

# **MAT2001 – Numerical Methods for Engineers**

## **MATLAB Report**

**Prepared by**

**Name: Amit Kumar Sahu**

**Reg No: 18MIS7250**

**Submitted to**

**Dr Satyanarayana Badeti**

**Course Instructor**

## MATLAB Experiment No – 1

**Name:** Amit Kumar Sahu

**Reg No:** 18MIS7250

**Aim:** To implement Newton's Raphson method for a system for linear system of equation.

**Objective:** we have to solve a nonlinear equation,  $f(x)=0$  that we cannot easily solve analytically.

**Algorithm :**

This is a very popular method that usually converges rapidly. It solves the equation  $f(x)=0$ , assuming that we can compute  $f'(x)$ . The iterations start with an initial guess  $x_0$  and proceeds as 
$$x_{k+1}=x_k-\{f(x_k)/f'(x_k)\}.$$

**MATLAB Code:**

```
function [x,y]=Newton(fun,funpr,x1,tol,kmax)

x(1)=x1;

y(1)=feval(fun,x(1));

ypr(1)=feval(funpr,x(1));

for k=2:kmax

    x(k)=x(k-1)-y(k-1)/ypr(k-1);

    y(k)=feval(fun,x(k));

    if abs(x(k)-x(k-1))<tol

        disp('Newton method has converged');

        break;

    end

    ypr(k)=feval(funpr,x(k));

    iter=k;

end

if(iter>=kmax)

    disp('zero not found to desired tolerance');

end
```

```

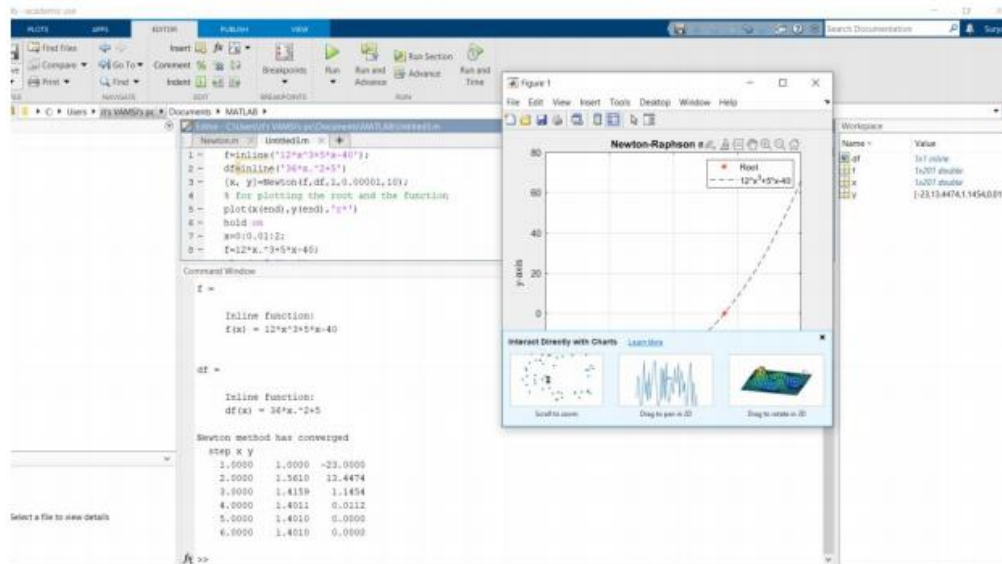
n=length(x);
k=1:n;
out=[k' x' y'];
disp(' step x y')
disp(out)

Untitled3.m

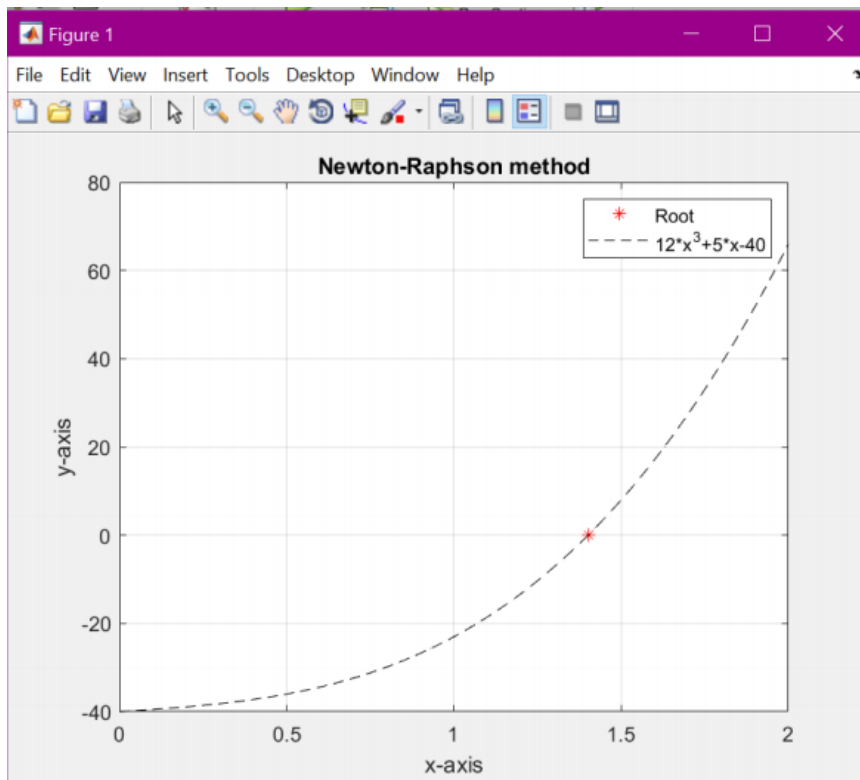
f=inline('12*x^3+5*x-40')
df=inline('36*x.^2+5')
[x, y]=Newton(f,df,1,0.00001,10);
% for plotting the root and the function plot(x(end),y(end),'r*')
hold on
x=0:0.01:2;
f=12*x.^3+5*x-40;
plot(x,f,'k--')
grid on
xlabel('x-axis')
ylabel('y-axis')
title('Newton-Raphson method')
legend('Root','12*x^3+5*x-40')

```

**Output:**



Graph:



## MATLAB Experiment No – 2

**Name:** Amit Kumar Sahu

**Reg No:** 18MIS7250

**Aim:** To implement Newton's method for a system of three equations

**Objective:** we have to solve a nonlinear equation,  $f(x)=0$  that we cannot easily solve analytically.

**Algorithm :**

This is a very popular method that usually converges rapidly. It solves the equation  $f(x)=0$ , assuming that we can compute  $f'(x)$ . The iterations start with an initial guess  $x_0$  and proceeds as

$$x_{k+1} = x_k - \{f(x_k)/f'(x_k)\}.$$

**MATLAB Code:**

```
function x = NewtonSys(F,J,x0,tol,kmax)
xold=x0; iter=1;
while(iter<=kmax)
    y=-feval(J,xold)\feval(F,xold);
    xnew=xold+y';
    dif=norm(xnew-xold);
    disp([iter xnew dif]);
    if dif<=tol
        x=xnew;
        disp('Newton method has converged')
    return;
    else
        xold=xnew;
    end
    iter=iter+1
end
disp('Newton method has converged')
x=xnew

disp("For A=1 & B=1 the values are")
F=inline('[1+x(1)^2*x(2)-2*x(1); x(1)-x(1)^2*x(2)]');
F1=inline('[1+x(1)^2*x(2)-4*x(1); 3*x(1)-x(1)^2*x(2)]');
F2=inline('[1+x(1)^2*x(2)-3*x(1); 2*x(1)-x(1)^2*x(2)]');
J=inline('[2*x(1)*x(2) - 2, x(1)^2;1 - 2*x(1)*x(2), -x(1)^2]')
x0=[1 1]; tol=0.0001;kmax=20;
disp("For A=1 & B=1 the values are")
x=NewtonSys(F,J,x0,tol,kmax)
disp("For A=1 & B=3 the values are")
x1=NewtonSys(F1,J,x0,tol,kmax)
disp("For A=1 & B=2 the values are")
x2=NewtonSys(F2,J,x0,tol,kmax)
```

### Output:

```
>> runningnewtonsysmethod  
For A=1 & B=1 the values are
```

```
J =
```

```
Inline function:
```

```
J(x) = [2*x(1)*x(2) - 2, x(1)^2; 1 - 2*x(1)*x(2), -x(1)^2]
```

```
For A=1 & B=1 the values are
```

```
1      1      1      0
```

```
Newton method has converged
```

```
x =
```

```
1      1
```

```
For A=1 & B=3 the values are
```

```
1      1      3      2
```

```
iter =
```

```
2
```

```
2      1      3      0
```

```
Newton method has converged
```

```
x1 =
```

```
1      3
```

```
For A=1 & B=2 the values are
```

```
1      1      2      1
```

```
iter =
```

```
2
```

```
2      1      2      0
```

```
Newton method has converged
```

```
x2 =
```

```
1      2
```

### MATLAB Experiment No – 3

**Name:** Amit Kumar Sahu

**Reg No:** 18MIS7250

**Aim:** To solve the system secant method

**Objective:** To find root  $r$  that uses a succession of roots of secant lines to better approximate a root of a function  $f$ .

**Algorithm :** The secant method is defined by the recurrence relation

$$x_n = x_{n-1} - f(x_{n-1}) \frac{x_{n-1} - x_{n-2}}{f(x_{n-1}) - f(x_{n-2})} = \frac{x_{n-2}f(x_{n-1}) - x_{n-1}f(x_{n-2})}{f(x_{n-1}) - f(x_{n-2})}.$$

As can be seen from the recurrence relation, the secant method requires two initial values,  $x_0$  and  $x_1$ , which should ideally be chosen to lie close to the root.

#### MATLAB Code:

```
function [xx, yy]=Secant(f,a,b,tol,kmax)
y(1)=f(a);
y(2)=f(b);
x(1)=a;
x(2)=b;
Dx(1)=0;
Dx(2)=0;
disp(' step x(k-1) x(k) x(k+1) y(k+1) Dx(k+1)')
for k=2:kmax
    x(k+1)=x(k)-y(k)*(x(k)-x(k-1))/(y(k)-y(k-1));
    y(k+1)=f(x(k+1));
    Dx(k+1)=x(k+1)-x(k);
    iter=k-1;
    out=[iter, x(k-1),x(k),x(k+1),y(k+1),Dx(k+1)];
    disp(out)
    xx=x(k+1);
    yy=y(k+1);
    if abs(y(k+1))<tol
        disp('Secant method has converged'); break;
    end
    if (iter>=kmax)
        disp('zero not found to desired tolerance');
    end
end
```

```
f=@(x) 2*x.^2+3*log(x)-1;
```

```

a=1;b=2;
tol=0.00001;kmax=10;
[xx, yy]=Secant(f,a,b,tol,kmax);
x=0:0.01:3;
y=2*x.^2+3*log(x)-1;
plot(x,y)
hold on
plot(xx(end),yy(end),'r*')
hold on
xlabel('X-Axis')
ylabel('Y-Axis')
title('Secant Method')

```

### Output:

step x(k-1) x(k) x(k+1) y(k+1) Dx(k+1

1.0000 0.5000 1.0000 0.8603 0.0289 -0.1397

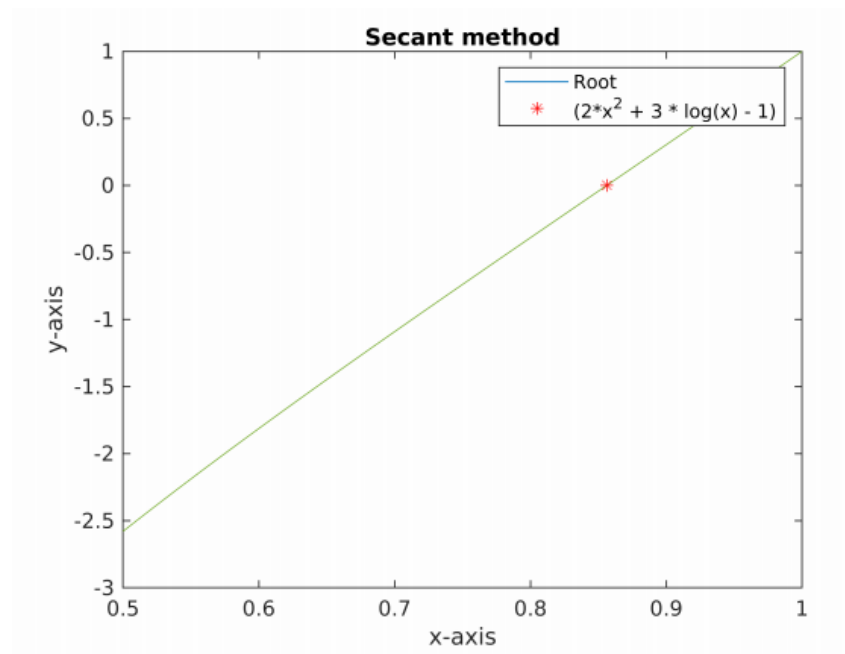
2.0000 1.0000 0.8603 0.8562 0.0001 -0.0042

3.0000 0.8603 0.8562 0.8561 -0.0000 -0.0000

secant method has converged

0.8561 -0.0000

### Graph:





## MATLAB Experiment No – 4

**Name:** Amit Kumar Sahu

**Reg No:** 18MIS7250

**Aim:** To solve the system using Gauss Elimination

**Objective:** Solving systems of linear equations. It consists of a sequence of operations performed on the corresponding matrix of coefficients

**Algorithm:** Gaussian elimination allows the computation of the determinant of a square matrix, we have to recall how the elementary row operations change the determinant:

- Swapping two rows multiplies the determinant by  $-1$
- Multiplying a row by a nonzero scalar multiplies the determinant by the same scalar
- Adding to one row a scalar multiple of another does not change the determinant.

If Gaussian elimination applied to a square matrix  $A$  produces a row echelon matrix  $B$ , let  $d$  be the product of the scalars by which the determinant has been multiplied, using the above rules. Then the determinant of  $A$  is the quotient by  $d$  of the product of the elements of the diagonal of  $B$ :

$$\det(A) = \frac{\prod \text{diag}(B)}{d}.$$

### MATLAB Code:

```
function x=Gaussele(A,b);
A=[1 3 5;2 -1 -3;4 5 -1];
b=[14;3;7];
[m,n]=size(A);
if m~=n
    error('Matrix A must be square');
end
nb=n+1;
Aug=[A b];

for k=1:n-1
    for i=k+1:n
        factor=Aug(i,k)/Aug(k,k);
        Aug(i,k:nb)=Aug(i,k:nb)-factor*Aug(k,k:nb);
    end
end
```

```
x=zeros(n,1);
x(n)=Aug(n,nb)/Aug(n,n);
for i=n-1:-1:1
    x(i)=(Aug(i,nb)-Aug(i,i+1:n)*x(i+1:n))/Aug(i,i);
end
disp('Gauss elimination method')
x(i);
```

**Output:**

```
gaussian_method
Gauss elimination method
```

```
ans =
```

```
    5
   -2
    3
```

## MATLAB Experiment No – 5

**Name:** Amit Kumar Sahu

**Reg No:** 18MIS7250

**Aim:** To solve the system Gauss Siedel method

**Objective:** Iteratively solving the system of linear equations

**Algorithm:**

Inputs:  $A$ ,  $b$

Output:

Choose an initial guess to the solution

**repeat** until convergence

**for**  $i$  from 1 until  $n$  do

**for**  $j$  from 1 until  $n$  do

**if**  $j \neq i$  then

**end if**

**end** ( $j$ -loop)

**end** ( $i$ -loop)

    check if convergence is reached

**end** (repeat)

**MATLAB Code:**

```
clear ; clc ; close all
n = input('size of the equation system n = ');
C = input('Matrix C ');
b = input('Matrix b ');
dett = det(C)
if dett == 0
    print('cannot solve because det(C) = 0 ')
else
    b = b'
    A = [ C b ]
    for j = 1:(n-1)
        for i= (j+1) : n
            mult = A(i,j)/A(j,j) ;
            for k= j:n+1
                A(i,k) = A(i,k) - mult*A(j,k) ;
            A
```

```

        end
    end
end
for p = n:-1:1
    for r = p+1:n
        x(p) = A(p,r)/A(p,r-1)
    end
end
end

```

### Output:

size of the equation system n =

3

Matrix C

[6 -2 1;1 2 -5;-2 7 2]

Matrix b

[0 0 0]

dett =

229.0000

b =

0

0

0

A =

6 -2 1 0

1 2 -5 0

-2 7 2 0

A =

|    |    |    |   |
|----|----|----|---|
| 6  | -2 | 1  | 0 |
| 0  | 2  | -5 | 0 |
| -2 | 7  | 2  | 0 |

A =

|         |         |         |   |
|---------|---------|---------|---|
| 6.0000  | -2.0000 | 1.0000  | 0 |
| 0       | 2.3333  | -5.0000 | 0 |
| -2.0000 | 7.0000  | 2.0000  | 0 |

A =

|         |         |         |   |
|---------|---------|---------|---|
| 6.0000  | -2.0000 | 1.0000  | 0 |
| 0       | 2.3333  | -5.1667 | 0 |
| -2.0000 | 7.0000  | 2.0000  | 0 |

A =

|         |         |         |   |
|---------|---------|---------|---|
| 6.0000  | -2.0000 | 1.0000  | 0 |
| 0       | 2.3333  | -5.1667 | 0 |
| -2.0000 | 7.0000  | 2.0000  | 0 |

A =

|        |         |         |   |
|--------|---------|---------|---|
| 6.0000 | -2.0000 | 1.0000  | 0 |
| 0      | 2.3333  | -5.1667 | 0 |
| 0      | 7.0000  | 2.0000  | 0 |

A =

|        |         |         |   |
|--------|---------|---------|---|
| 6.0000 | -2.0000 | 1.0000  | 0 |
| 0      | 2.3333  | -5.1667 | 0 |
| 0      | 6.3333  | 2.0000  | 0 |

A =

|        |         |         |   |
|--------|---------|---------|---|
| 6.0000 | -2.0000 | 1.0000  | 0 |
| 0      | 2.3333  | -5.1667 | 0 |
| 0      | 6.3333  | 2.3333  | 0 |

A =

|        |         |         |   |
|--------|---------|---------|---|
| 6.0000 | -2.0000 | 1.0000  | 0 |
| 0      | 2.3333  | -5.1667 | 0 |
| 0      | 6.3333  | 2.3333  | 0 |

A =

|        |         |         |   |
|--------|---------|---------|---|
| 6.0000 | -2.0000 | 1.0000  | 0 |
| 0      | 2.3333  | -5.1667 | 0 |
| 0      | 0       | 2.3333  | 0 |

A =

|        |         |         |   |
|--------|---------|---------|---|
| 6.0000 | -2.0000 | 1.0000  | 0 |
| 0      | 2.3333  | -5.1667 | 0 |
| 0      | 0       | 16.3571 | 0 |

A =

|        |         |         |   |
|--------|---------|---------|---|
| 6.0000 | -2.0000 | 1.0000  | 0 |
| 0      | 2.3333  | -5.1667 | 0 |
| 0      | 0       | 16.3571 | 0 |

x =

|   |         |
|---|---------|
| 0 | -2.2143 |
|---|---------|

x =

|         |         |
|---------|---------|
| -0.3333 | -2.2143 |
|---------|---------|

x =

|         |         |
|---------|---------|
| -0.5000 | -2.2143 |
|---------|---------|

## MATLAB Experiment No – 6

**Name:** Amit Kumar Sahu

**Reg No:** 18MIS7250

**Aim:** To solve the system Jacobi method

**Objective:** For determining the solutions of a strictly diagonally dominant system of linear equations.

**Algorithm :**

```
Input: initial guess  $x^{(0)}$  to the solution, (diagonal dominant) matrix  $A$ , right-hand side vector  $b$ , convergence criterion  
Output: solution when convergence is reached  
Comments: pseudocode based on the element-based formula above
```

```
k = 0  
while convergence not reached do  
    for i := 1 step until n do  
         $\sigma = 0$   
        for j := 1 step until n do  
            if j  $\neq$  i then  
                 $\sigma = \sigma + a_{ij}x_j^{(k)}$   
            end  
        end  
         $x_i^{(k+1)} = \frac{1}{a_{ii}} (b_i - \sigma)$   
    end  
    k = k + 1  
end
```

**MATLAB Code:**

```
clc;  
clear all;  
A=[5 -2 3;-3 9 1;2 -1 -7]  
b=[-1;2;3]  
N=40  
x=[1,1,1]  
jacobi(A, b, N)  
  
function jacobi(A, b, N)  
test=all((2*abs(diag(A)))- sum(abs(A),2)>=0);  
if test==0  
    A([1 2],:) = A([2 1],:);  
    b([1 2]) = b([2 1]);  
end  
  
test=all((2*abs(diag(A)))- sum(abs(A),2)>=0);  
  
if test==0  
    A([2 1],:) = A([1 2],:);  
    b([2 1]) = b([1 2]);  
    A([1 3],:) = A([3 1],:);  
    b([1 3]) = b([3 1]);  
    disp("not a dominant vector")
```

```

end
disp(" dominant vector")

d=diag(A);
D=diag(d);
disp("Displaying the diagonal matrix")
disp(D)
D_inv=inv(D);
disp("Displaying the inverse of diagonal matrix")
disp(D_inv)
E=A-D;
disp("Displaying remainder matrix")
disp(E)
x=[1;1;1];
T=-D_inv*E;
C=D_inv*b;

for j=1:N
    x=T*x+C;
end
disp("Here are the result of the following matrix: ")
disp(x)
end

```

### Output:

A =

|    |    |    |
|----|----|----|
| 5  | -2 | 3  |
| -3 | 9  | 1  |
| 2  | -1 | -7 |

b =

|    |
|----|
| -1 |
| 2  |
| 3  |

N =

40

x =



1      1      1

dominant vector

Displaying the diagonal matrix

5      0      0  
0      9      0  
0      0     -7

Displaying the inverse of diagonal matrix

0.2000              0              0  
0      0.1111              0  
0              0     -0.1429

Displaying remainder matrix

0     -2      3  
-3      0      1  
2     -1      0

Here are the result of the following matrix:

0.1861  
0.3312  
-0.4227

## MATLAB Experiment No – 7

**Name:** Amit Kumar Sahu

**Reg No:** 18MIS7250

**Aim:** To solve the system using LU Decomposition

**Objective:** Factors a matrix as the product of a lower triangular matrix and an upper triangular matrix.

**Algorithm:**

Let  $A$  be a square matrix. An **LU factorization** refers to the factorization of  $A$ , with proper row and/or column orderings or permutations, into two factors – a lower triangular matrix  $L$  and an upper triangular matrix  $U$ :

$$A=LU$$

In the lower triangular matrix all elements above the diagonal are zero, in the upper triangular matrix, all the elements below the diagonal are zero. For example, for a  $3 \times 3$  matrix  $A$ , its LU decomposition looks like this:

$$\begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix} = \begin{bmatrix} \ell_{11} & 0 & 0 \\ \ell_{21} & \ell_{22} & 0 \\ \ell_{31} & \ell_{32} & \ell_{33} \end{bmatrix} \begin{bmatrix} u_{11} & u_{12} & u_{13} \\ 0 & u_{22} & u_{23} \\ 0 & 0 & u_{33} \end{bmatrix}.$$

Without a proper ordering or permutations in the matrix, the factorization may fail to materialize.

For example, it is easy to verify (by expanding the matrix multiplication) that  $\ell_{21}u_{11} = a_{21}$ . If  $a_{21} \neq 0$ , then

at least one of  $\ell_{21}$  and  $u_{11}$  has to be zero, which implies that either  $L$  or  $U$  is [singular](#). This is impossible if  $A$  is nonsingular (invertible). This is a procedural problem. It can be removed by simply reordering the rows of  $A$  so that the first element of the permuted matrix is nonzero. The same problem in subsequent factorization steps can be removed the same way; see the basic procedure below.

**MATLAB Code:**

```
clc;
clear all;
A = [10 -7 0
     -3  2 6
       5 -1 5];
[L,U] = lu(A)
disp("calculating L*U")
```

```

L*U
[L,U,P] = lu(A)
disp("calculating P'*L*U")
P'*L*U

```

**Output:**

L =

|         |         |        |
|---------|---------|--------|
| 1.0000  | 0       | 0      |
| -0.3000 | -0.0400 | 1.0000 |
| 0.5000  | 1.0000  | 0      |

U =

|         |         |        |
|---------|---------|--------|
| 10.0000 | -7.0000 | 0      |
| 0       | 2.5000  | 5.0000 |
| 0       | 0       | 6.2000 |

calculating L\*U

ans =

|         |         |        |
|---------|---------|--------|
| 10.0000 | -7.0000 | 0      |
| -3.0000 | 2.0000  | 6.0000 |
| 5.0000  | -1.0000 | 5.0000 |

L =

|         |         |        |
|---------|---------|--------|
| 1.0000  | 0       | 0      |
| 0.5000  | 1.0000  | 0      |
| -0.3000 | -0.0400 | 1.0000 |

U =

|         |         |   |
|---------|---------|---|
| 10.0000 | -7.0000 | 0 |
|---------|---------|---|

|   |        |        |
|---|--------|--------|
| 0 | 2.5000 | 5.0000 |
| 0 | 0      | 6.2000 |

P =

|   |   |   |
|---|---|---|
| 1 | 0 | 0 |
| 0 | 0 | 1 |
| 0 | 1 | 0 |

calculating  $P' * L * U$

ans =

|         |         |        |
|---------|---------|--------|
| 10.0000 | -7.0000 | 0      |
| -3.0000 | 2.0000  | 6.0000 |
| 5.0000  | -1.0000 | 5.0000 |

## MATLAB Experiment No – 8

**Name:** Amit Kumar Sahu

**Reg No:** 18MIS7250

**Aim:** Implementing Power Method.

**Objective:** The algorithm will produce a number Lambda, which is the greatest (in absolute value) eigenvalue of A, and a nonzero vector v, which is a corresponding eigenvector of Lambda, that is,  $Av=(\text{Lambda})*(v)$ .

**Algorithm:** The power iteration algorithm starts with a vector  $b_0$ , which may be an approximation to the dominant eigenvector or a random vector. The method is described by the recurrence relation

$$b_{k+1} = \frac{Ab_k}{\|Ab_k\|}$$

**MATLAB Code:**

```
n=input('Enter dimension of the matrix, n: ');
A = zeros(n,n);
x = zeros(1,n);
y = zeros(1,n);
tol = input('Enter the tolerance, tol: ');
m = input('Enter maximum number of iterations, m: ');

A=[1 2 0; -2 1 2; 1 3 1];
x=[1 1 1];

k = 1; lp = 1;
amax = abs(x(1));
for i = 2 : n
    if abs(x(i)) > amax
        amax = abs(x(i));
        lp = i;
    end
end
for i = 1 : n
    x(i) = x(i)/amax;
end

fprintf('\n\n Ite.      Eigenvalue      .....Eigenvectores.....\n');
while k <= m
    for i = 1 : n
        y(i) = 0;
```

```

        for j = 1 : n
            y(i) = y(i) + A(i,j) * x(j);
        end
    end
    ymu = y(lp);
    lp = 1;
    amax = abs(y(1));
    for i = 2 : n
        if abs(y(i)) > amax
            amax = abs(y(i));
            lp = i;
        end
    end
    if amax <= 0
        fprintf('0 eigenvalue - select another ');
        fprintf('initial vector and begin again\n');
    else
        err = 0;
        for i = 1 : n
            t = y(i)/y(lp);
            if abs(x(i)-t) > err
                err = abs(x(i)-t);
            end
            x(i) = t;
        end
        fprintf('%4d      %11.8f', k, ymu);
        for i = 1 : n
            fprintf('      %11.8f', x(i));
        end
        fprintf('\n');
        if err <= tol
            fprintf('\n\nThe eigenvalue after %d iterations is: %11.8f \n',k, ymu);
            fprintf('The corresponding eigenvector is: \n');
            for i = 1 : n
                fprintf('                %11.8f \n', x(i));
            end
            fprintf('\n');
            break;
        end
        k = k+1;
    end
end
if k > m
    fprintf('Method did not converge within %d iterations\n', m);
end

```

### Output:

powermethod

Enter dimension of the matrix, n:

3

Enter the tolerance, tol:

0.001

Enter maximum number of iterations, m:

8

| Ite. | Eigenvalue | .....Eigenvectores..... |            |            |
|------|------------|-------------------------|------------|------------|
| 1    | 3.00000000 | 0.60000000              | 0.20000000 | 1.00000000 |
| 2    | 2.20000000 | 0.45454545              | 0.45454545 | 1.00000000 |
| 3    | 2.81818182 | 0.48387097              | 0.54838710 | 1.00000000 |
| 4    | 3.12903226 | 0.50515464              | 0.50515464 | 1.00000000 |
| 5    | 3.02061856 | 0.50170648              | 0.49488055 | 1.00000000 |
| 6    | 2.98634812 | 0.49942857              | 0.49942857 | 1.00000000 |
| 7    | 2.99771429 | 0.49980938              | 0.50057186 | 1.00000000 |
| 8    | 3.00152497 | 0.50006351              | 0.50006351 | 1.00000000 |

The eigenvalue after 8 iterations is: 3.00152497

The corresponding eigenvector is:

0.50006351

0.50006351

1.00000000

## MATLAB Experiment No – 9

**Name:** Amit Kumar Sahu

**Reg No:** 18MIS7250

**Aim:** Implementing Lagrange's interpolation.

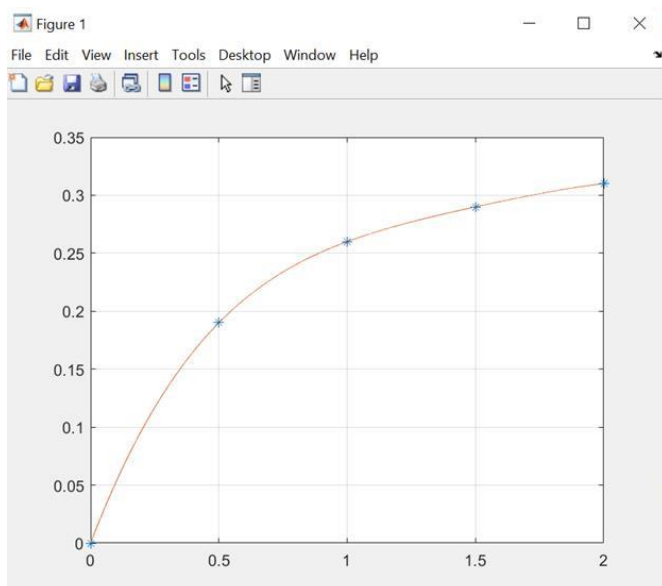
**MATLAB Code:**

```
function y=lagrange(x,pointx,pointy)
n=size(pointx,2);
L=ones(n,size(x,2));
if (size(pointx,2)~=size(pointy,2))
    fprintf(1, '\nERROR!\nPOINTX and POINTY must have the same number of elements\n');
    y=NaN;
else
    for i=1:n
        for j=1:n
            if (i~=j)
                L(i,:)=L(i,:).*(x-pointx(j))/(pointx(i)-pointx(j));
            end
        end
    end
end

y=0;

for i=1:n
    y=y+pointy(i)*L(i,:);
end
end
```

**Output:**





## MATLAB Experiment No – 10

**Name:** Amit Kumar Sahu

**Reg No:** 18MIS7250

**Aim:** To solve the system using Tridiagonal Method (Thomas Algorithm).

**Objective:** used to solve tridiagonal systems of equations

**Algorithm:**

```
Sub TriDiagonal_Matrix_Algorithm(N%, A#(), B#(), C#(), D#(), X#())
    Dim i%, W#
    For i = 2 To N
        W = A(i) / B(i - 1)
        B(i) = B(i) - W * C(i - 1)
        D(i) = D(i) - W * D(i - 1)
    Next i
    X(N) = D(N) / B(N)
    For i = N - 1 To 1 Step -1
        X(i) = (D(i) - C(i) * X(i + 1)) / B(i)
    Next i
End Sub
```

**MATLAB Code:**

```
%Solving Linear system by using Thomas algorithm /Tridiagonal system
clc;clear all;close all;
format 'short'
%%Triangularization
m=input('Enter the order of TDmatrix:=');%Choose any square matrix
m=4
% Lower diagonal element such that first entry is zero.
a=input('\n Enter the lower diagonal vector:=')%lower diagonal elements
a=[0 -1 -1 -1];
b=input('\n Enter the Main diagonal vector:=')%diagonal elements
b=[2.04 2.04 2.04 2.04];
% Upper diagonal element such that last entry is zero.
c=input('\n Enter the upper diagonal vector:=')%upperdiagonal elements
c=[-1 -1 -1 0];
d=input('Enter the right side vector:=')
d=[4.08 0.8 0.8 2.08];
alpha=zeros(1,m);
for i=1:m
    if i==1
        alpha(i)=b(i);
        beta(i)=d(i);
    else
        ivalue=i
        alpha(i)=b(i)-(a(i)/alpha(i-1))*c(i-1);
        beta(i)=d(i)-(a(i)/alpha(i-1))*beta(i-1);
    end
end
```

```

    end
end
alpha
beta
%% Back substitution
x=zeros(1,m);
for i=m:-1:1
    if i==m
        x(i)=beta(i)/alpha(i);
    else
        x(i)=(beta(i)-c(i)*x(i+1))/alpha(i);
    end
end
x

```

### Output:

Enter the order of TDmatrix:=

5

Enter the lower diagonal vector:=

[0 1 1 1 1]

a =

0      1      1      1      1

Enter the Main diagonal vector:=

[-2 -2 -2 -2 -2]

b =

-2      -2      -2      -2      -2

Enter the upper diagonal vector:=

[1 1 1 1 0]

c =

1      1      1      1      0

Enter the right side vector:=

[1;0;0;0;0]

d =

1  
0  
0  
0  
0

ivalue =

2

ivalue =

3

ivalue =

4

ivalue =

5

alpha =

-2.0000   -1.5000   -1.3333   -1.2500   -1.2000

beta =

|        |        |        |        |        |
|--------|--------|--------|--------|--------|
| 1.0000 | 0.5000 | 0.3333 | 0.2500 | 0.2000 |
|--------|--------|--------|--------|--------|

x =

|         |         |         |         |         |
|---------|---------|---------|---------|---------|
| -0.8333 | -0.6667 | -0.5000 | -0.3333 | -0.1667 |
|---------|---------|---------|---------|---------|

## MATLAB Experiment No – 11

**Name:** Amit Kumar Sahu

**Reg No:** 18MIS7250

**Aim:** To solve the system of equation using Trapezoidal rule.

**Objective:** approximating the definite integral.

**Algorithm:**

$$\int_a^b f(x) dx \approx \sum_{k=1}^N \frac{f(x_{k-1}) + f(x_k)}{2} \Delta x_k = \frac{\Delta x}{2} (f(x_0) + 2f(x_1) + 2f(x_2) + 2f(x_3) + 2f(x_4) + \cdots + 2f(x_{N-1}) + f(x_N)).$$

**MATLAB Code:**

```
clc;
clear all;
f=@(x)cosh(x);
% create a handle to the function f with an @ sign.
a=input('Enter lower limit a: ');
b=input('Enter upper limit b: ');
n=input('Enter the no. of subinterval: ');
h=(b-a)/n;
sum=0;
for k=1:1:n-1
    x(k)=a+k*h;
    y(k)=f(x(k));
    sum=sum+y(k);
end
% Formula: (h/2)*[(y0+yn)+2*(y2+y3+..+yn-1)]
answer=(h/2)*(f(a)+f(b)+2*sum);
fprintf('\n The value of integration is %f',answer);
```

**Output:**

Enter lower limit a:

0

Enter upper limit b:

2

Enter the no. of subinterval:

4

The value of integration is 3.702107

## MATLAB Experiment No – 12

**Name:** Amit Kumar Sahu

**Reg No:** 18MIS7250

**Aim:** To solve the system using Simpson's 1/3<sup>rd</sup> Rule

**Objective:** approximations for definite integrals

**Algorithm:**

$$\int_a^b f(x) dx \approx \frac{b-a}{6} \left[ f(a) + 4f\left(\frac{a+b}{2}\right) + f(b) \right].$$

**MATLAB Code:**

```
clc;
clear all;
f=@(x)cosh(x); %Change here for different function
a=input('Enter lower limit a: ');
b=input('Enter upper limit b: ');
n=input('Enter the number of sub-intervals n: ');
h=(b-a)/n;
if rem(n,2)==1
    fprintf('\n Enter valid n!!!');
    n=input('\n Enter n as even number ');
end
for k=1:1:n
    x(k)=a+k*h;
    y(k)=f(x(k));
end
so=0;se=0;
for k=1:1:n-1
    if rem(k,2)==1
        so=so+y(k);%sum of odd terms
    else
        se=se+y(k); %sum of even terms
    end
end
% Formula: (h/3)*[(y0+yn)+2*(y3+y5+..odd term)+4*(y2+y4+y6+...even terms)]
answer=h/3*(f(a)+f(b)+4*so+2*se);
fprintf('\n The value of integration is %f',answer); % exmple The value of
integration is 0.408009
```

**Output:**

1

Enter upper limit b:

2

Enter the number of sub-intervals n:

16

The value of integration is 2.451659