

PRACTICE PROBLEMS BASED ON MAGNETIC DISK-

Problem-01:

Consider a disk pack with the following specifications- 16 surfaces, 128 tracks per surface, 256 sectors per track and 512 bytes per sector.

Answer the following questions-

1. What is the capacity of disk pack?
2. What is the number of bits required to address the sector?
3. If the format overhead is 32 bytes per sector, what is the formatted disk space?
4. If the format overhead is 64 bytes per sector, how much amount of memory is lost due to formatting?
5. If the diameter of innermost track is 21 cm, what is the maximum recording density?
6. If the diameter of innermost track is 21 cm with 2 KB/cm, what is the capacity of one track?
7. If the disk is rotating at 3600 RPM, what is the data transfer rate?
8. If the disk system has rotational speed of 3000 RPM, what is the average access time with a seek time of 11.5 msec?

Solution-

Given-

- Number of surfaces = 16
- Number of tracks per surface = 128
- Number of sectors per track = 256
- Number of bytes per sector = 512 bytes

Part-01: Capacity of Disk Pack-

Capacity of disk pack

= Total number of surfaces x Number of tracks per surface x Number of sectors per track x Number of bytes per sector

= $16 \times 128 \times 256 \times 512$ bytes

Part-02: Number of Bits Required To Address Sector-

Total number of sectors

= Total number of surfaces x Number of tracks per surface x Number of sectors per track

= $16 \times 128 \times 256$ sectors

= 2^{19} sectors

Thus, Number of bits required to address the sector = 19 bits

Part-03: Formatted Disk Space-

Formatting overhead

= Total number of sectors x overhead per sector

= $2^{19} \times 32$ bytes

= $2^{19} \times 2^5$ bytes

= 2^{24} bytes

= 16 MB

Now, Formatted disk space

= Total disk space – Formatting overhead

= 256 MB – 16 MB

= 240 MB

Part-04: Formatting Overhead-

Amount of memory lost due to formatting

= Formatting overhead

= Total number of sectors x Overhead per sector

= $2^{19} \times 64$ bytes

= $2^{19} \times 2^6$ bytes

= 2^{25} bytes

= 32 MB

Part-05: Maximum Recording Density-

Storage capacity of a track

= Number of sectors per track x Number of bytes per sector

= 256×512 bytes

= $2^8 \times 2^9$ bytes

= 2^{17} bytes

= 128 KB

Circumference of innermost track

= $2 \times \pi \times \text{radius}$

= $\pi \times \text{diameter}$

= 3.14×21 cm

= 65.94 cm

Now, Maximum recording density

= Recording density of innermost track

= Capacity of a track / Circumference of innermost track

= 128 KB / 65.94 cm

= 1.94 KB/cm

Part-06: Capacity Of Track-

Circumference of innermost track

$$= 2 \times \pi \times \text{radius}$$

$$= \pi \times \text{diameter}$$

$$= 3.14 \times 21 \text{ cm}$$

$$= 65.94 \text{ cm}$$

Capacity of a track

$$= \text{Storage density of the innermost track} \times \text{Circumference of the innermost track}$$

$$= 2 \text{ KB/cm} \times 65.94 \text{ cm}$$

$$= 131.88 \text{ KB}$$

$$\cong 132 \text{ KB}$$

Part-07: Data Transfer Rate-

Number of rotations in one second

$$= (3600 / 60) \text{ rotations/sec}$$

$$= 60 \text{ rotations/sec}$$

Now, Data transfer rate

$$= \text{Number of heads} \times \text{Capacity of one track} \times \text{Number of rotations in one second}$$

$$= 16 \times (256 \times 512 \text{ bytes}) \times 60$$

$$= 2^4 \times 2^8 \times 2^9 \times 60 \text{ bytes/sec}$$

$$= 60 \times 2^{21} \text{ bytes/sec}$$

$$= 120 \text{ MBps}$$

Part-08: Average Access Time-

Time taken for one full rotation

$$= (60 / 3000) \text{ sec}$$

$$= (1 / 50) \text{ sec}$$

$$= 0.02 \text{ sec}$$

$$= 20 \text{ msec}$$

Average rotational delay

$$= 1/2 \times \text{Time taken for one full rotation}$$

$$= 1/2 \times 20 \text{ msec}$$

$$= 10 \text{ msec}$$

Now, average access time

$$= \text{Average seek time} + \text{Average rotational delay} + \text{Other factors}$$

$$= 11.5 \text{ msec} + 10 \text{ msec} + 0$$

$$= 21.5 \text{ msec}$$

Problem-02:

What is the average access time for transferring 512 bytes of data with the following specifications-

- Average seek time = 5 msec
- Disk rotation = 6000 RPM
- Data rate = 40 KB/sec
- Controller overhead = 0.1 msec

Solution-

Given-

- Average seek time = 5 msec
- Disk rotation = 6000 RPM
- Data rate = 40 KB/sec
- Controller overhead = 0.1 msec

Time Taken For One Full Rotation-

Time taken for one full rotation

$$= (60 / 6000) \text{ sec}$$

$$= (1 / 100) \text{ sec}$$

$$= 0.01 \text{ sec}$$

$$= 10 \text{ msec}$$

Average Rotational Delay-

Average rotational delay

$$= 1/2 \times \text{Time taken for one full rotation}$$

$$= 1/2 \times 10 \text{ msec}$$

$$= 5 \text{ msec}$$

Transfer Time-

Transfer time

$$= (512 \text{ bytes} / 40 \text{ KB}) \text{ sec}$$

$$= 0.0125 \text{ sec}$$

$$= 12.5 \text{ msec}$$

Average Access Time-

Average access time

$$= \text{Average seek time} + \text{Average rotational delay} + \text{Transfer time} + \text{Controller overhead} + \text{Queuing delay}$$

$$= 5 \text{ msec} + 5 \text{ msec} + 12.5 \text{ msec} + 0.1 \text{ msec} + 0$$

$$= 22.6 \text{ msec}$$

Problem-03:

A certain moving arm disk storage with one head has the following specifications-

- Number of tracks per surface = 200
- Disk rotation speed = 2400 RPM
- Track storage capacity = 62500 bits
- Average latency = P msec
- Data transfer rate = Q bits/sec

What is the value of P and Q?

Solution-

Given-

- Number of tracks per surface = 200
- Disk rotation speed = 2400 RPM
- Track storage capacity = 62500 bits

Time Taken For One Full Rotation-

Time taken for one full rotation

$$= (60 / 2400) \text{ sec}$$

$$= (1 / 40) \text{ sec}$$

$$= 0.025 \text{ sec}$$

$$= 25 \text{ msec}$$

Average Latency-

Average latency or Average rotational latency

$$= 1/2 \times \text{Time taken for one full rotation}$$

$$= 1/2 \times 25 \text{ msec}$$

$$= 12.5 \text{ msec}$$

Data Transfer Rate-

Data transfer rate

= Number of heads x Capacity of one track x Number of rotations in one second

= $1 \times 62500 \text{ bits} \times (2400 / 60)$

= 2500000 bits/sec

= $2.5 \times 10^6 \text{ bits/sec}$

Thus, $P = 12.5$ and $Q = 2.5 \times 10^6$

Problem-04:

A disk pack has 19 surfaces and storage area on each surface has an outer diameter of 33 cm and inner diameter of 22 cm. The maximum recording storage density on any track is 200 bits/cm and minimum spacing between tracks is 0.25 mm. Calculate the capacity of disk pack.

Solution-

Given-

- Number of surfaces = 19
- Outer diameter = 33 cm
- Inner diameter = 22 cm
- Maximum recording density = 200 bits/cm
- Inter track gap = 0.25 mm

Number Of Tracks On Each Surface-

Number of tracks on each surface

= $(\text{Outer radius} - \text{Inner radius}) / \text{Inter track gap}$

= $(16.5 \text{ cm} - 11 \text{ cm}) / 0.25 \text{ mm}$

$$= 5.5 \text{ cm} / 0.25 \text{ mm}$$

$$= 55 \text{ mm} / 0.25 \text{ mm}$$

$$= 220 \text{ tracks}$$

Capacity Of Each Track-

Capacity of each track

$$= \text{Maximum recording density} \times \text{Circumference of innermost track}$$

$$= 200 \text{ bits/cm} \times (3.14 \times 22 \text{ cm})$$

$$= 200 \times 69.08 \text{ bits}$$

$$= 13816 \text{ bits}$$

$$= 1727 \text{ bytes}$$

Capacity Of Disk Pack-

Capacity of disk pack

$$= \text{Total number of surfaces} \times \text{Number of tracks per surface} \times \text{Capacity of one track}$$

$$= 19 \times 220 \times 1727 \text{ bytes}$$

$$= 7218860 \text{ bytes}$$

$$= 6.88 \text{ MB}$$

Problem-05:

Consider a typical disk that rotates at 15000 RPM and has a transfer rate of 50×10^6 bytes/sec. If the average seek time of the disk is twice the average rotational delay and the controller's transfer time is 10 times the disk transfer time. What is the average time (in milliseconds) to read or write a 512 byte sector of the disk?

Solution-

Given-

- Rotation speed of the disk = 15000 RPM
- Transfer rate = 50×10^6 bytes/sec
- Average seek time = 2 x Average rotational delay
- Controller's transfer time = 10 x Disk transfer time

Time Taken For One Full Rotation-

Time taken for one full rotation

$$= (60 / 15000) \text{ sec}$$

$$= 0.004 \text{ sec}$$

$$= 4 \text{ msec}$$

Average Rotational Delay-

Average rotational delay

$$= 1/2 \times \text{Time taken for one full rotation}$$

$$= 1/2 \times 4 \text{ msec}$$

$$= 2 \text{ msec}$$

Average Seek Time-

Average seek time

$$= 2 \times \text{Average rotational delay}$$

$$= 2 \times 2 \text{ msec}$$

$$= 4 \text{ msec}$$

Disk Transfer Time-

Disk transfer time

$$= \text{Time taken to read or write 512 bytes}$$

$$\begin{aligned}
 &= 512 \text{ bytes} / (50 \times 10^6 \text{ bytes/sec}) \\
 &= 10.24 \times 10^{-6} \text{ sec} \\
 &= 0.01024 \text{ msec}
 \end{aligned}$$

Controller's Transfer Time-

$$\begin{aligned}
 &\text{Controller's transfer time} \\
 &= 10 \times \text{Disk transfer time} \\
 &= 10 \times 0.01024 \text{ msec} \\
 &= 0.1024 \text{ msec}
 \end{aligned}$$

Average Time To Read Or Write 512 Bytes-

$$\begin{aligned}
 &\text{Average time to read or write 512 bytes} \\
 &= \text{Average seek time} + \text{Average rotational delay} + \text{Disk transfer time} + \text{Controller's transfer time} + \text{Queuing delay} \\
 &= 4 \text{ msec} + 2 \text{ msec} + 0.01024 \text{ msec} + 0.1024 \text{ msec} + 0 \\
 &= 6.11 \text{ msec}
 \end{aligned}$$

Problem-06:

A hard disk system has the following parameters-

- Number of tracks = 500
- Number of sectors per track = 100
- Number of bytes per sector = 500
- Time taken by the head to move from one track to another adjacent track = 1 msec
- Rotation speed = 600 RPM

What is the average time taken for transferring 250 bytes from the disk?

Solution-

Given-

- Number of tracks = 500
- Number of sectors per track = 100
- Number of bytes per sector = 500
- Time taken by the head to move from one track to another adjacent track = 1 msec
- Rotation speed = 600 RPM

Average Seek Time-

Average seek time

= (Time taken by the head to move from track-1 to track-1 + Time taken by the head to move from track-1 to track-500) / 2

= (0 + 499 x 1 msec) / 2

= 249.5 msec

Time Taken For One Full Rotation-

Time taken for one full rotation

= (60 / 600) sec

= 0.1 sec

= 100 msec

Average Rotational Delay-

Average rotational delay

= 1/2 x Time taken for one full rotation

= 1/2 x 100 msec

= 50 msec

Capacity Of One Track-

Capacity of one track

= Number of sectors per track x Number of bytes per sector

= 100 x 500 bytes

= 50000 bytes

Data Transfer Rate-

Data transfer rate

= Number of heads x Capacity of one track x Number of rotations in one second

= 1 x 50000 bytes x (600 / 60)

= 50000 x 10 bytes/sec

= 5×10^5 bytes/sec

Transfer Time-

Transfer time

= (250 bytes / 5×10^5 bytes) sec

= 50×10^{-5} sec

= 0.5 msec

Average Time Taken To Transfer 250 Bytes-

Average time taken to transfer 250 bytes

= Average seek time + Average rotational delay + Transfer time + Controller overhead + Queuing delay

= 249.5 msec + 50 msec + 0.5 msec + 0 + 0

= 300 msec

Problem-07:

A hard disk has 63 sectors per track, 10 platters each with 2 recording surfaces and 1000 cylinders.

The address of a sector is given as a triple (c, h, s) where c is the cylinder number, h is the surface number and s is the sector number. Thus, the 0th sector is addressed as (0,0,0), the 1st sector as (0,0,1) and so on.

Part-01:

The address <400, 16, 29> corresponds to sector number-

1. 505035
2. 505036
3. 505037
4. 505038

Part-02:

The address of 1039 sector is-

1. <0, 15, 31>
2. <0, 16, 30>
3. <0, 16, 31>
4. <0, 17, 31>

Storage Design Based on Application Requirements and Disk Performance

Determining storage requirements for an application begins with determining the required storage capacity. This is easily estimated by the size and number of file systems and database components used by applications. The I/O size, I/O characteristics, and the number of I/Os generated by the application at peak workload are other factors that affect disk performance, I/O response time, and design of storage systems. The I/O block size depends on the file system and the database on which the application is built. Block size in a database environment is controlled by the underlying database engine and the environment variables.

The disk service time (TS) for an I/O is a key measure of disk performance; TS, along with disk utilization rate (U), determines the I/O response time for an application. As discussed earlier, the total disk service time (TS) is the sum of the seek time (T), rotational latency (L), and internal transfer time (X):

$$TS = T + L + X.$$

Consider an example with the following specifications provided for a disk:

The average seek time is 5 ms in a random I/O environment; therefore, $T = 5$ ms.

Disk rotation speed of 15,000 revolutions per minute or 250 revolutions per second — from which rotational latency (L) can be determined, which is one-half of the time taken for a full rotation or $L = (0.5/250 \text{ rps expressed in ms})$.

40 MB/s internal data transfer rate, from which the internal transfer time (X) is derived based on the block size of the I/O — for example, an I/O with a block size of 32 KB; therefore $X = 32 \text{ KB}/40 \text{ MB}$.

Consequently, the time taken by the I/O controller to serve an I/O of block size 32 KB is $(TS) = 5 \text{ ms} + (0.5/250) + 32 \text{ KB}/40 \text{ MB} = 7.8 \text{ ms}$.

Therefore, the maximum number of I/Os serviced per second or IOPS is $(1/TS) = 1/(7.8 \times 10^{-3}) = 128 \text{ IOPS}$

Table 2-1: IOPS Performed by Disk Drive

BLOCK SIZE	$T_s = T + L + X$	$IOPS = 1/T_s$
4 KB	$5 \text{ ms} + (0.5/250 \text{ rps}) + 4 \text{ K}/40 \text{ MB} = 5 + 2 + 0.1 = 7.1$	140
8 KB	$5 \text{ ms} + (0.5/250 \text{ rps}) + 8 \text{ K}/40 \text{ MB} = 5 + 2 + 0.2 = 7.2$	139
16 KB	$5 \text{ ms} + (0.5/250 \text{ rps}) + 16 \text{ K}/40 \text{ MB} = 5 + 2 + 0.4 = 7.4$	135
32 KB	$5 \text{ ms} + (0.5/250 \text{ rps}) + 32 \text{ K}/40 \text{ MB} = 5 + 2 + 0.8 = 7.8$	128
64 KB	$5 \text{ ms} + (0.5/250 \text{ rps}) + 64 \text{ K}/40 \text{ MB} = 5 + 2 + 1.6 = 8.6$	116

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