

CENG 789 – Digital Geometry Processing

14- Main DGP Tasks in a Nutshell

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Shape/Mesh Processing Tasks

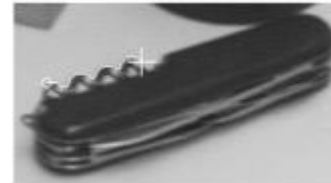
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- ✓ Already covered some important tasks (check out previous lectures).
 - ✓ Shape descriptors, generation, reconstruction, registration.
 - ✓ Mesh deformation, parameterization, remeshing, repairing.
- ✓ Talk about some other prominent tasks today.
 - ✓ Shape segmentation.
 - ✓ Shape representation/approximation.
 - ✓ Shape correspondence.
 - ✓ Shape retrieval.
 - ✓ Groupwise alignment.
 - ✓ Human-centric shape analysis (indirect).
 - ✓ Shape interpolation/morphing.
 - ✓ Scene synthesis and labeling.
 - ✓ Slides in the sequel represent Potential Project Topics.

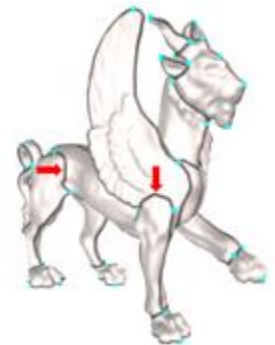
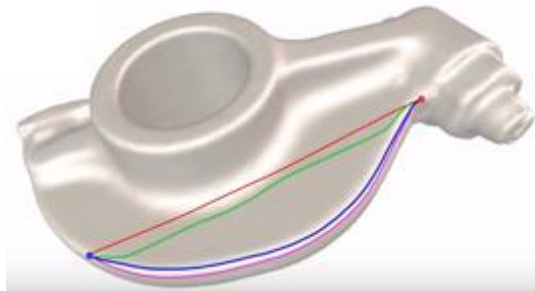
Shape Segmentation

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- ✓ User-guided shape segmentation.
 - ✓ Live-wire interaction (well-known in image processing).



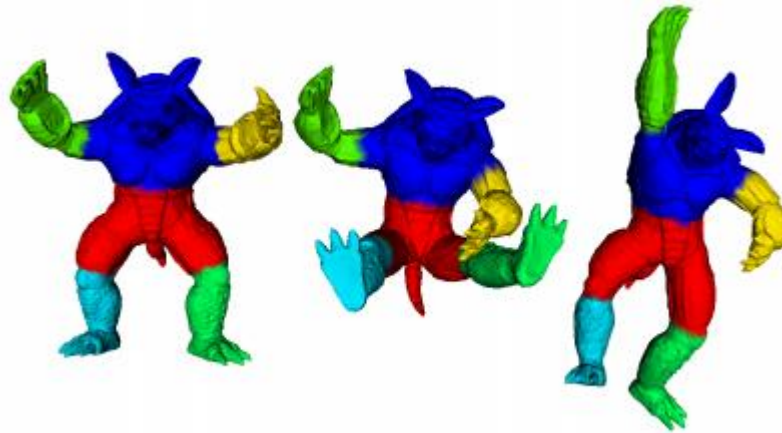
- ✓ <https://www.youtube.com/watch?v=XRj8AFIkZfY>



Shape Segmentation

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- ✓ Fully-automatic shape segmentation.

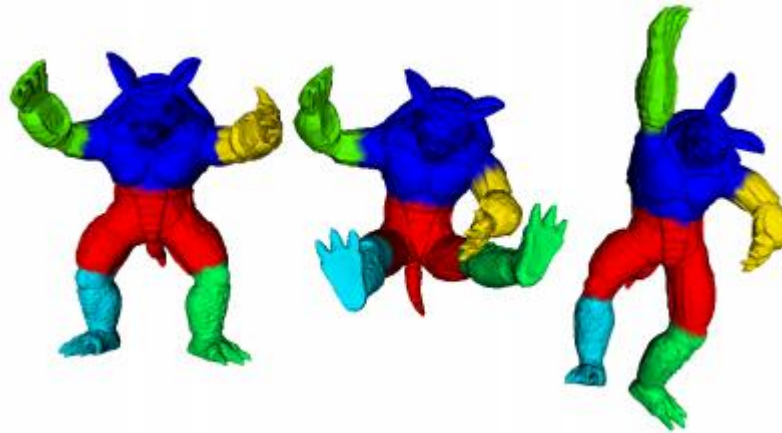


- ✓ Shape representation: MDS.
- ✓ Followed by k-means clustering algorithm.

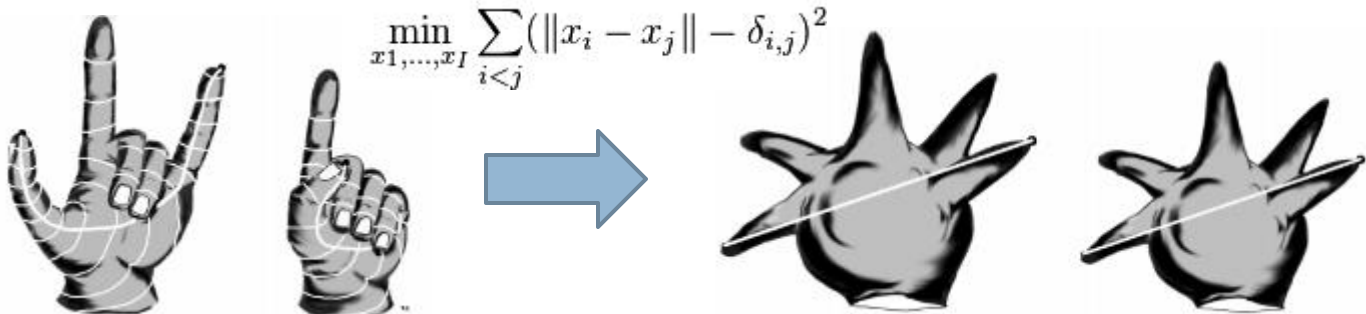
Shape Segmentation

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- ✓ Fully-automatic shape segmentation.



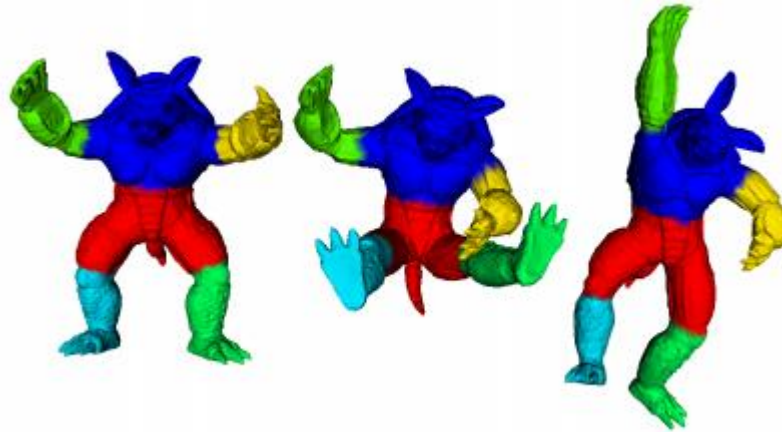
- ✓ Shape representation: MDS (bending-invariant).



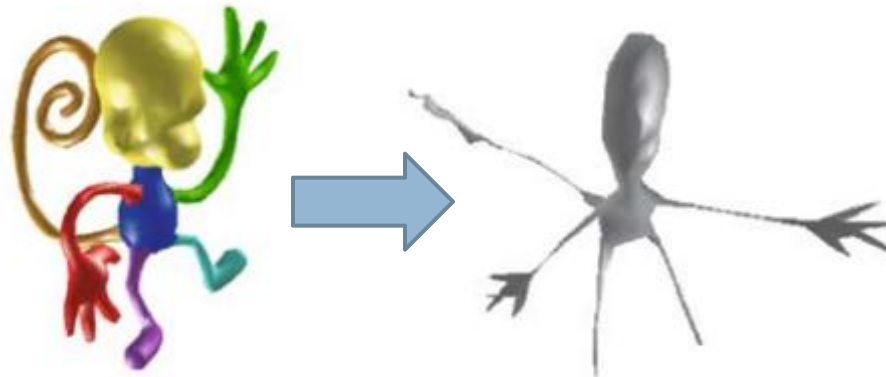
Shape Segmentation

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- ✓ Fully-automatic shape segmentation.



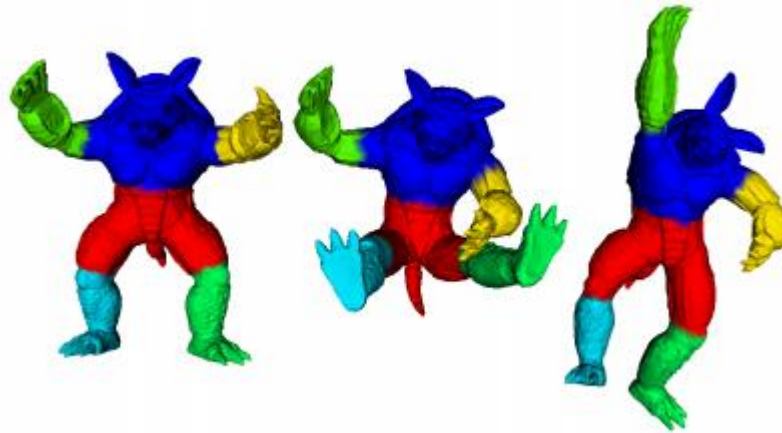
- ✓ Shape representation: MDS (bending-invariant).



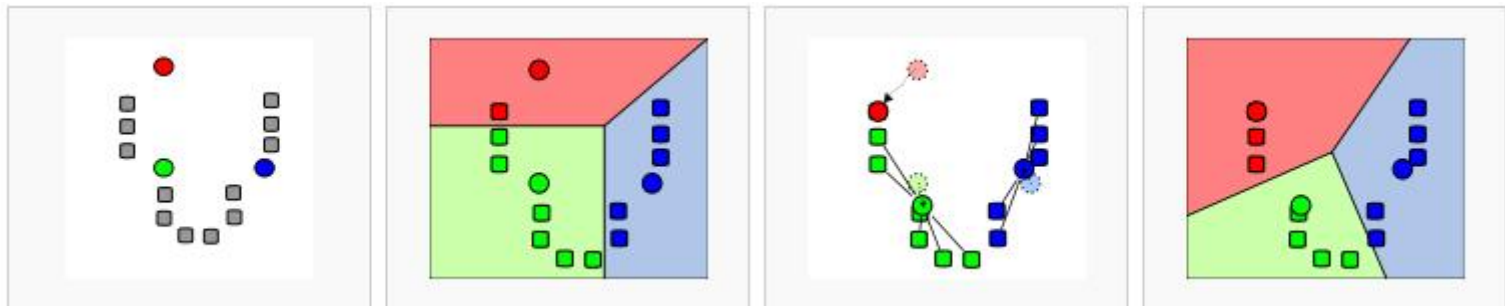
Shape Segmentation

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- ✓ Fully-automatic shape segmentation.



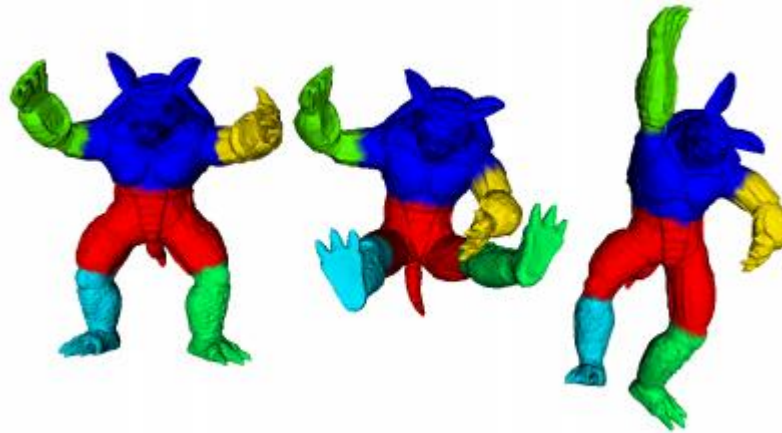
- ✓ K-means clustering.



Shape Segmentation

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- ✓ Fully-automatic shape segmentation.



- ✓ More sophisticated data-driven segmentation methods exist.

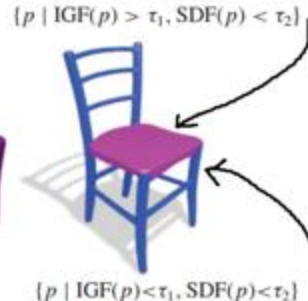
- ✓ Hierarchical decomposition.
- ✓ Randomized cuts.
- ✓ Core extraction.
- ✓ Fitting primitives.
- ✓ Shape diameter function (SDF).
- ✓ Intrinsic girth function (IGF).



IGF



SDF



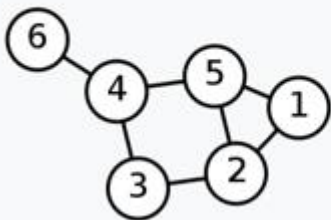
$\{p \mid \text{IGF}(p) > \tau_1, \text{SDF}(p) < \tau_2\}$

$\{p \mid \text{IGF}(p) < \tau_1, \text{SDF}(p) < \tau_2\}$

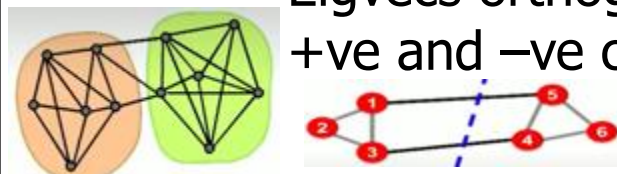
Shape Segmentation

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- ✓ Fully-automatic shape segmentation via spectral clustering.
- ✓ Spectrum (eigvals) of a matrix, the Laplacian Matrix = Degree – Adj.

Labelled graph	Degree matrix	Adjacency matrix	Laplacian matrix
	$\begin{pmatrix} 2 & 0 & 0 & 0 & 0 & 0 \\ 0 & 3 & 0 & 0 & 0 & 0 \\ 0 & 0 & 2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 3 & 0 & 0 \\ 0 & 0 & 0 & 0 & 3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 & 0 & 0 & 1 & 0 \\ 1 & 0 & 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 1 & 1 \\ 1 & 1 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \end{pmatrix}$	$\begin{pmatrix} 2 & -1 & 0 & 0 & -1 & 0 \\ -1 & 3 & -1 & 0 & -1 & 0 \\ 0 & -1 & 2 & -1 & 0 & 0 \\ 0 & 0 & -1 & 3 & -1 & -1 \\ -1 & -1 & 0 & -1 & 3 & 0 \\ 0 & 0 & 0 & -1 & 0 & 1 \end{pmatrix}$

- ✓ $Lx = 0$ for all const vectors, e.g., $x = [1 \ 1 \dots 1]^T$. Eigval = 0, eigvec = c.
- ✓ 2nd smallest eigval is more useful; it comes with the Fiedler eigenvector.
- ✓ This eigval/vec, call it x_2 , approximates the sparsest cut of a graph.
 - ✓ Eigvecs orthogonal: x_1 is constant, so to make dot product 0, x_2 has +ve and -ve components. These 2 sets of components are clusters.



- ✓ Not directly applicable to Mesh Segmentation as mesh graph is regular.

Shape Segmentation

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- ✓ Why segment? Once you have the parts, you can go wild, e.g., collage



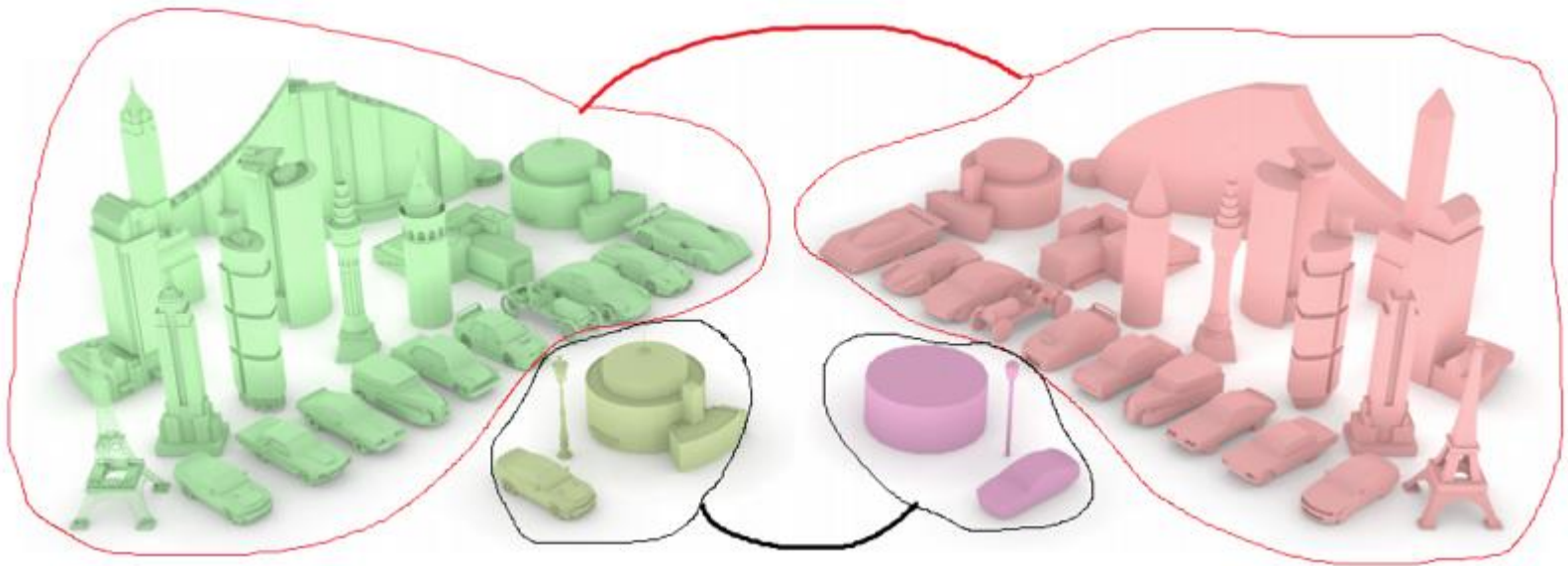
- ✓ Collection understanding through part-level correspondences, ..



Shape Approximation

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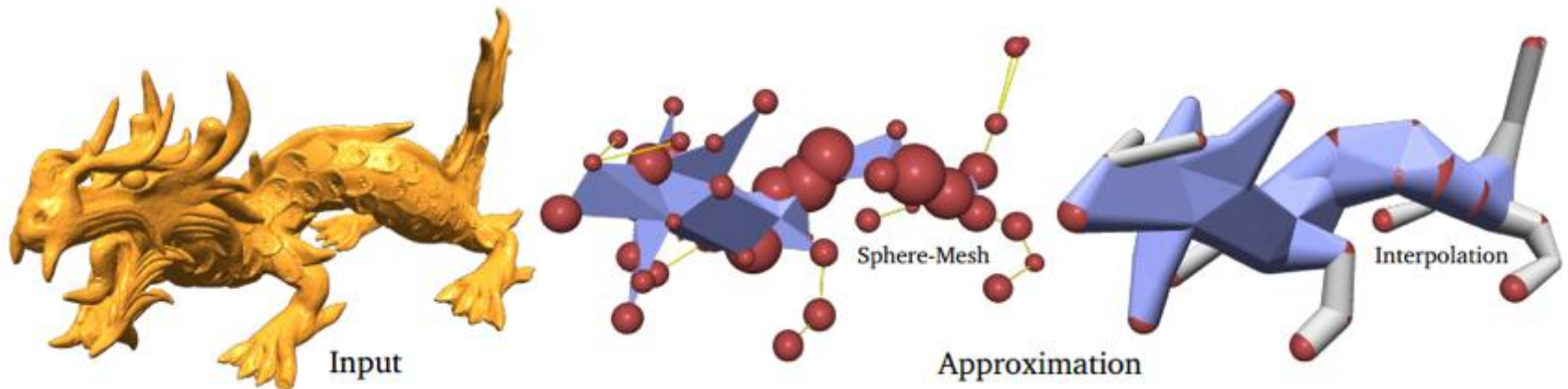
- ✓ Computing simple geometric descriptions for dense surfaces.
 - ✓ Mesh decimation (minimal elements; already covered).
 - ✓ Mesh decimation based on context. See https://youtu.be/62_1CQirnzM



Shape Approximation

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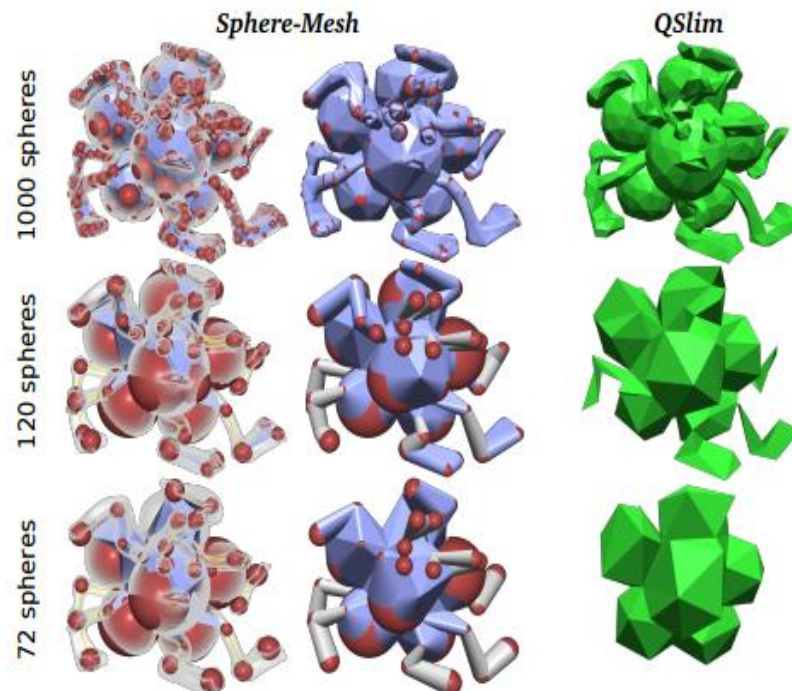
- ✓ Computing simple geometric descriptions for dense surfaces.
 - ✓ Mesh decimation (minimal elements; already covered).
 - ✓ Mesh decimation based on volume.
 - ✓ At extreme simplification levels, model the volumetric extent of the original shape. See <https://youtu.be/Jz09SAeBWIO>



Shape Approximation

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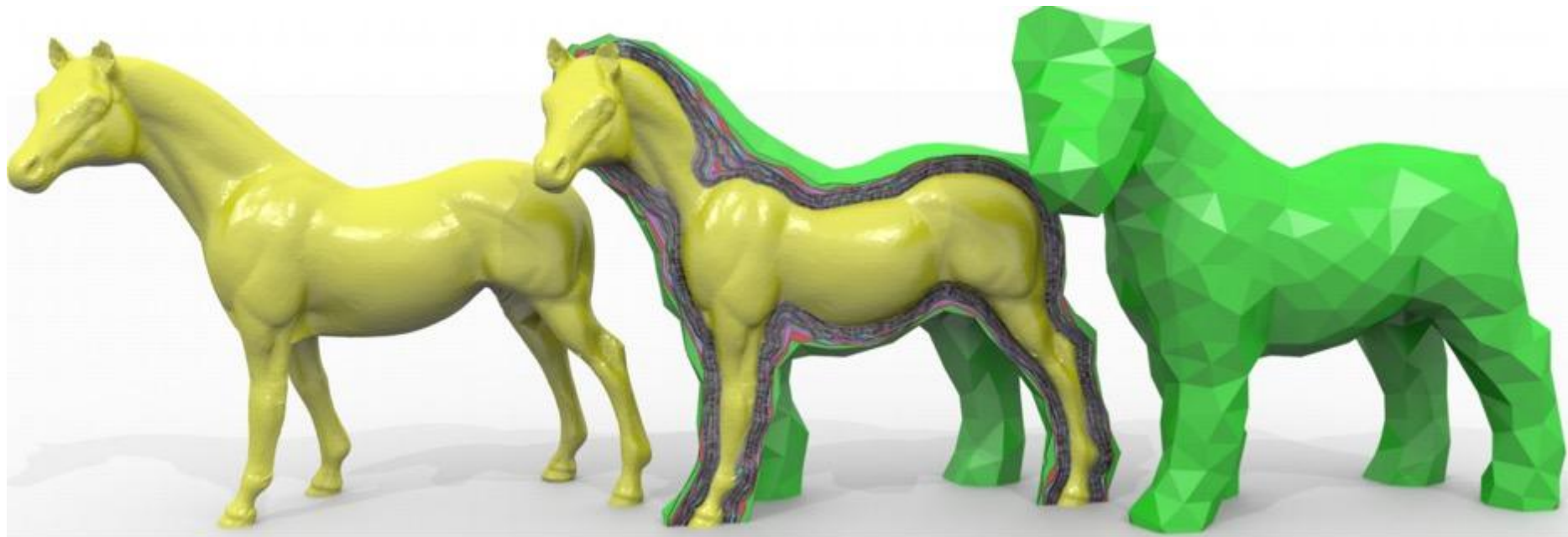
- ✓ Computing simple geometric descriptions for dense surfaces.
 - ✓ Mesh decimation (minimal elements; already covered).
 - ✓ Mesh decimation based on volume.
 - ✓ Sphere interpolation replacing classic point interpolation.



Shape Approximation

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- ✓ Computing simple geometric descriptions for dense surfaces.
 - ✓ Mesh decimation (minimal elements; already covered).
 - ✓ Mesh decimation based on level.
 - ✓ Nested cages for faster collision detection and deformation.



Shape Approximation

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- ✓ Computing simple geometric descriptions for dense surfaces.
 - ✓ Mesh decimation (minimal elements; already covered).
 - ✓ Mesh decimation based on level.
 - ✓ Nested cages. Shrink, re-inflate. See https://youtu.be/tTEGDPhv_AI



Shape Approximation

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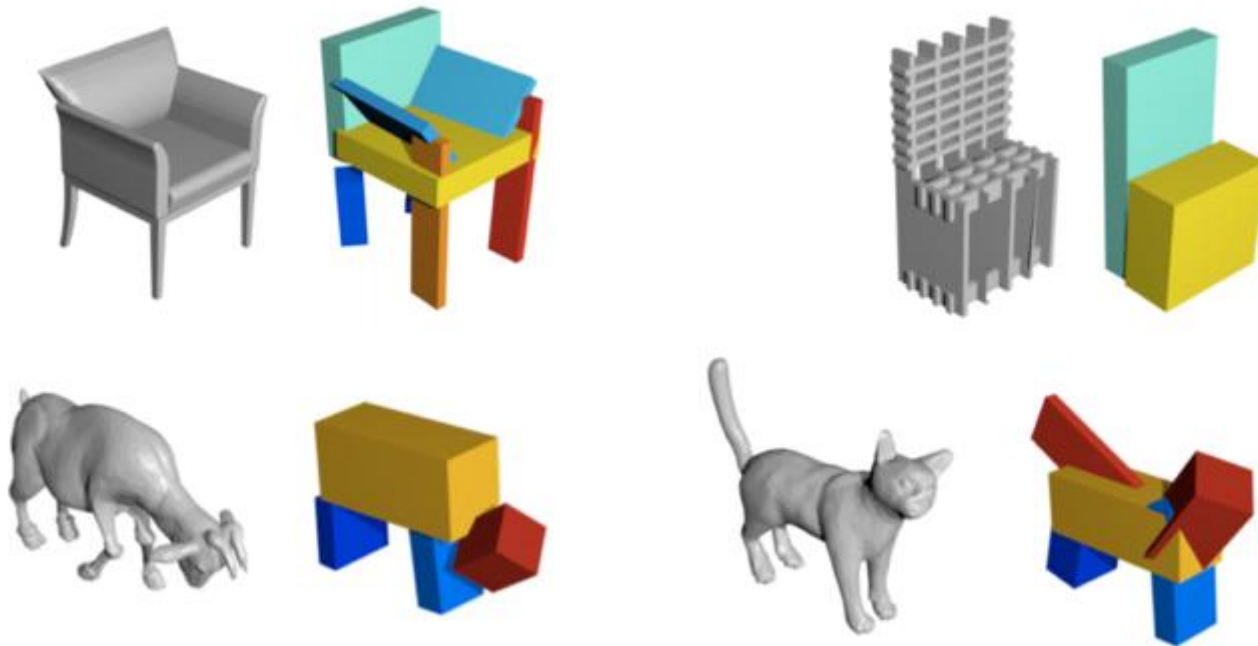
- ✓ Computing simple geometric descriptions for dense surfaces.
 - ✓ Mesh decimation (minimal elements; already covered).
 - ✓ Mesh decimation based on level.
 - ✓ Nested cages. Shrink, re-inflate. See https://youtu.be/tTEGDPHv_AI
 - ✓ Cage-based deformations. Read
 - ✓ Spatial Deformation Transfer. <https://youtu.be/ayeKIItDliUc>
 - ✓ Embedded Deformation. <https://youtu.be/BEEN7Dmo9vI>



Shape Approximation

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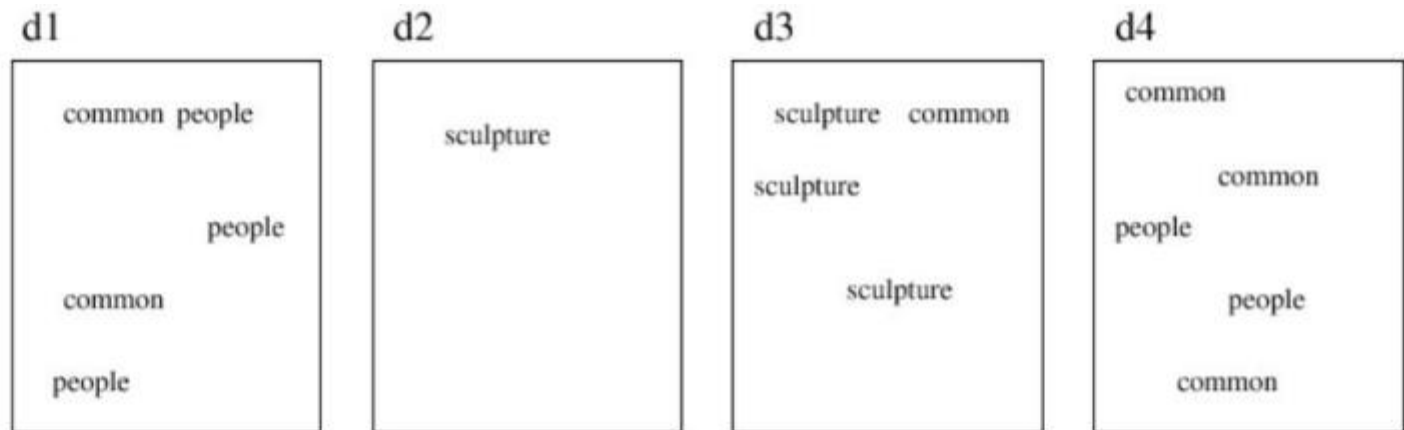
- ✓ Computing simple geometric descriptions for dense surfaces.
- ✓ Assemble of volumetric primitives.



Shape Representation

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- ✓ Computing simple geometric descriptions for dense surfaces.
 - ✓ Bag-of-words (bag-of-features) shape representation.



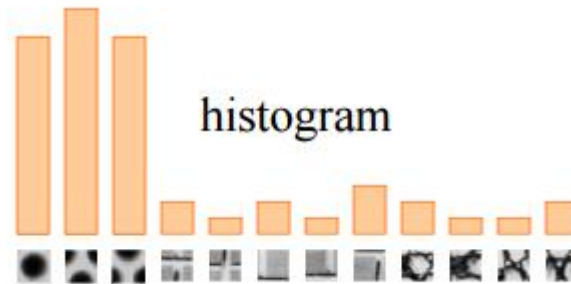
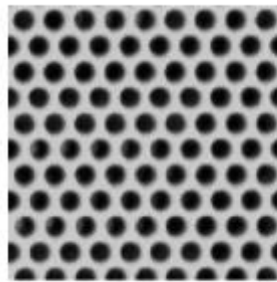
Bag-of-words

Common	2	0	1	3
People	3	0	0	2
Sculpture	0	1	3	0
...

Shape Representation

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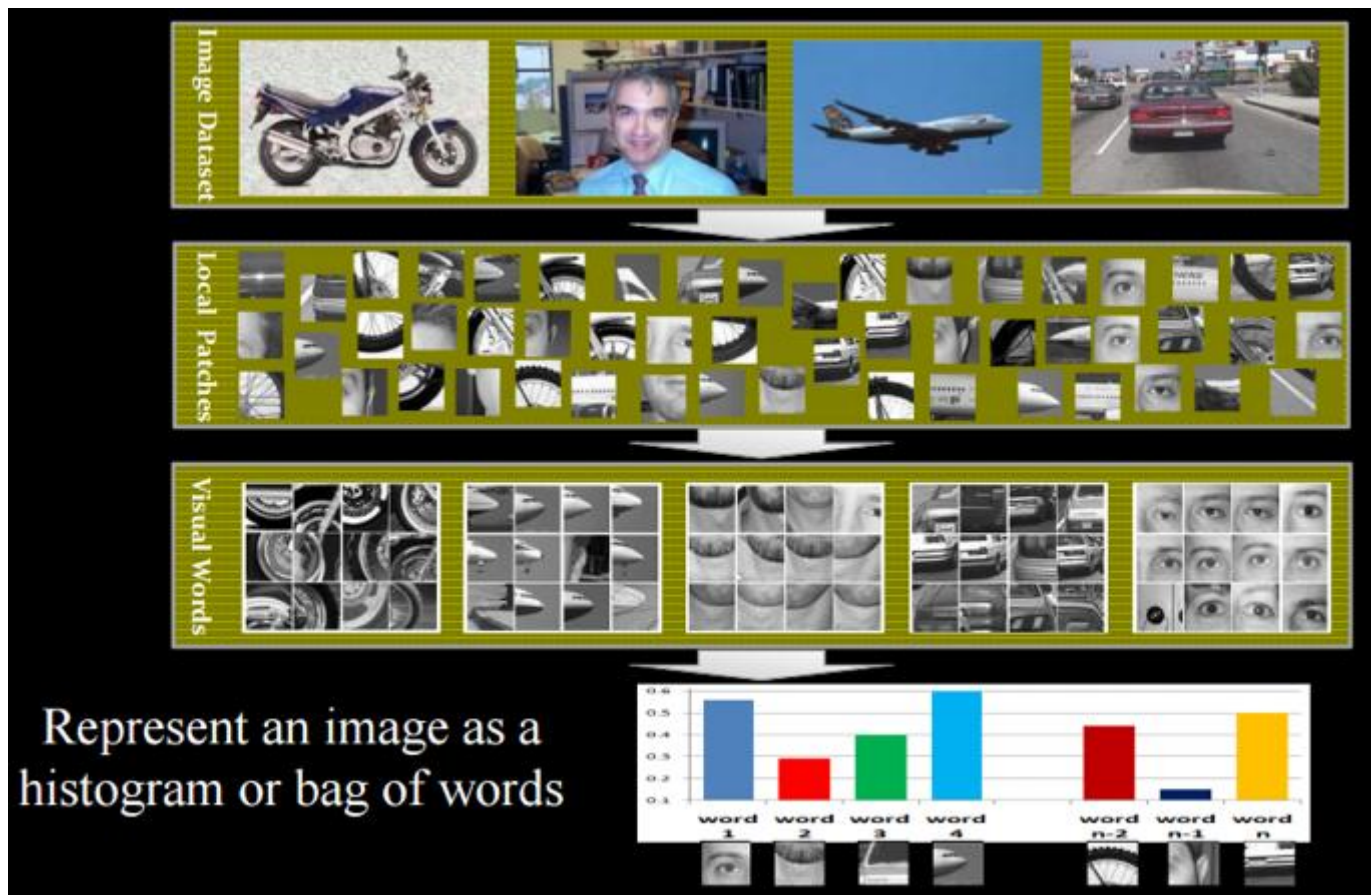
- ✓ Computing simple geometric descriptions for dense surfaces.
 - ✓ Bag-of-words (bag-of-features) shape representation.
 - ✓ Need a visual vocabulary for shape (not text) processing.



Shape Representation

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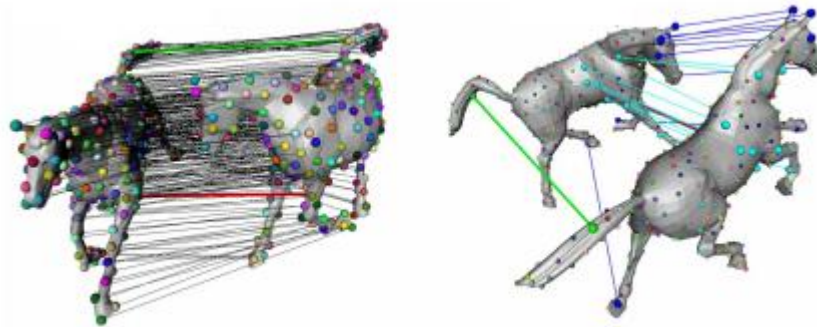
- ✓ Computing simple geometric descriptions for dense surfaces.
- ✓ Bag-of-words (bag-of-features) shape representation.



Shape Correspondence

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- ✓ Define a map-distortion function that quantifies how good a given map is.
- ✓ Combinatorial search on space of maps.
 - ✓ Use the map minimizing the distortion function.



Shape Correspondence

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- ✓ Define a map-distortion function that quantifies how good a given map is. Many variants in the literature; see
 - ✓ Coarse-to-Fine Combinatorial Matching For Dense Isometric Shape Correspondence (C2FCM)
 - ✓ Scale Normalization for Isometric Shape Matching
 - ✓ Non-rigid registration under isometric deformations
 - ✓ Blended intrinsic maps
 - ✓ Generalized multidimensional scaling
- ✓ Cast the problem as matching between function values, not points: Functional Maps (not covered here).
 - ✓ By the author: <https://youtu.be/l9pqyo85nFE?t=884>
 - ✓ A good function. Laplace-Beltrami eigenfunctions: <https://youtu.be/CpdJVCXQte4?t=502>

Isometric Distortion

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- ✓ Given $\xi : S \rightarrow T$, measure its isometric distortion (from C2FCM):

$$D_{\text{iso}}(\xi) = \frac{1}{|\xi|} \sum_{(s_i, t_j) \in \xi} d_{\text{iso}}(s_i, t_j)$$

$$d_{\text{iso}}(s_i, t_j) = \frac{1}{|\xi'|} \sum_{(s_l, t_m) \in \xi'} |g(s_i, s_l) - g(t_j, t_m)|$$

$\xi' = \xi - \{(s_i, t_j)\}$ in the most general setting.

$g(.,.)$: normalized geodesic distance b/w two vertices.

- ✓ $O(N^2)$ for a map of size N .

Isometric Distortion Illustration

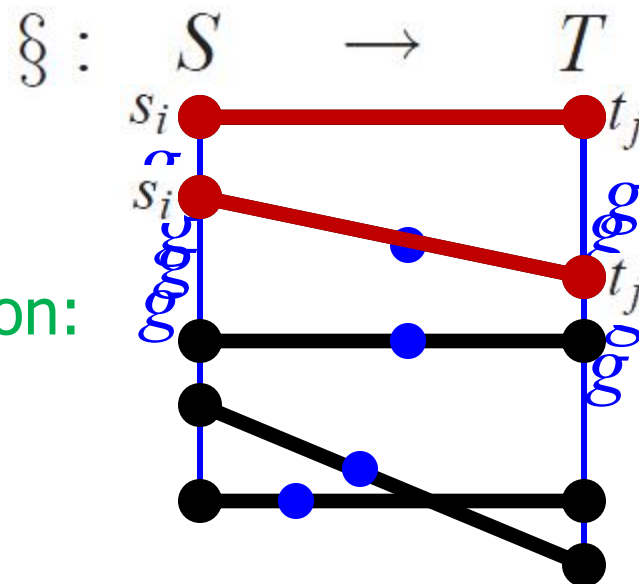
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$$D_{\text{iso}}(\xi) = \frac{1}{|\xi|} \sum_{(s_i, t_j) \in \xi} d_{\text{iso}}(s_i, t_j)$$

$$d_{\text{iso}}(s_i, t_j) = \frac{1}{|\xi'|} \sum_{(s_l, t_m) \in \xi'} |g(s_i, s_l) - g(t_j, t_m)|$$

$$\xi' = \xi - \{(s_i, t_j)\}$$

in action:

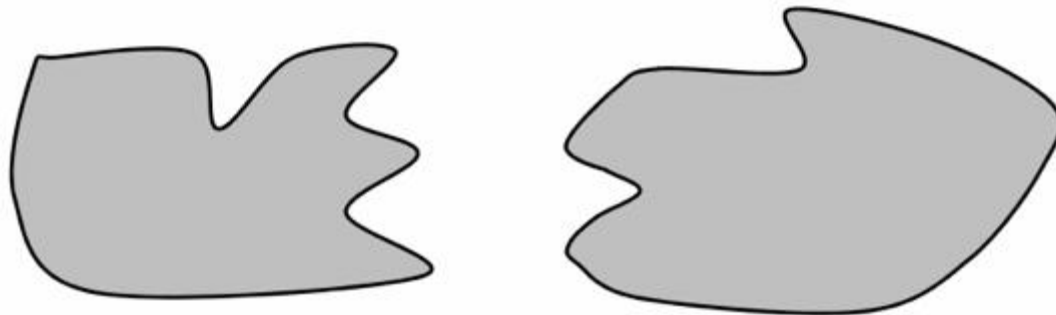


$$\left. \begin{array}{l} d_{\text{iso}}(s_i, t_j) = >0 + 0 + >0 + 0 \\ d_{\text{iso}}(s_i, t_j) = \dots \\ \vdots \end{array} \right\} \text{average for } D_{\text{iso}}(\xi).$$

Shape Correspondence

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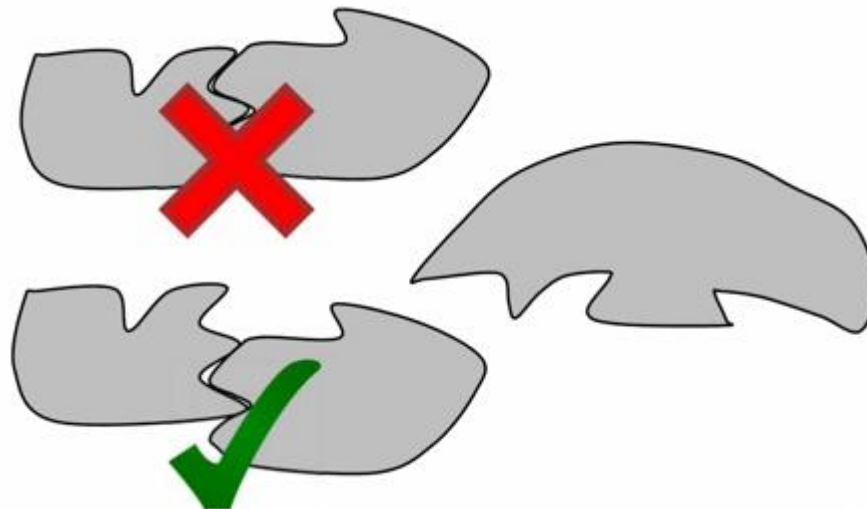
- ✓ Well-studied for isolated pair of X shapes.
- ✓ $X =$
 - ✓ Isometric or non-rigid
 - ✓ Rigid
 - ✓ Non-isometric
- ✓ At its infancy for collection analysis.
 - ✓ Use context info to improve results.



Shape Correspondence

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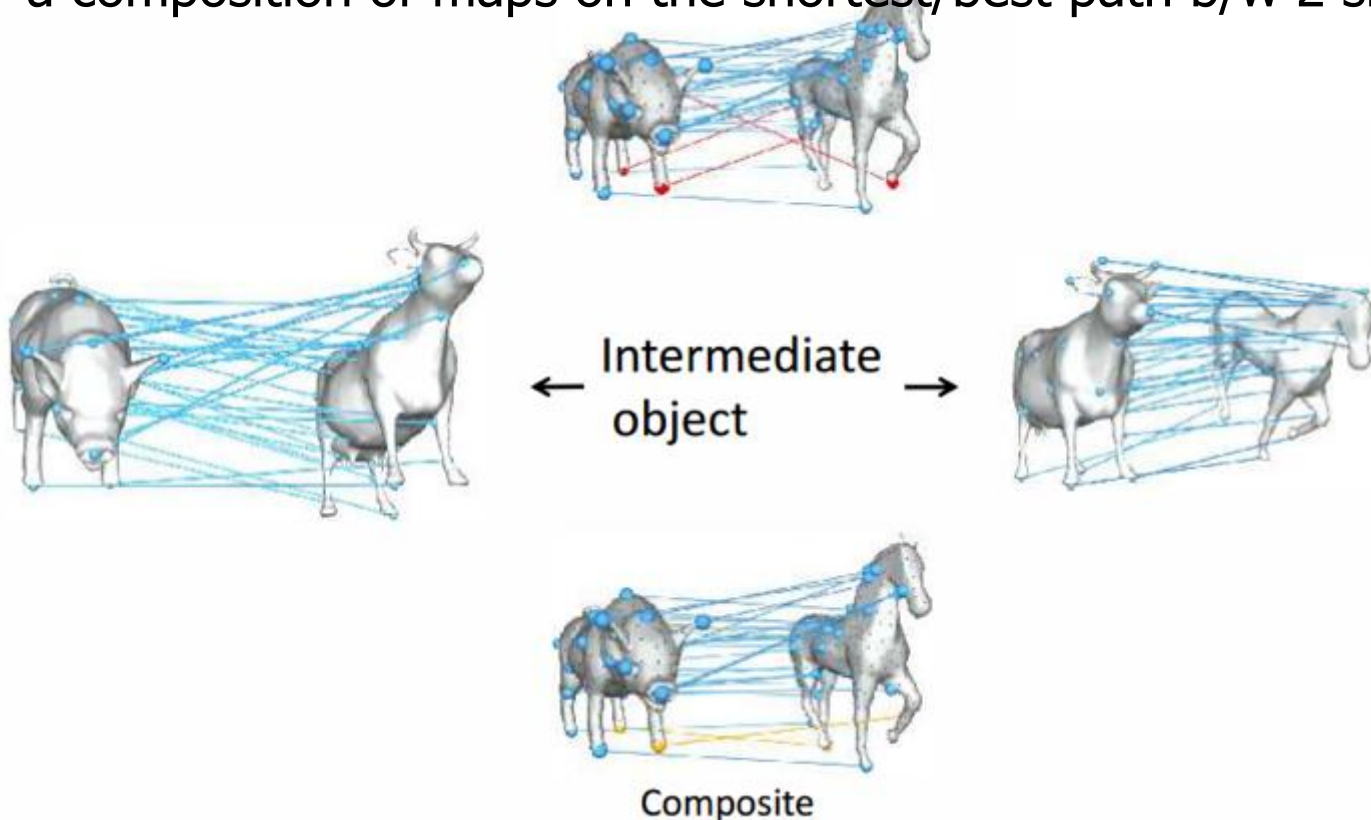
- ✓ Well-studied for isolated pair of X shapes.
- ✓ $X =$
 - ✓ Isometric or non-rigid
 - ✓ Rigid
 - ✓ Non-isometric
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Shape Correspondence

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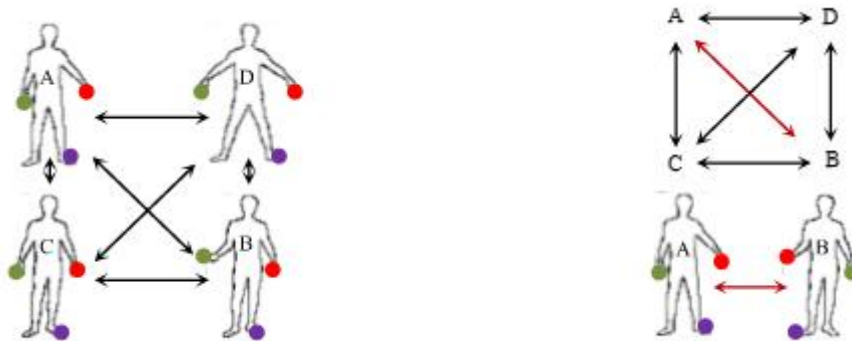
- ✓ At its infancy for collection analysis.
- ✓ Replace a (bad) map w/ a composition of (better) maps.
- ✓ = w/ a composition of maps on the shortest/best path b/w 2 shapes.



Shape Correspondence

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- ✓ At its infancy for collection analysis.
- ✓ Consistent (left) vs. inconsistent (right) maps.

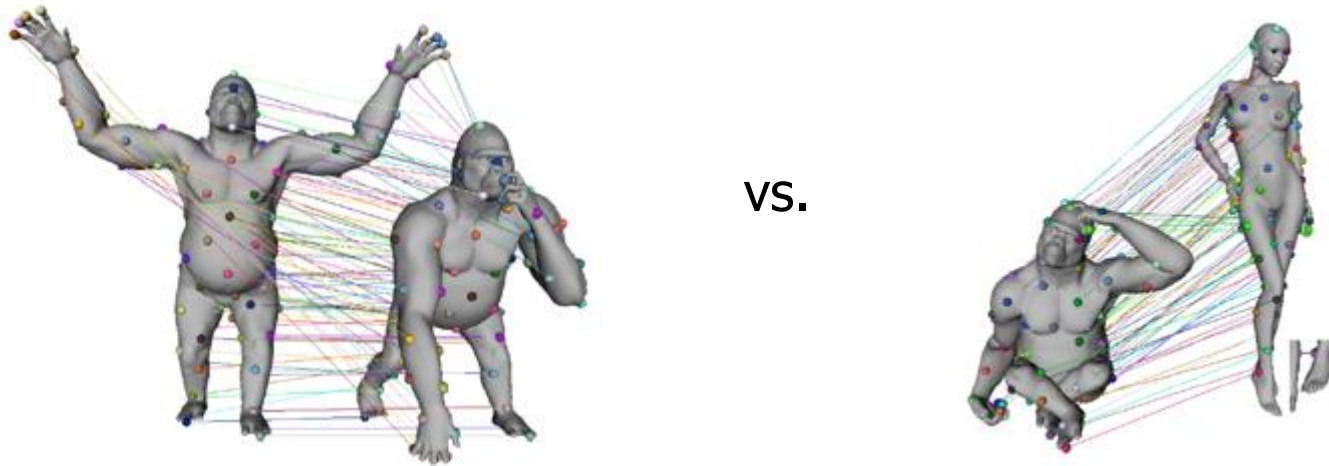


- ✓ Read
 - ✓ An optimization approach to improving collections of shape maps
 - ✓ Multiple shape correspondence by dynamic programming

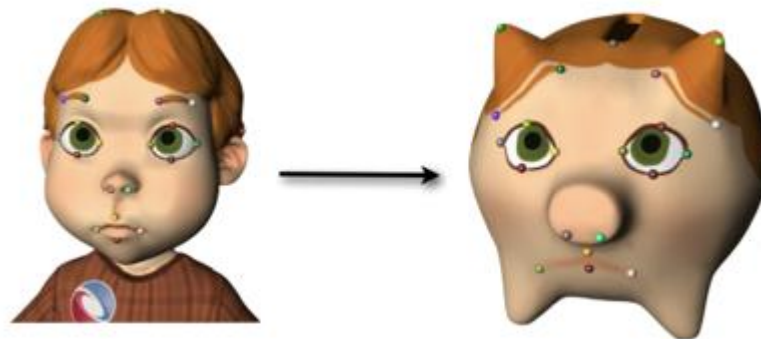
Shape Correspondence

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- ✓ Non-isometric case harder due to stretching.



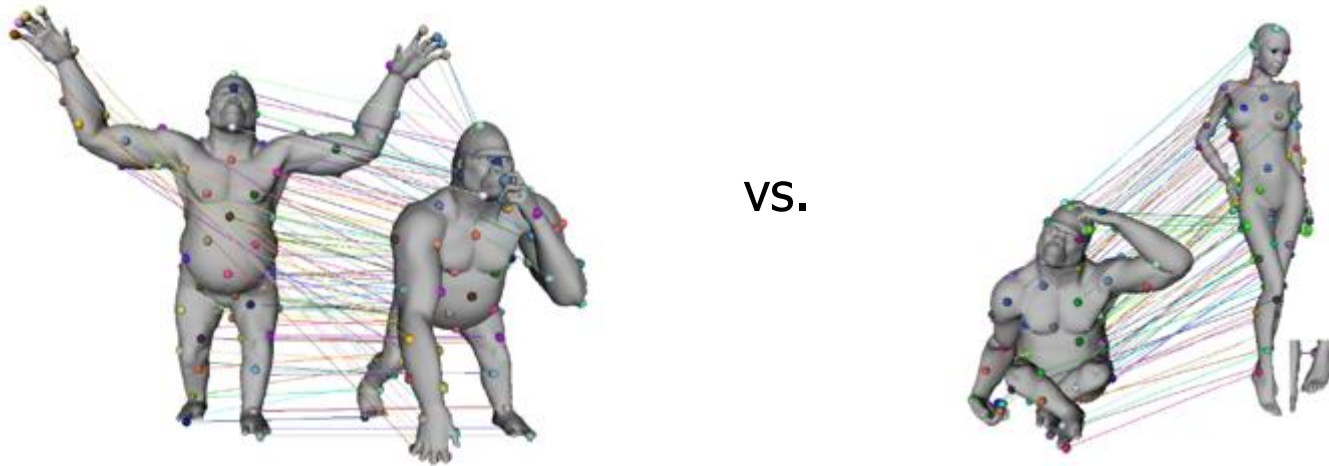
- ✓ Idea: Interpolate a few predefined correspondences on landmarks
 - ✓ Weighted averages on surfaces. See <https://youtu.be/tlMsB6tBO2w>



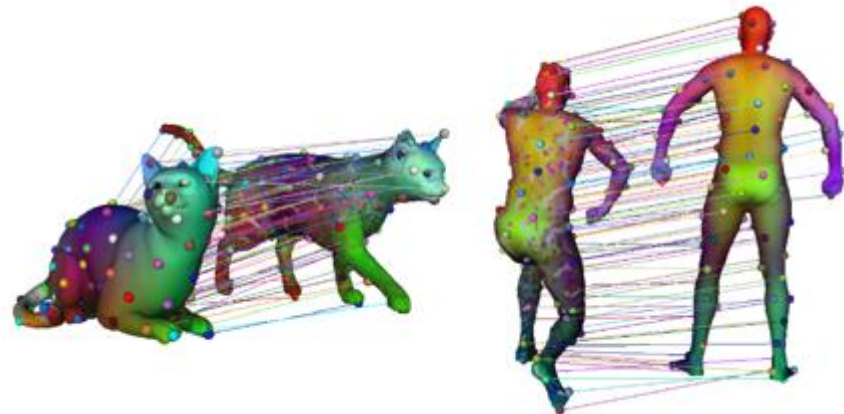
Shape Correspondence

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- ✓ Non-isometric case harder due to stretching.



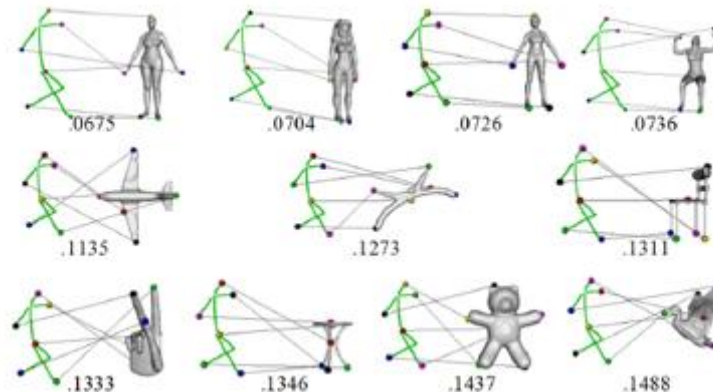
- ✓ Idea: Interpolate a few predefined correspondences on landmarks
 - ✓ Blended intrinsic maps.
 - ✓ Non-smooth blend:



Shape Retrieval

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- ✓ Query-by-text.
 - ✓ Google search.
 - ✓ Shape adaptation: DB needs to be manually tagged ☹
- ✓ Query-by-example.
 - ✓ Shape adaptation: User provides a 3D model; popular but hard to come up with a 3D model ☹.
- ✓ Query-by-sketch.
 - ✓ Shape adaptation: User simply draws; easy for user but not so accurate due to view and drawing differences ☹.
 - ✓ Articulated:



Shape Retrieval

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- ✓ Query-by-text.
 - ✓ Google search.
 - ✓ Shape adaptation: DB needs to be manually tagged ☹
- ✓ Query-by-example.
 - ✓ Shape adaptation: User provides a 3D model; popular but hard to come up with a 3D model ☹.
- ✓ Query-by-sketch.
 - ✓ Shape adaptation: User simply draws; easy for user but not so accurate due to view and drawing differences ☹.
 - ✓ Non-articulated: See <https://youtu.be/IVszERiVaJI>



Shape Retrieval

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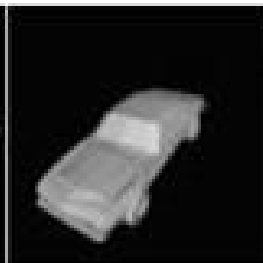
- ✓ Index database models with
 - ✓ Features.
 - ✓ Bending-invariant representations.
 - ✓ Bag-of-words.
 - ✓ ..
- ✓ Convert to query model into that index.
 - ✓ Retrieve the most compatible model according to the indexing.



1.00



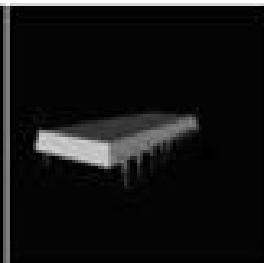
0.90



0.88



0.85



0.85

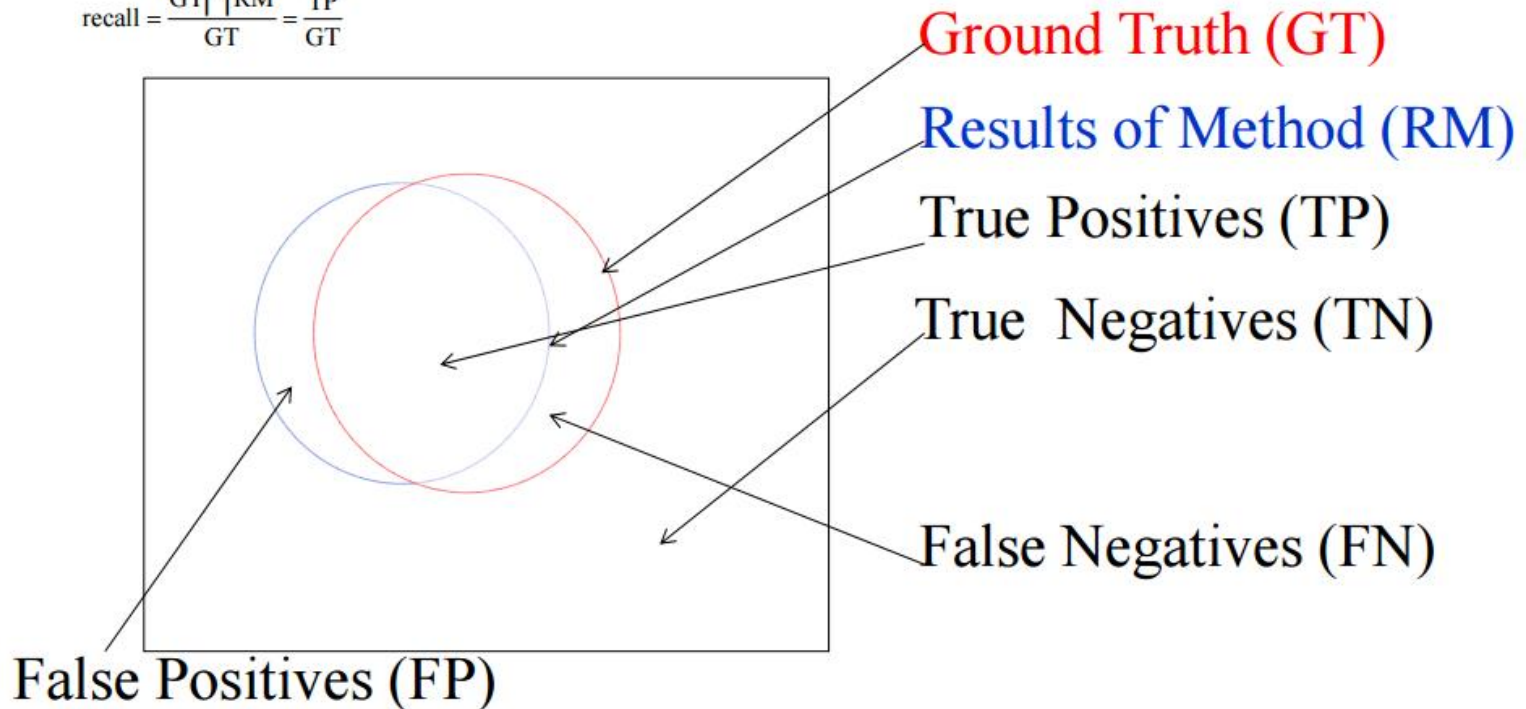
Shape Retrieval

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- ✓ Evaluation of shape retrieval performance.
- ✓ Precision-recall plots.

$$\text{precision} = \frac{GT \cap RM}{RM} = \frac{TP}{RM}$$

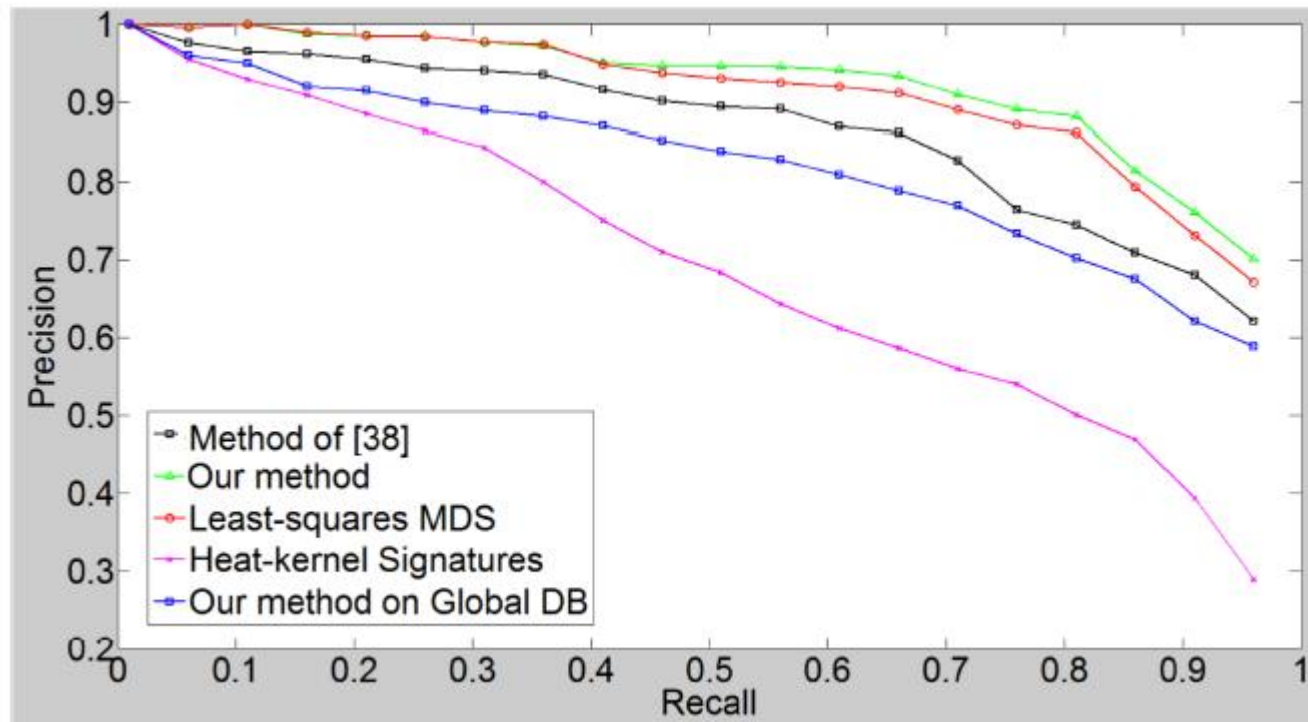
$$\text{recall} = \frac{GT \cap RM}{GT} = \frac{TP}{GT}$$



Shape Retrieval

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- ✓ Evaluation of shape retrieval performance.
- ✓ Precision-recall plots.
 - ✓ Ideally this curve should be a horizontal line at unit precision.



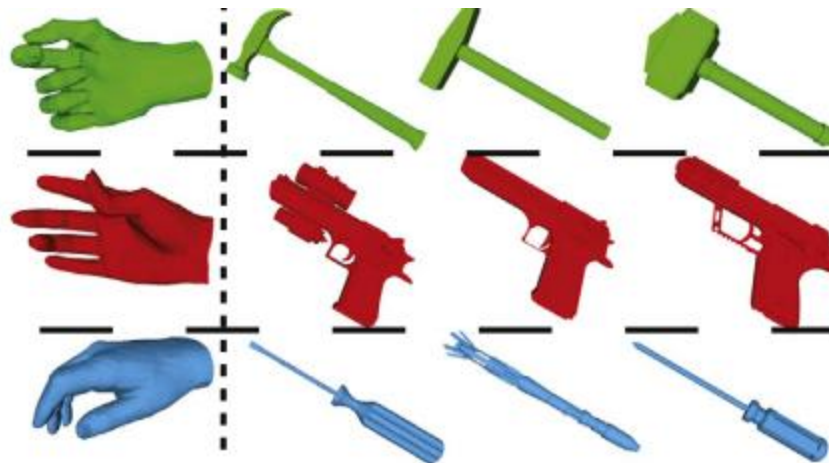
Human-centric Shape Analysis

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- ✓ Recognize/classify/segment objects based on their interaction with human agents.
 - ✓ Human body.



- ✓ Human hand.

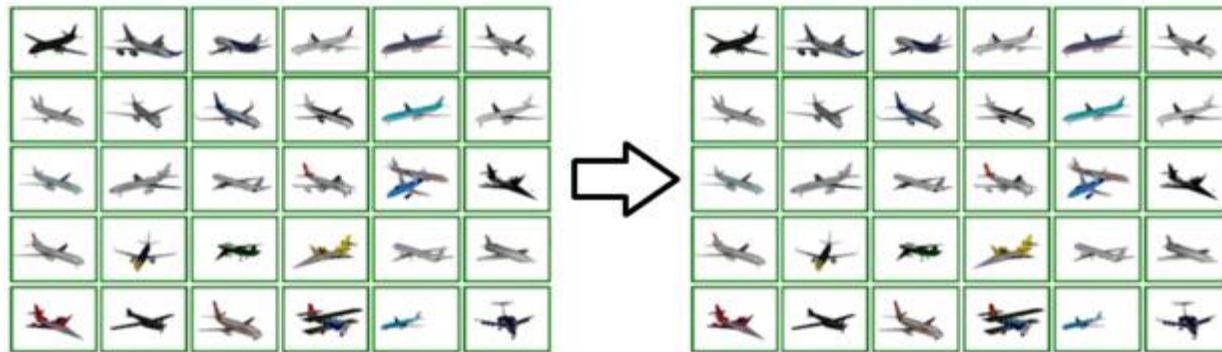


- ✓ ..

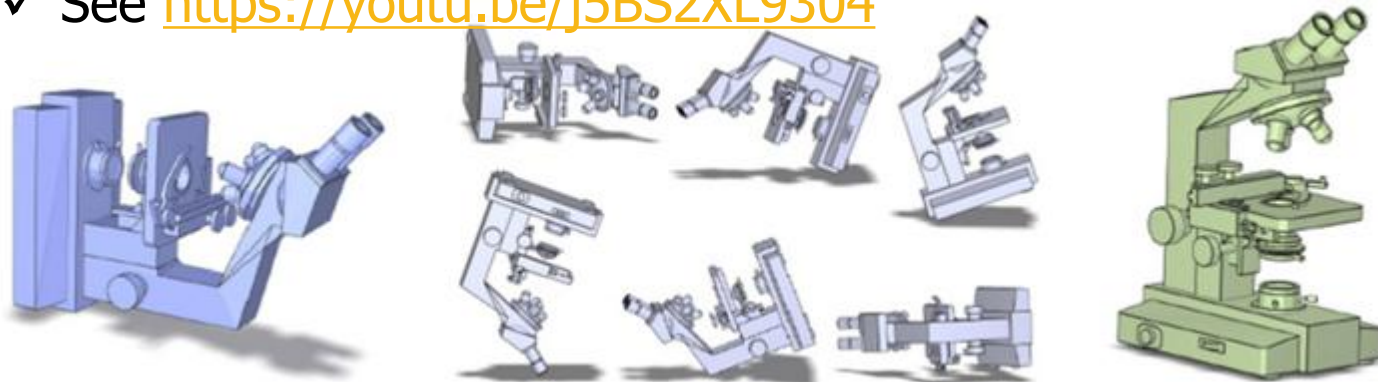
Groupwise Shape Alignment

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- ✓ Make every shape in collection look right.
 - ✓ See <https://youtu.be/m584yqGtlCE>



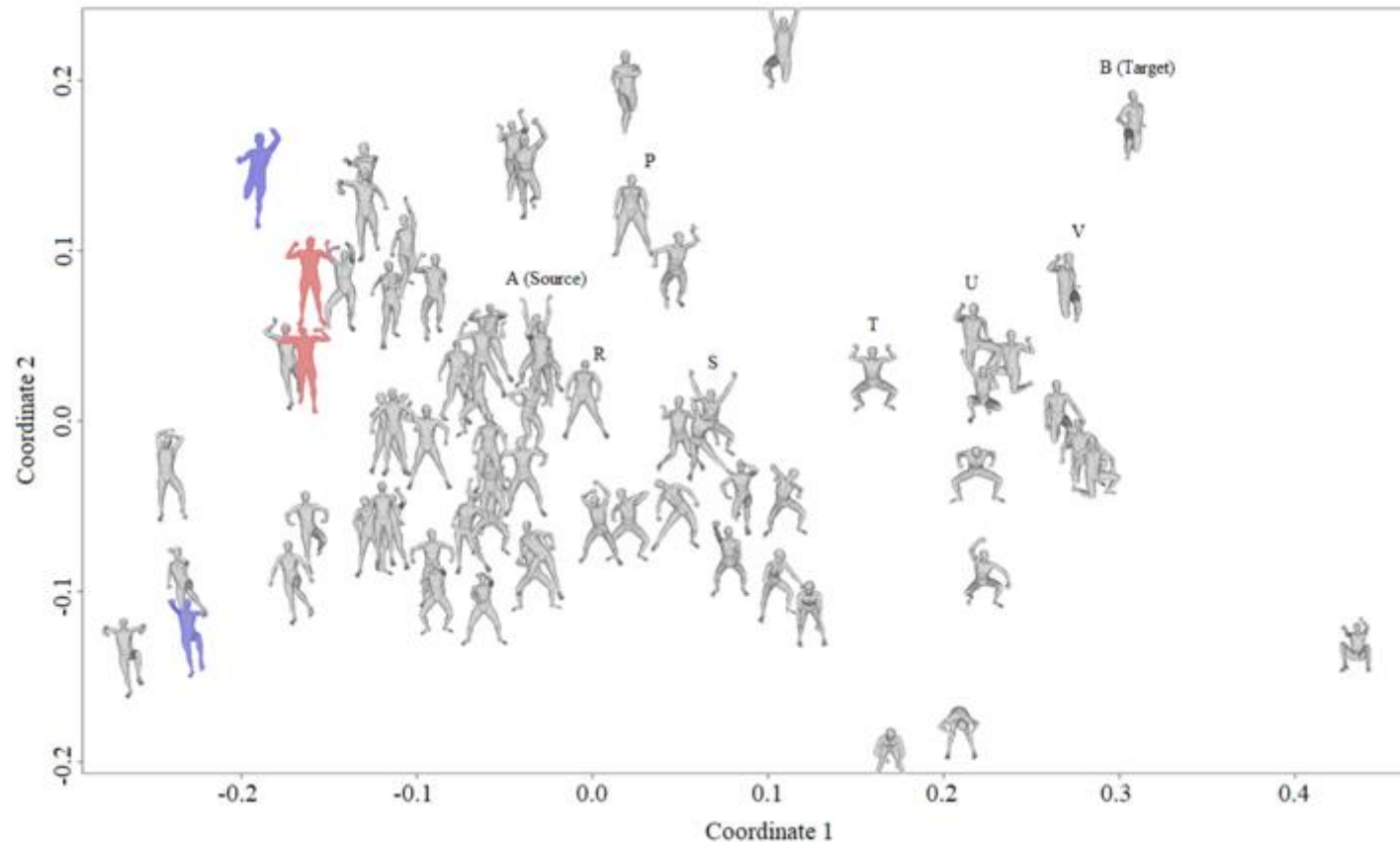
- ✓ Put every shape in collection in upright orientation.
 - ✓ See <https://youtu.be/j5BS2XL9304>



Shape Interpolation

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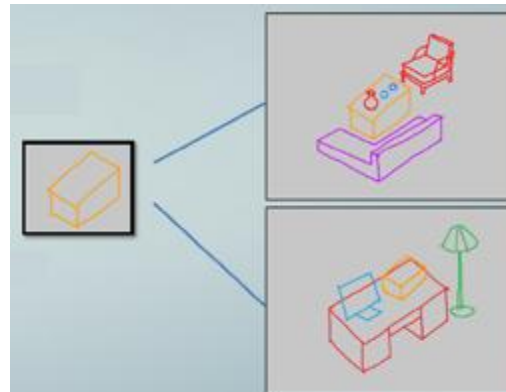
- ✓ Instead of interpolating directly from A to B, create a path of shapes in data-driven fashion: $A \rightarrow R \rightarrow S \rightarrow T \rightarrow U \rightarrow V$. Connecting more similar shapes along the path is bound to give better results.



Scene Synthesis

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- ✓ An intuitive approach is to keep the user in the loop via sketches.



Scene Segmentation and Labeling

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- ✓ In order to issue this command to a robot: Get me the **mug** on **table**, need segmentation & labels on scene point cloud (acquired by a depth sensor).



- ✓ User guidance might help for segmentation: https://youtu.be/z_TcWC7yjj0
- ✓ Pairwise analysis might help for labeling.

