

ASSIGNMENT - 1

Name: Amit Kumar Sahu

Reg. No: 18MIS7250

Slot: 11

Subject: Numerical Methods for Engineers

Assignment - 1

Que 1 The flow rate, Q in a pipe system connecting two reservoirs is described by the equation $Qe^Q - 1 = 0$. Approximate the real root of the eqⁿ in the interval $0 \leq Q \leq 1$

solⁿ let $Q_0 = 1$

$$f'(Q) = [Qe^Q + e^Q] - 0$$
$$= Qe^Q + e^Q$$

$$f'(Q_0) = 1 \cdot e^1 + e^1 = 2e^1 = 2 \times (2.7182)$$
$$= 5.43656$$

First iteration $Q_1 = Q_0 - \frac{f(Q_0)}{f'(Q_0)}$

$$= 1 - \frac{(2.7182 - 1)}{5.43656}$$
$$= 0.6839$$

Second iteration $Q_2 = Q_1 - \frac{f(Q_1)}{f'(Q_1)}$

$$= 0.6839 - \frac{(e^{0.6839} \times 0.6839) - 1}{2 \times e^{0.6839}}$$
$$= 0.6839 - \frac{1.7104}{3.9632}$$
$$= 0.2523$$

Third iteration: $Q_3 = Q_2 - \frac{f(Q_2)}{f'(Q_2)}$

$$= 0.2523 - \frac{(e^{0.2523} \times 0.2523 - 1)}{2 \times e^{0.2523}}$$

$$= 0.2523 - \frac{(-0.6753)}{(2.57396)}$$

$$= 0.51466$$

Fourth iteration: $Q_4 = Q_3 - \frac{f(Q_3)}{f'(Q_3)}$

$$= 0.5147 - \frac{(e^{0.5147} \times 0.5147 - 1)}{2 \times e^{0.5147}}$$

$$= 0.5147 - \left[\frac{-0.00388}{3.3462} \right]$$

$$= 0.5147 + \frac{0.1388}{3.3462}$$

$$= 0.55618$$

Approx real root can be ≈ 0.55618

2. Estimate the minimum weight of a bib taps when bore is 20 mm using:

Bore (in mm)	8	10	15	25	32	40	50
Weight (in kg)	0.25	0.30	0.40	1.25	1.70	2.15	3.65

x_1	x	Δ	Δ^2	Δ^3	Δ^4	Δ^5	Δ^6
8	0.25						
		0.025					
10	0.30		-0.000102	2.60×10^{-4}			
		0.02		2.60×10^{-4}			
15	0.40		0.00433		4.16×10^{-7}		
		0.085		2.52×10^{-4}		1.028×10^{-7}	
25	1.25		-0.00121		3.73×10^{-6}		
		0.0643		1.377×10^{-3}		-0.142×10^{-5}	
32	1.70		0.03321		-3.4×10^{-4}		
		0.5625		-0.01049			
40	2.15		-0.2292				
		0.15					
50	3.65						

Using Newton's divided difference formula eg:-

$$f[x_1, x_2] = \frac{f_2 - f_1}{x_2 - x_1}$$

And finally

$$\Delta^6 = \frac{(-0.005 \times 10^{-5} - 1.028 \times 10^{-7})}{(50-8)} = -0.000202 - 2.75 \times 10^{-7}$$

Using Newton's Divided formula -

$$\begin{aligned} f(20) &= f(x_0) + f(x-x_0) f[x_0, x_1] + f(x-x_0) f[x-x_1] \\ &\quad f[x_0, x_1, x_2] + \dots \\ &= 0.25 + (20-8)(0.025) + (12)(20-10)(-0.000202) + \\ &\quad 12 \times 10 \times (20-15)(2.6 \times 10^{-9}) + \\ &\quad 12 \times 10 \times 5 \times (20-25) \times (4.16 \times 10^{-7}) + \\ &\quad 12 \times 10 \times 5 \times (-5) \times (20-32) \times (1.028 \times 10^{-7}) + \\ &\quad 12 \times 10 \times 5 \times (-5) \times (-32) \times (20-40) \times (-0.000202) \\ &= 0.25 + 0.3 + (-0.01224) + 0.156 - (1.243 \times 10^{-3}) \\ &\quad + (3.7008 \times 10^{-3}) + 0.148 \\ &= 0.89088708 \end{aligned}$$

Hence when bore size is 20mm the weight is approximately 0.89088708 kg