10, L0, mdr, addmc L20**

multiplies register **L0** by the **mdr**, adds register **L20** to the product, and stores the sum into register **L10**.

# Multi-precision multiplication examples

Both operands unsigned



# Multi-precision multiplication: unsigned

A 

--	--

X

B 

--	--

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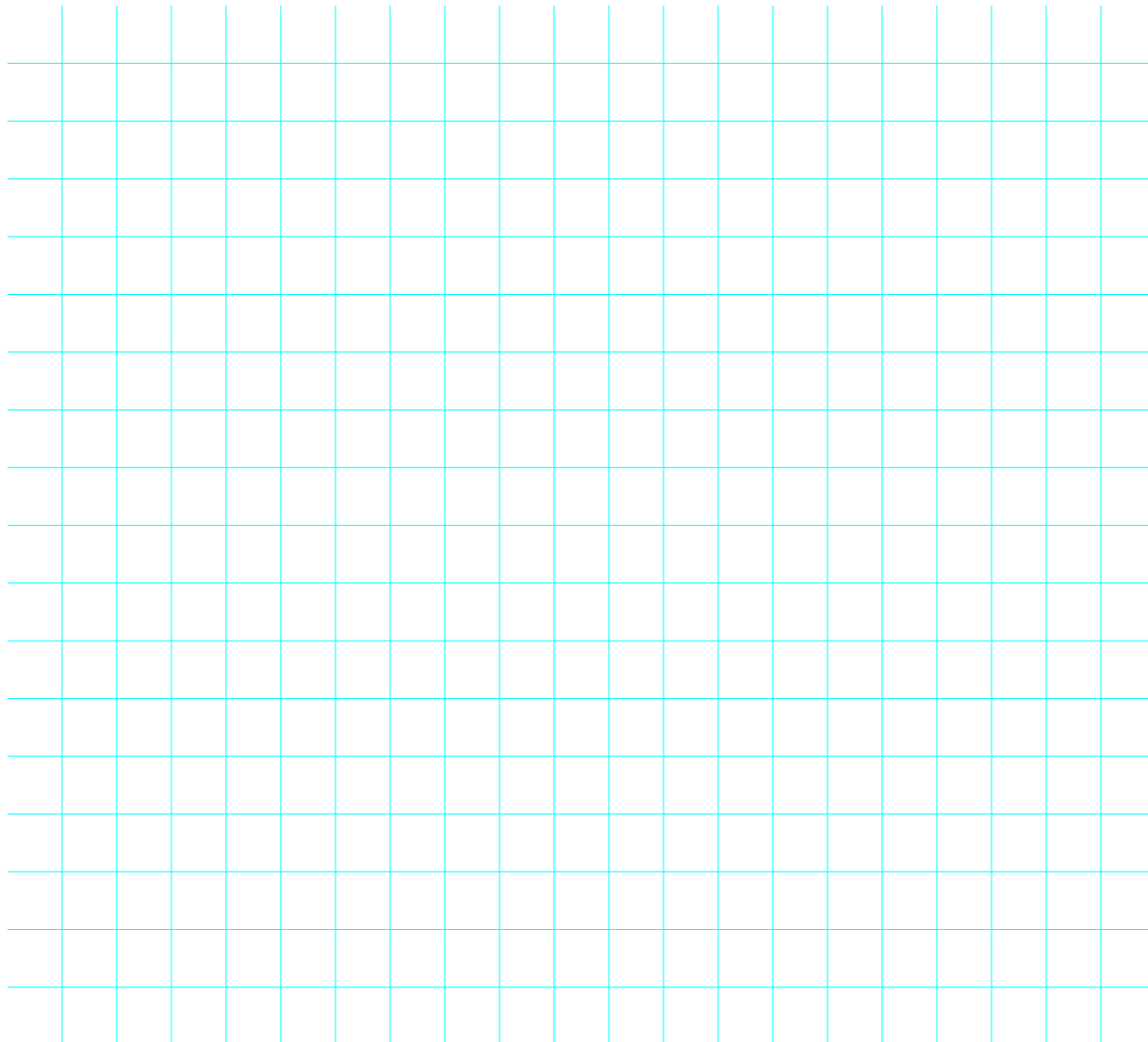
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# Multiply-accumulate

Note that neither **addmc** nor **addmhi** set or use the **mp** flag:

- the **mp** flag is local to the ALU;
- such a flag is not needed in the multiplier. Why?



# Multiplication's actual operands

When we write, for example:

```
mult    L10, L0, mdr, addmc L20
```

register **L0** is OpA and the **mdr** is OpB.

However, it would be the same even if we swapped them, as in:

```
mult    L10, mdr, L0, addmc L20
```

since the **mdr** can only be OpB the assembler swaps them automatically. In this case it would not make any difference, but it would with signed multiplication. In this instruction:

```
multsb  L4, mdr, L10, addmc L20
```

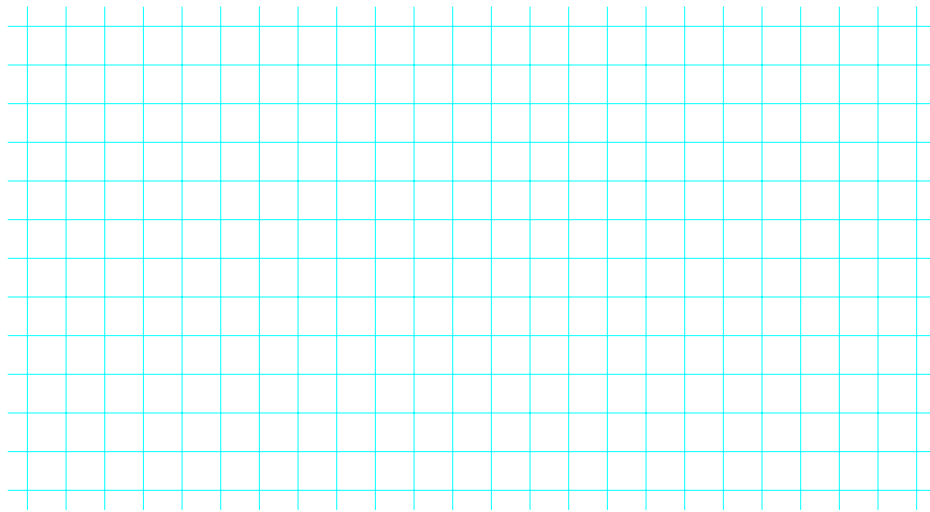
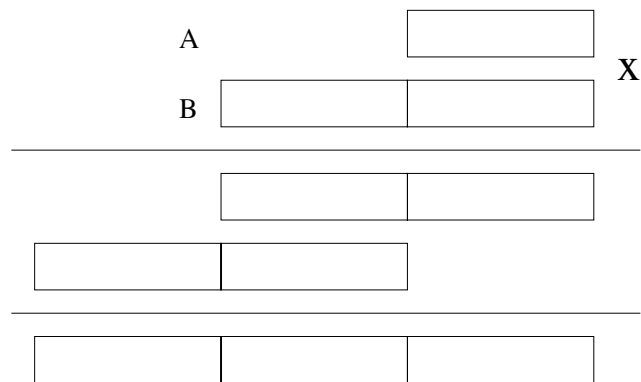
it is **L10** that is considered signed, not the **mdr**.

**Always write the operands as OpA, OpB to avoid confusion!**



# Signed Multi-precision multiplication

A signed, B unsigned



Use the signed operations only on the MSB of each signed operand.  
When using signed operations, sign-extend the partial product.

# Signed multiplication: sign extensions

In most cases (excluding some operand conflicts) the sign extensions of all registers is available by just **pre-pending the letter **S** to the register name.**

**SSR registers: **SL0** to **SL31**, and **SR0** to **SR31****

**MHI register: **smhi****

**MDR register: **smdr****

The sign extensions are *rvalues* only.





# Multi-precision multiplication: signed

A 

--	--

 X

B 

--	--

---

--	--	--	--

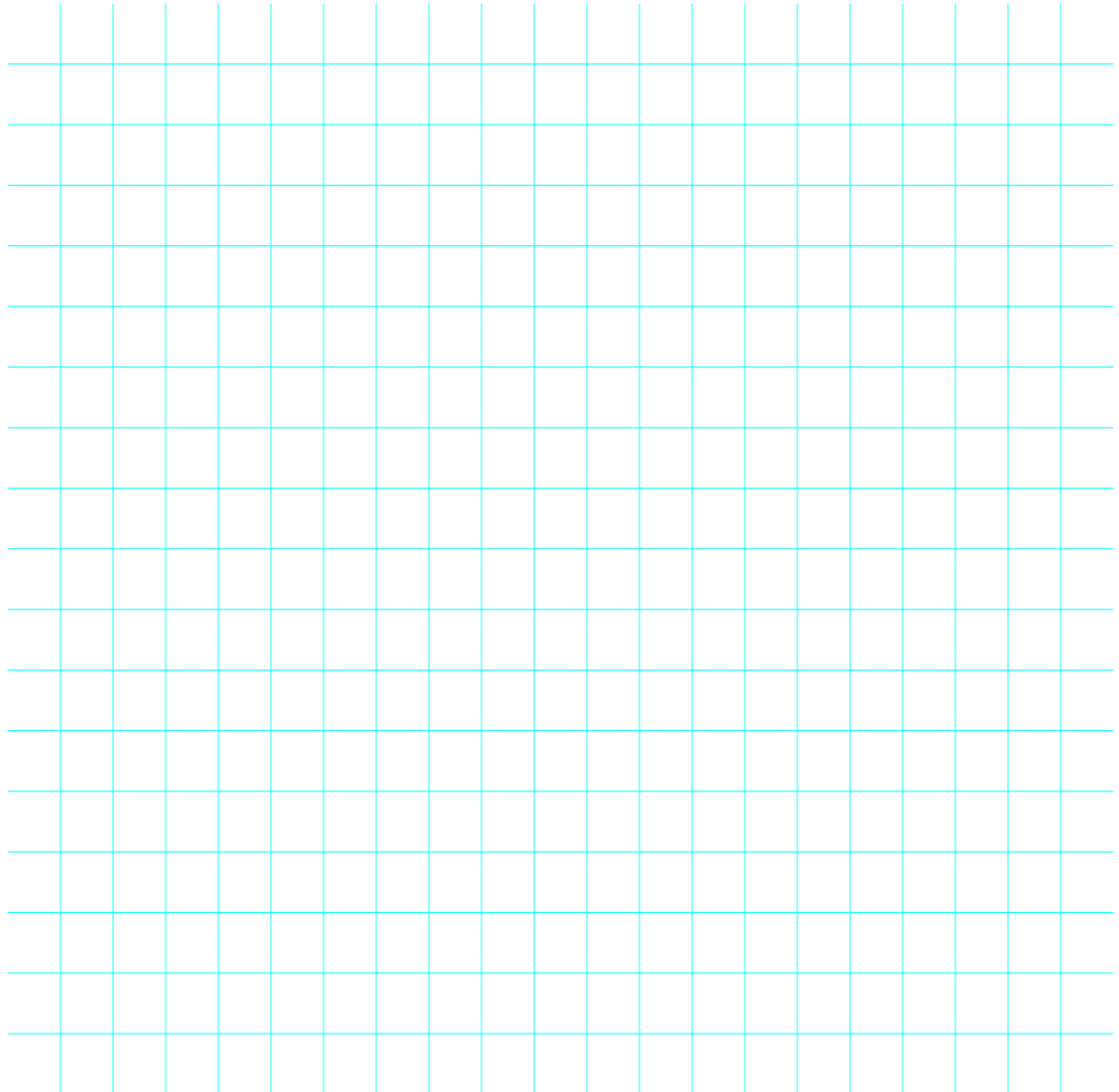
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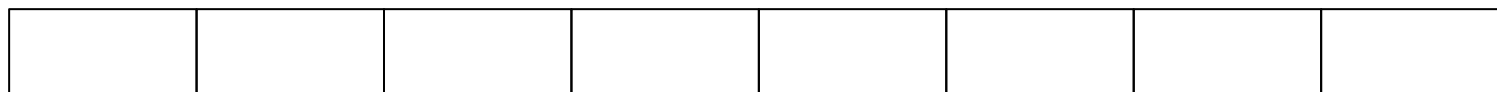
# Signed multi-precision multiplication

Why use the signed operations only on the MSB of each operand?



# Fixed-point representation

Used extensively in image processing and in machine learning.  
Also used in our last SIMD assignment, Mandelbrot, like this:



## Optional programming assignment: fixed-point multiplication

Multiply two 2-byte numbers that represent fixed-point values in the format 4.12 (4-bit integer part and 12-bit fractional part), and produce a product *in the same format*, on two bytes.

# Actual shift operations in Kestrel (1/2)

In Kestrel, shifting is done with the multiplier, NOT with the bit-shifter. Example of **left shift**:  $[L1:L0] \ll 3$



# Actual shift operations in Kestrel (2/2)

Example of **right shift**:  $[L1:L0] \gg 3$ .

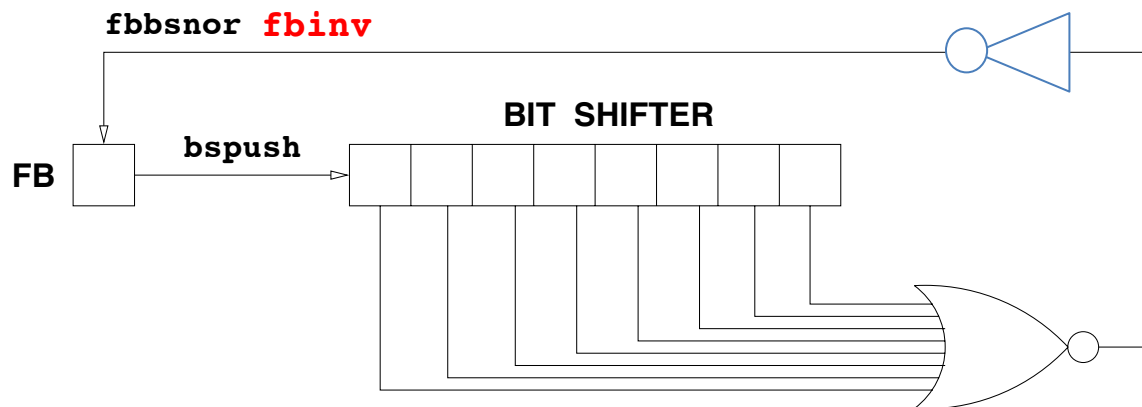
How to differentiate between logic and arithmetic right shift?



1) Save the bit shifter in a register or in memory

2) Push onto the bit shifter a bit to summarize the on/off state of the PE with **fbbsnor fbinv**, which writes the flag bus with the OR of all bits in the bit shifter.

Note that there is no need to clear the bit shifter before pushing it.



## Deeply nested conditionals (cont.)

3) Restore the bit shifter when returning:

```
move    L29, L29 bslatch
```

that executes in all PEs regardless of the mask, and sets the mask.

NOTE that:

```
move    L29, L29, bscondlatch
```

only executes in active PEs and does *not* set the mask, therefore do not use it for conditional stack execution. We'll see its use later.

