

CENG 789 – Digital Geometry Processing

15- 3D Printing

Also presented in Eurasia Graphics 2018 Workshop as
3D Printing: Technology and Research

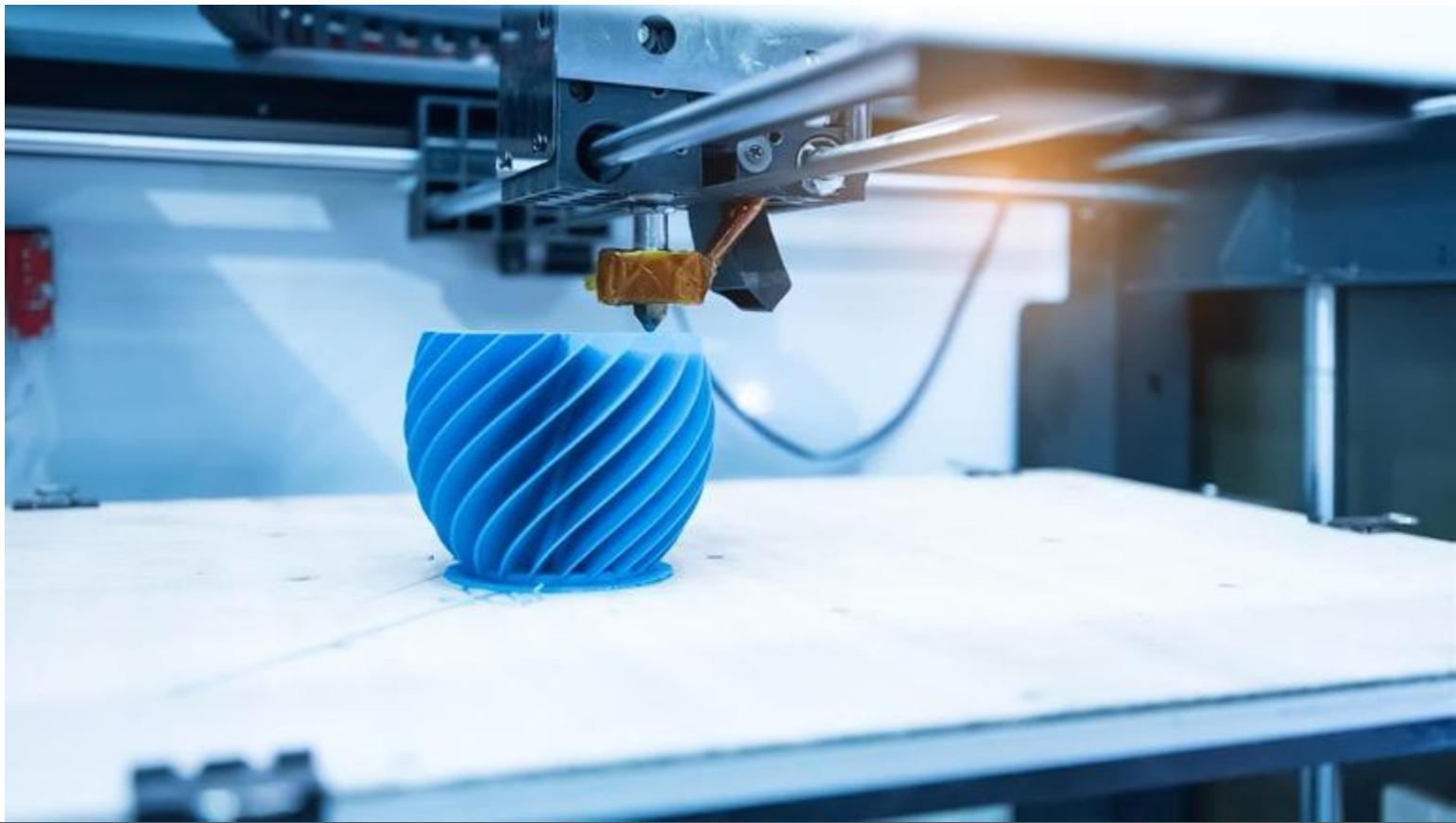
Prof. Dr. Yusuf Sahillioğlu

Computer Eng. Dept,  **MIDDLE EAST TECHNICAL UNIVERSITY**, Turkey

Definition

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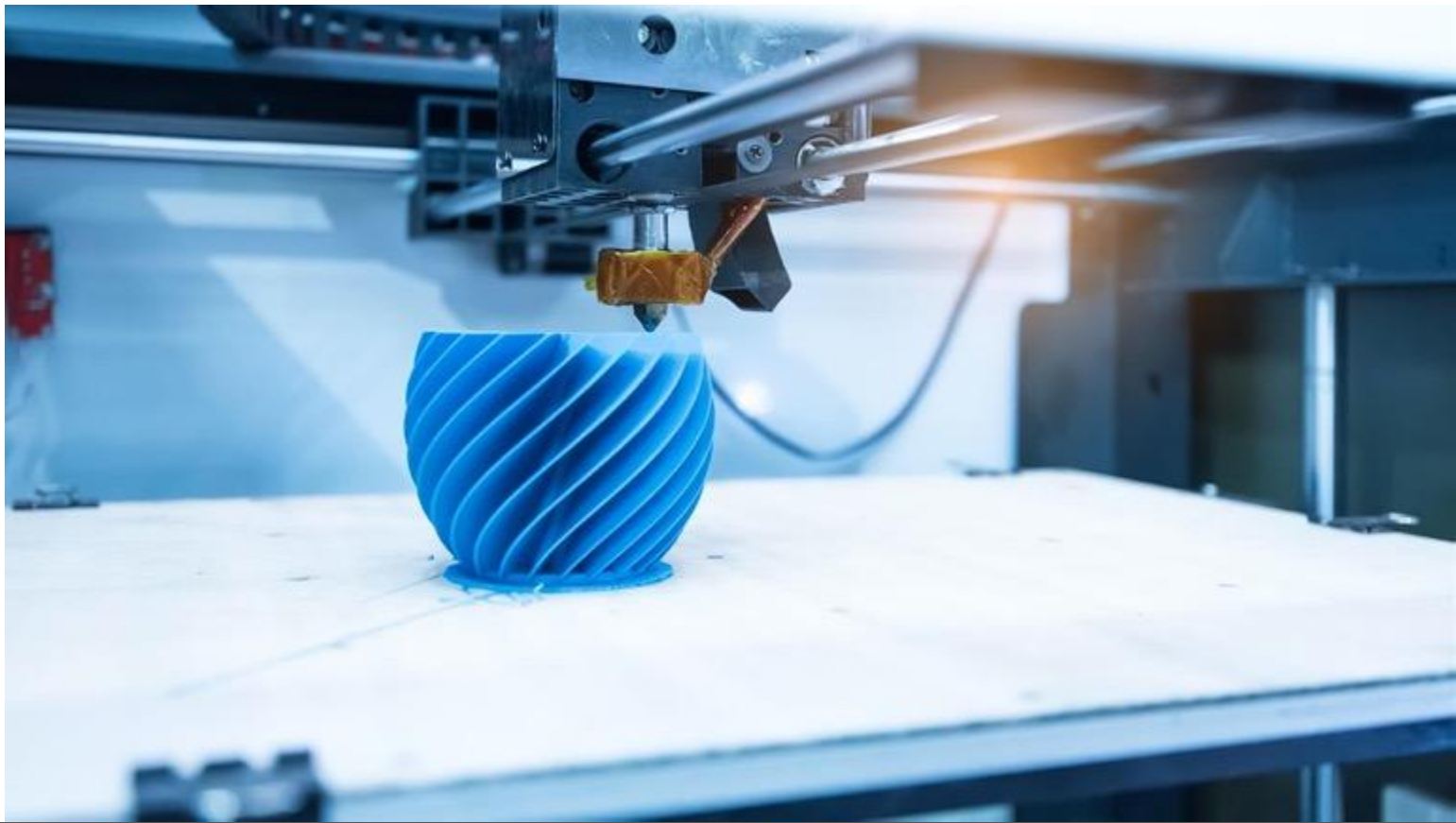
- ✓ Adding material (often in sequential layers) under computer control to create a 3D object.



Definition

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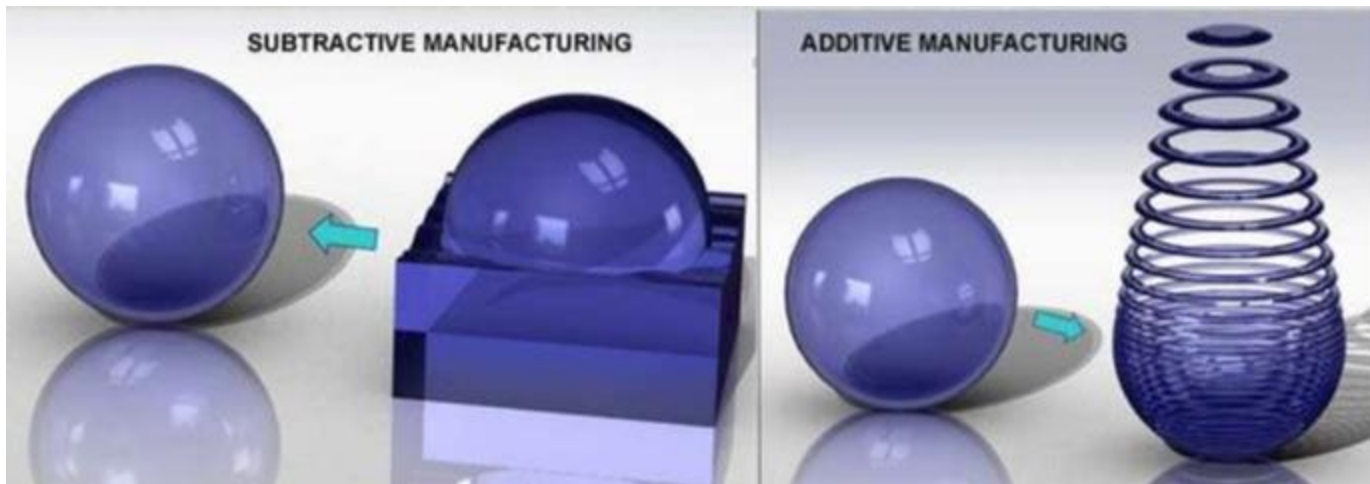
- ✓ Adding material (often in sequential layers) under computer control to create a 3D object.
- ✓ An Additive Manufacturing (AM) technology.



Definition

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- ✓ Adding material (often in sequential layers) under computer control to create a 3D object.
- ✓ Opposite Subtractive Manufacturing (SM): remove material from stock.



History

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- ✓ Despite the recent interest, 3D printing technology dates back to 1981.
- ✓ Became a hot topic since 2009 when FDM patents (Stratasys) expired.
 - ✓ Paves the way to innovation in FDM 3D printers.
 - ✓ Drops desktop 3D printer prices.
 - ✓ Initiates online 3D printing services (Sculpteo).
 - ✓ Increases visibility.
- ✓ FDM not the only AM technique. The first one ('81) was SLA, not FDM.

History

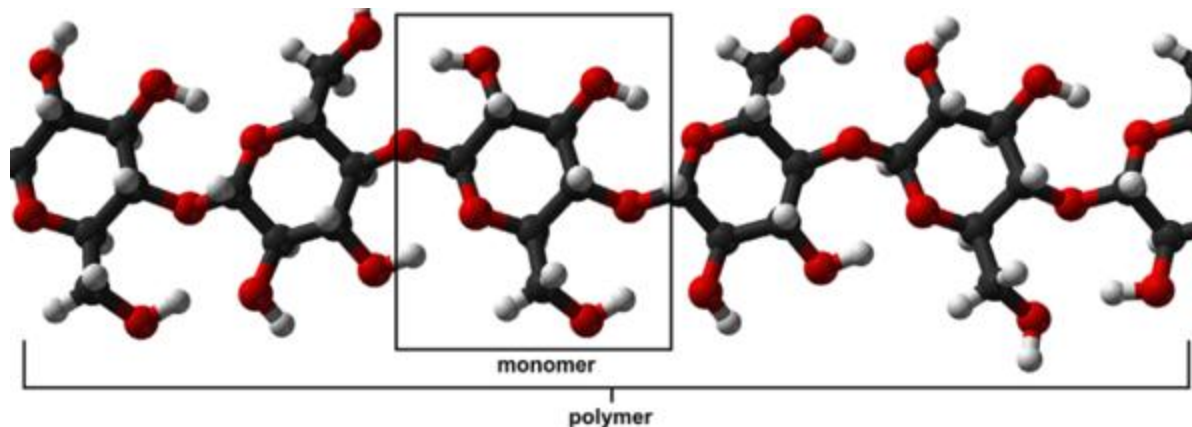
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 - ✓ Hideo Kodama, "Automatic method for fabricating a three-dimensional plastic model with photo-hardening polymer," Review of Scientific Instruments, Vol. 52, No. 11, pp. 1770–73, November 1981.
 - ✓ Resin was polymerized by UV light where UV exposure is controlled by a mask.

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 - ✓ Resin was polymerized by UV light where UV exposure is controlled by a mask.
 - ✓ Polymerization: formation of **polymers** (**many parts**) from **monomers** (**one part**).
 - ✓ A monomer is a molecule that has the ability to chemically bond (covalent) with other molecules in a long chain; a polymer is a chain of monomers.



History

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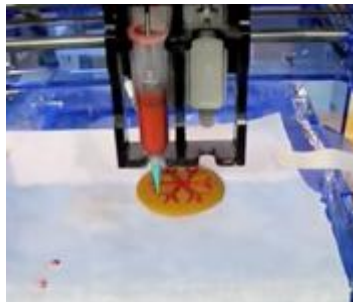
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 - ✓ Resin was polymerized by UV light where UV exposure is controlled by a mask.
 - ✓ Polymerization: formation of **polymers** (**many parts**) from **monomers** (**one part**).
 - ✓ Spider silk is the strongest natural polymer. String confetti is a synthetic one.



History

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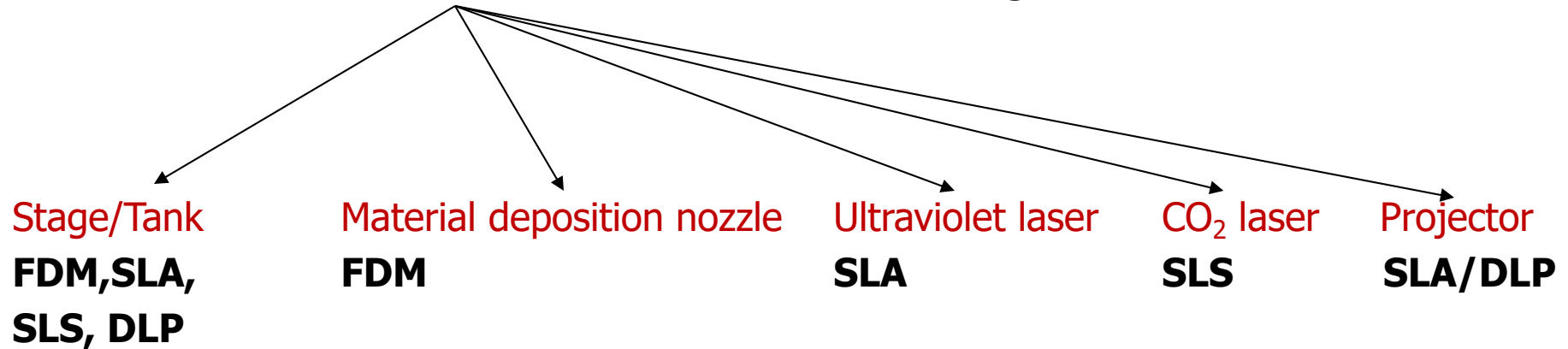
- ✓ Some recent cool 3D printing activities are
 - ✓ First 3D printed prototype car by Urbee, 2010
 - ✓ First 3D food printer by Cornell, 2011
 - ✓ First 3D printed and implanted prosthetic jaw by Hasselt, 2012
 - ✓ First 3D printed animal bone using bio-ink by Trinitiy, 2016.



Components

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- ✓ Uses translational elements to fabricate a digital model.

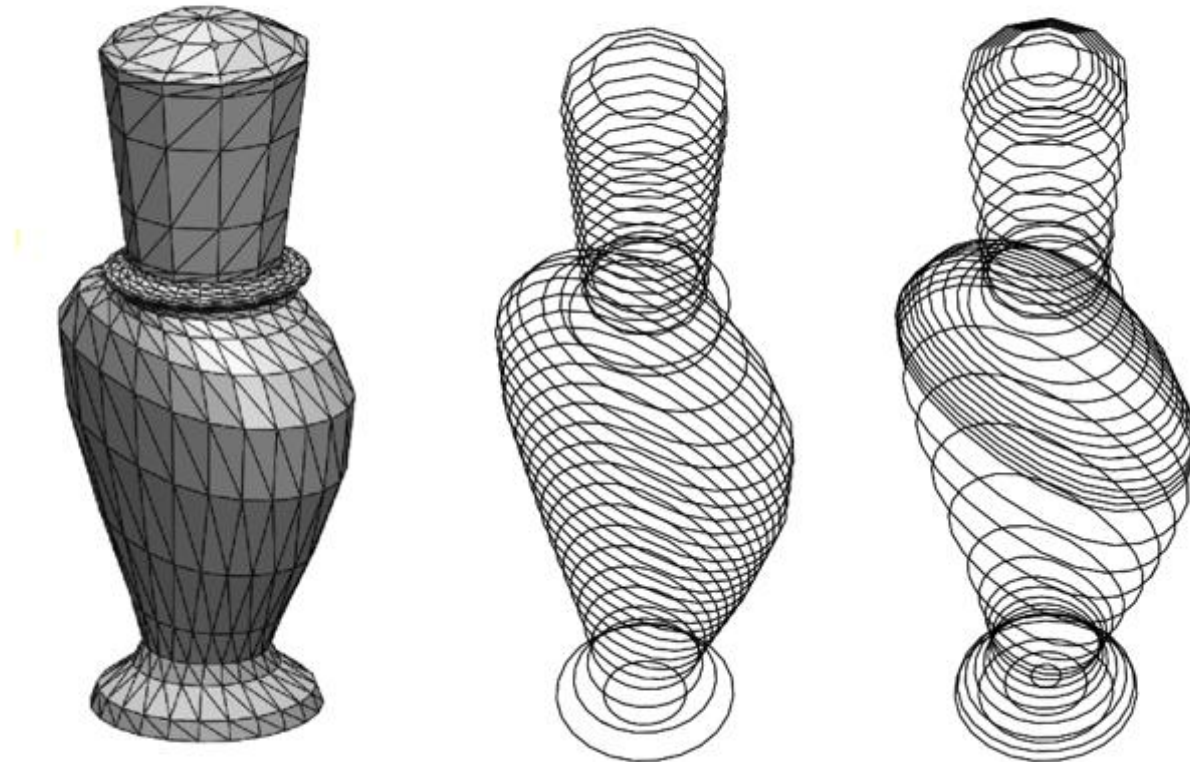


- ✓ **Bolds: Technologies.**

Technology

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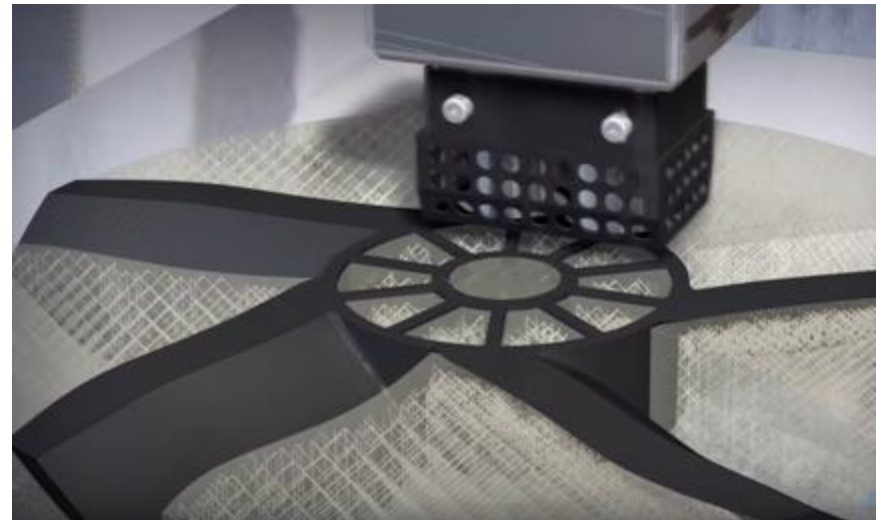
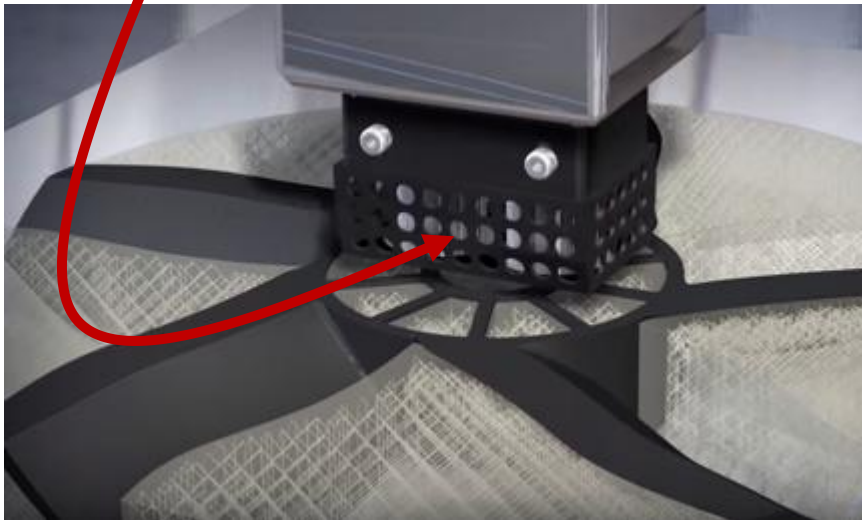
- ✓ FDM: Fused Deposition Modeling.
- ✓ Begins by slicing 3D digital model into layers.



Technology

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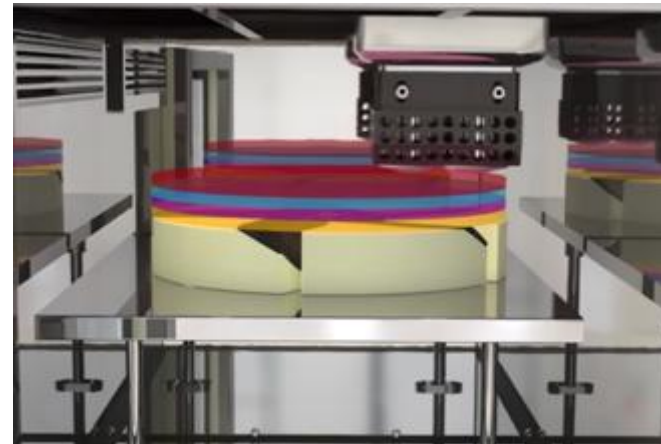
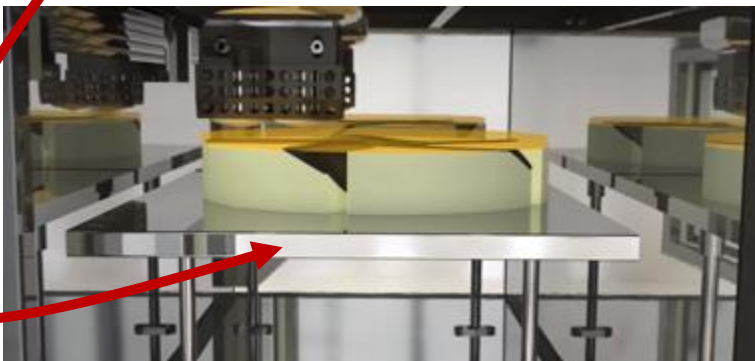
- ✓ FDM: Fused Deposition Modeling.
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- ✓ **Material deposition nozzle**, aka extrusion nozzle, pours **polymeric filament** in the horizontal X-Y plane to build the current layer L_c .
- ✓ Filament is cooled down with the fans around nozzle.



Technology

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- ✓ **Material deposition nozzle**, aka extrusion nozzle, pours **polymeric filament** in the horizontal X-Y plane to build the current layer L_c .
- ✓ Filament is cooled down with the fans around nozzle.
- ✓ **Stage**, aka build plate, moves down one layer when L_c is done.

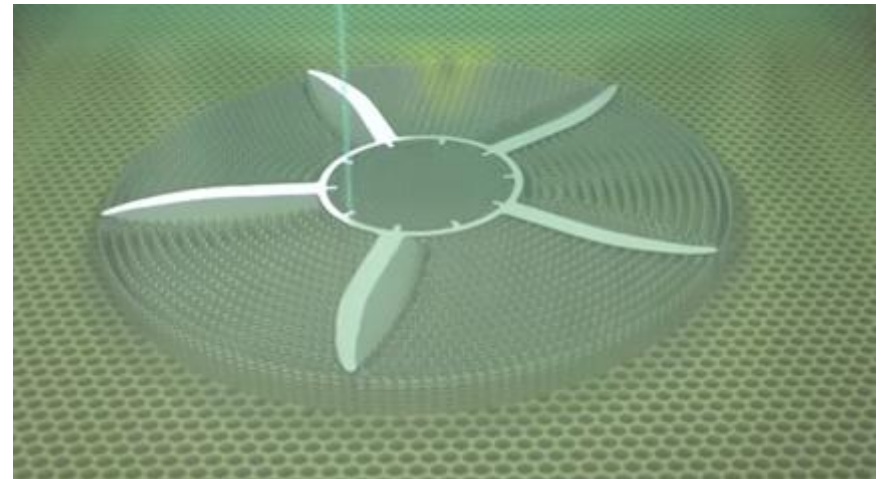
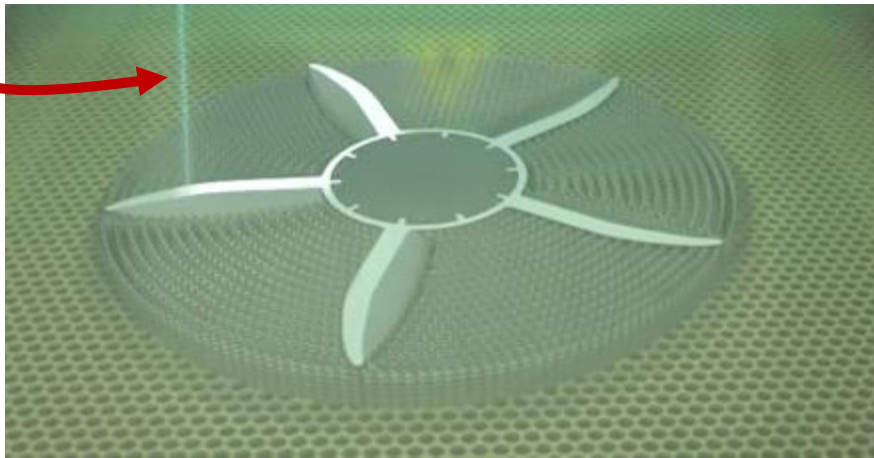


- ✓ Principle: Material deposition.
- ✓ Cool demo: <https://youtu.be/WHO6G67GJbM>

Technology

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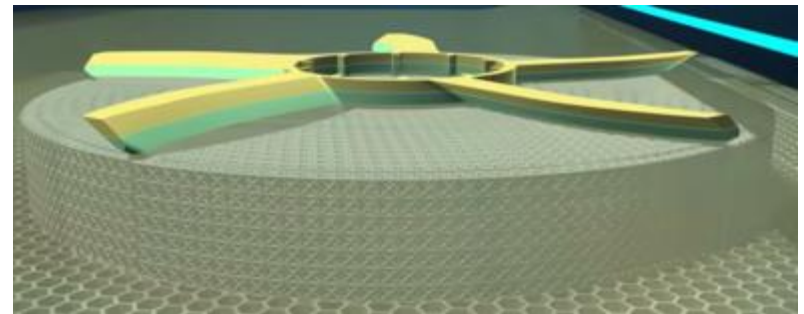
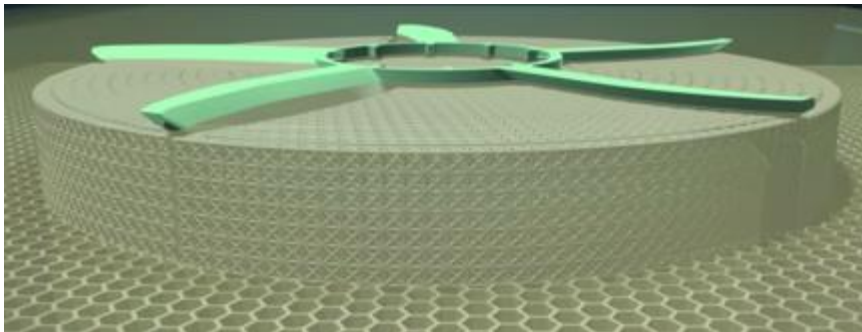
- ✓ SLA: Stereolithography.
- ✓ Begins by slicing 3D digital model into layers.
- ✓ **Ultraviolet laser** is directed (via mirrors) in the horizontal X-Y plane to harden the liquid **photopolymer/resin** on contact w/ the cross-section to build the current layer L_c .



Technology

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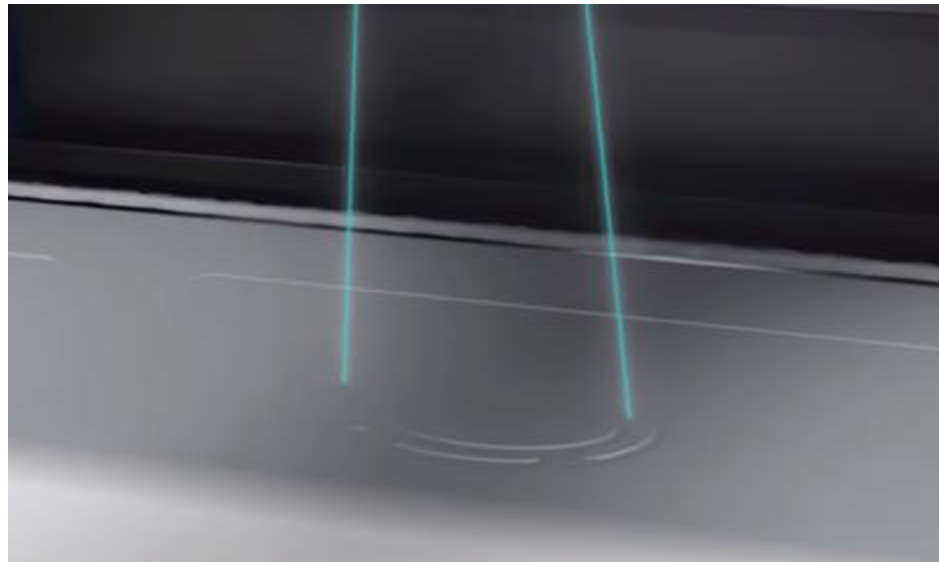


- ✓ Principle: Material solidification.
- ✓ Cool demo: <https://youtu.be/NM55ct5KwiI>

Technology

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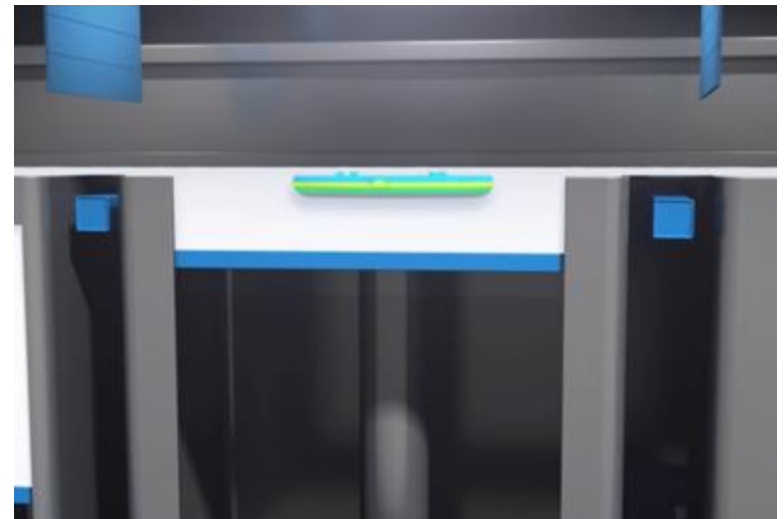
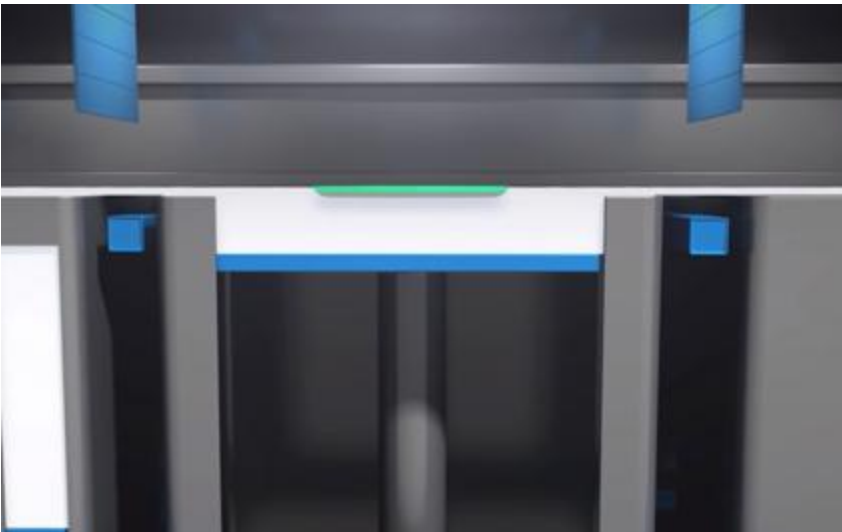
- ✓ SLS: Selective Laser Sintering.
- ✓ Begins by slicing 3D digital model into layers.
- ✓ **CO₂ laser** is directed in the horizontal X-Y plane to fuse the **polymer powder** on contact w/ the cross-section to build the current layer L_c .



Technology

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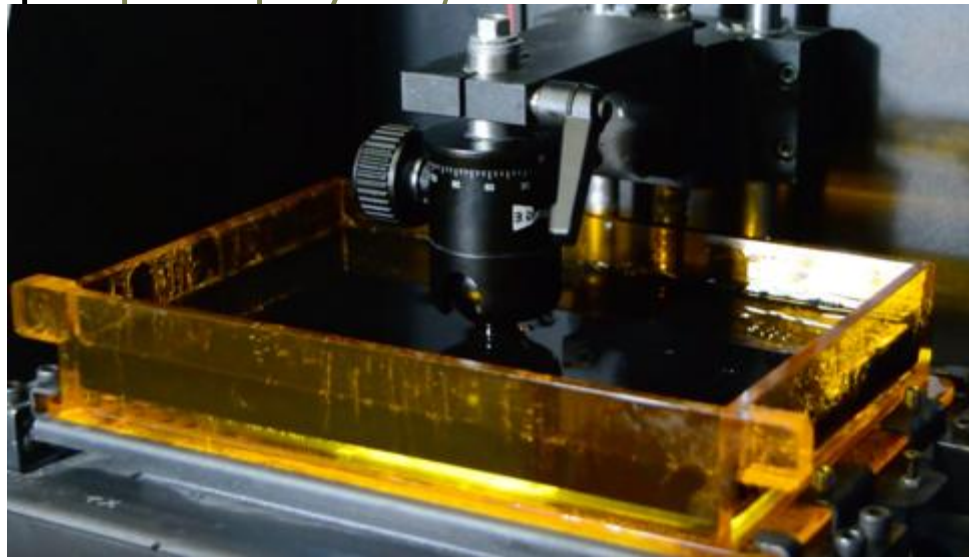


- ✓ Principle: Material solidification.
- ✓ Cool demo: https://youtu.be/9E5MfBAV_tA

Technology

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- ✓ SLA/DLP: Direct Light Processing based SLA.
- ✓ Begins by slicing 3D digital model into layers.
- ✓ Instead of a continuous path a deposition (FDM) or laser (SLA, SLS), you project a set of contour/cross-section images via DLP **projector** onto the liquid **photopolymer/resin** to build the current layer.



- ✓ Principle: Material solidification.
- ✓ Cool demo: <https://youtu.be/hQ21gbeYFYQ>

Technology

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- ✓ SLA/DLP: Direct Light Processing based SLA.
- ✓ Begins by slicing 3D digital model into layers.
- ✓ Instead of a *continuous* path a deposition (FDM) or laser (SLA, SLS), you project a set of contour/cross-section *images* via DLP projector onto the liquid photopolymer/resin to build the current layer.
- ✓ SLA/DLP is *raster*-based, all other technologies are *vector*-based.

Technology Wrap-Up

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- ✓ FDM: Fused Deposition Modeling. //polymeric filament, nozzle.
- ✓ SLA: Stereolithography. //photopolymer: resin, UV laser.
- ✓ SLS: Selective Laser Sintering. //polymer powder, CO₂ laser.
- ✓ SLA/DLP: DLP-based SLA. //photopolymer: resin, image.



Technology Wrap-Up

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- ✓ Go with FDM for multi-material/color (deposition).

Technology Wrap-Up

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- ✓ Go with FDM for multi-material/color (deposition).
- ✓ Go with FDM for fully closed empty voids (non-solidified material gets trapped there in the other technologies).

Technology Wrap-Up

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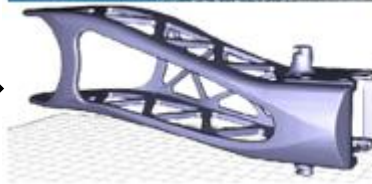
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 - ✓ Go with FDM for fully closed empty voids (non-solidified traps there).
 - ✓ Go with SLS, SLA, SLA/DLP for complex geometries (creation and removal of support structures are problematic and inevitable in FDM).

Without support,
overhangs fall →



Sacrificial external
support structure, and

3D input model →



model after its removal.

Technology Wrap-Up

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- ✓ Dual-nozzle 3D FDM printers w/ soluble support material available.



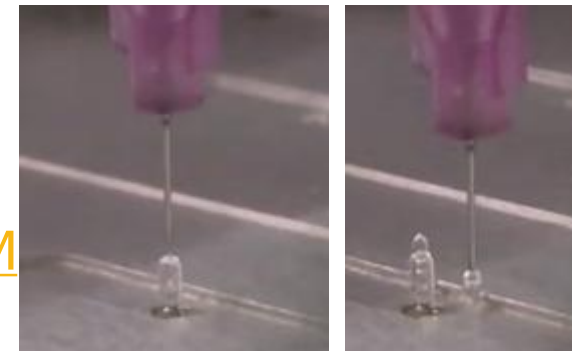
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- ✓ New techs can print out-of-plane (doable with FDM if you manage to avoid nozzle hitting an already printed part): youtu.be/NWBa8OWgApM



Technology Wrap-Up

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- ✓ New techs can print out-of-plane (FDM logic; a biological fabrication technique via silkworms):
<https://youtu.be/0ePriBJKYt8>



Technology Wrap-Up

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- ✓ New techs can print out-of-plane (doable with FDM if you manage to avoid nozzle hitting an already printed part).
- ✓ Print time depends on part volume in FDM, part height in others (cos constant sweeptime requird per layer); they're bad for single small obj.

Product Development Pipeline

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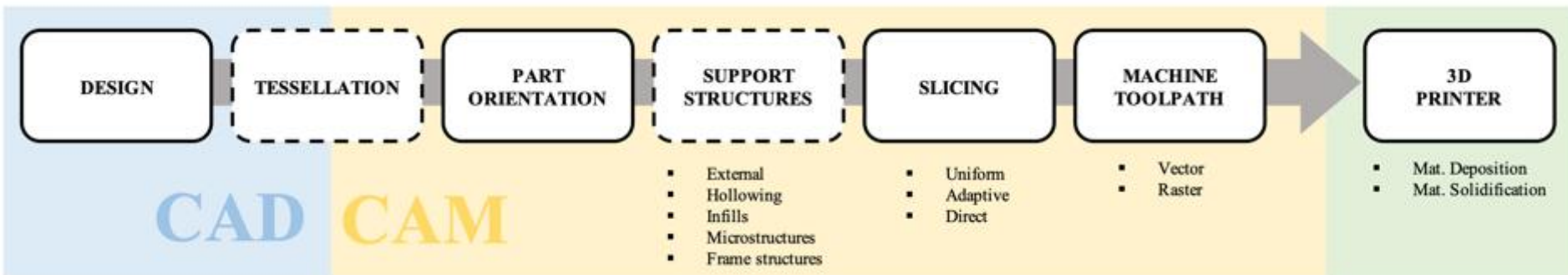


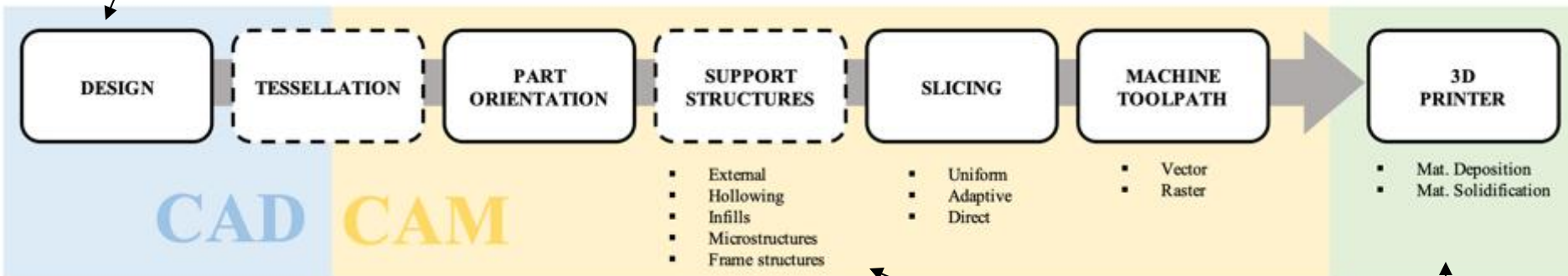
Figure from: Livesu et al., 2017, From 3D models to 3D prints: an overview of the processing pipeline.

Process Planning Pipeline (Yellow Part)

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- ✓ We assume that product concept, e.g., Armadillo, is already designed, e.g., by a CAD expert, without knowing whether it'll be printed or not.



- ✓ We will go through each single step in *Process Planning* (PP) pipeline (dashed boxes optional) that prepares the 3D model for fabrication.
 - ✓ PP: After design and before actual manufacturing.

Process Planning Pipeline in a Nutshell

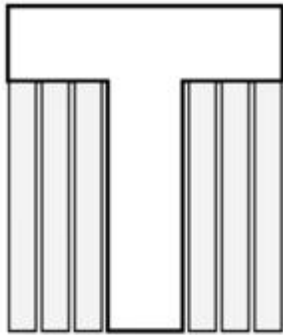
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- ✓ Update the mesh to comply with the input representation requirements.
 - ✓ Tessellated geometry must be watertight: enclose a solid: no water leakage.

Process Planning Pipeline in a Nutshell

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- ✓ Update the mesh to comply with the input representation requirements.
 - ✓ Tessellated geometry must be watertight: enclose a solid: no water leakage.
- ✓ Orient optimally to minimize print time, support need, .. or fit chamber.



Should have been
upside-down T.

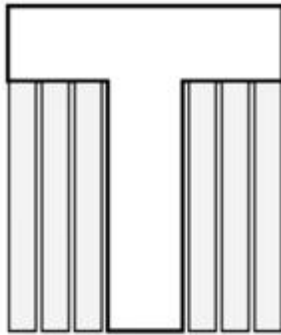


Sagged result
without support.

Process Planning Pipeline in a Nutshell

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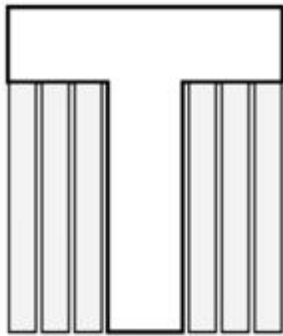
Sagged result
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- ✓ Create support structures (if FDM in use).

Process Planning Pipeline in a Nutshell

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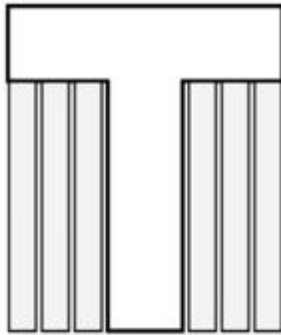
- ✓ Create support structures (if FDM in use).
- ✓ Slice the model uniformly or adaptively.



Process Planning Pipeline in a Nutshell

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Should have been
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Sagged result
without support.

- ✓ Create support structures (if FDM in use).
- ✓ Slice the model uniformly or adaptively.
- ✓ Convert each slice to a toolpath (vector) or grid of solid pixels (raster).



```
26 [layer count: 336  
27 [layer: 0  
28 M107  
29 G0 F9000 X91.800 Y93.520 Z0.300  
30 [TYPE:SKIRT  
31 G1 F1200 X92.617 Y92.870 E0.01964  
32 G1 X93.518 Y92.432 E0.03865  
33 G1 X94.458 Y92.141 E0.05705  
34 G1 X95.218 Y92.072 E0.07143  
35 G1 X95.998 Y92.064 E0.08608
```

Audience

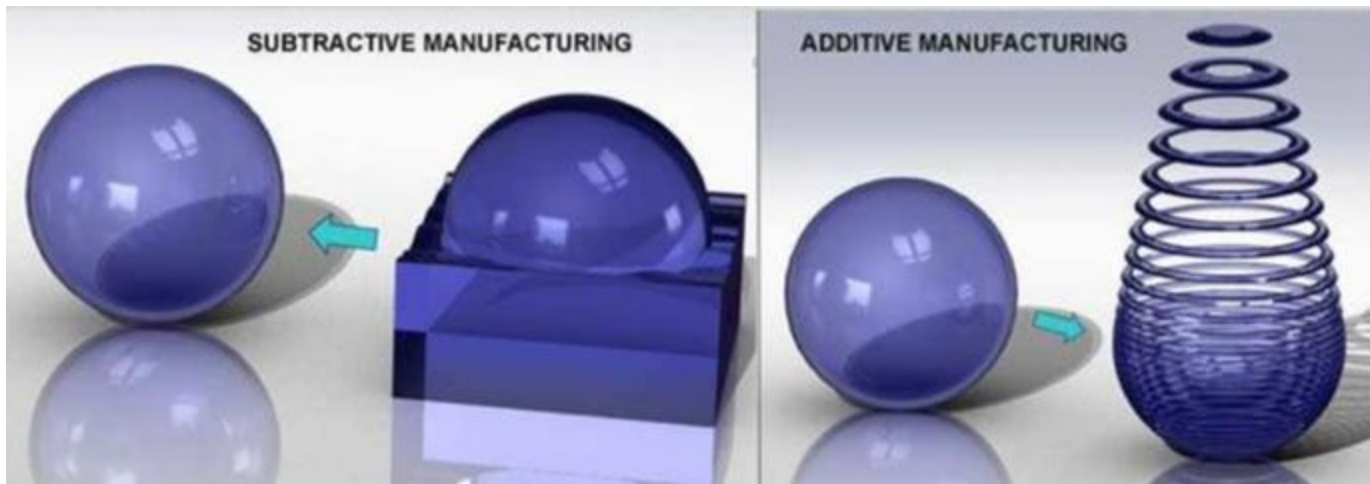
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- ✓ People who contribute to the PP pipeline in the context of AM:
 - ✓ Computer graphics experts.
 - ✓ Mechanical engineers.
 - ✓ Material scientists.
 - ✓ Mathematicians.

AM vs. SM

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- ✓ PP in traditional SM, such as CNC machining, is complex, e.g., experienced skilled manufacturer needed.
- ✓ PP in AM is mostly algorithmic.
- ✓ Also notice the significantly less material waste in AM.



AM vs. SM

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- ✓ AM enables fabrication of shapes that cannot be done with SM.
 - ✓ Shapes that were interesting from a theoretical point can now be printed and their functionality can now be exploited.



- ✓ Made possible because 2D toolpaths are generated (within each slice) instead of complex 3D paths.

AM vs. SM

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- ✓ AM is excellent for customization.
 - ✓ 3D scan yourself or any other thing, manipulate digitally (optional), fabricate.



- ✓ Geometry Processing pipeline involved consists of acquisition, registration, reconstruction, remeshing, and smoothing. These steps and more are covered in our course CENG 789. <https://youtu.be/K6xgsscQac8>

AM vs. SM

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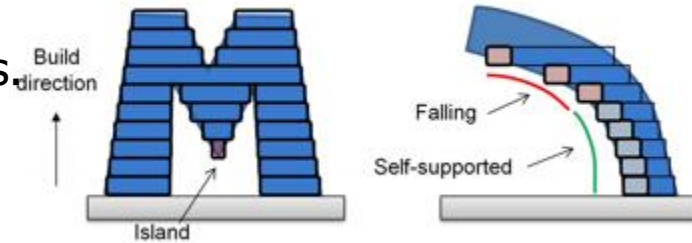
- ✓ AM is practical for multi-color and multi-material production.



AM vs. SM

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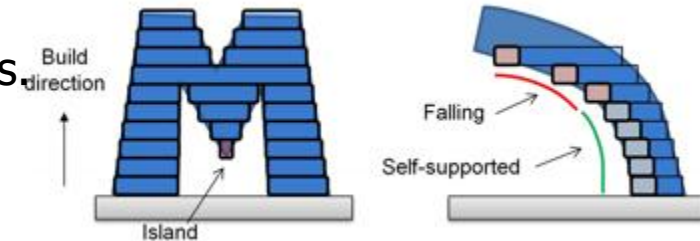
- ✓ Drawbacks of AM also exist.
 - ✓ Limited part sizes, fabrication speed, materials.
 - ✓ Poor surface finish.
 - ✓ High cost.
 - ✓ Gravity effective during manufacturing (overhangs/islands must be supported).
- ✓ So go with SM if you need many (speed) precise (surface finish) items.
- ✓ Or go with AM if you need highly complex and intricate items, e.g., those that require a hollow interior (to save weight or material).



AM vs. SM

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- ✓ Drawbacks of AM also exist.
 - ✓ Limited part sizes, fabrication speed, materials.
 - ✓ Poor surface finish.
 - ✓ High cost.
 - ✓ Gravity effective during manufacturing (overhangs/islands must be supported).



- ✓ Better yet, go with a hybrid solution: AM and SM together.



Surface finish achieved by AM (left) is improved with SM (right, milling).

Tuning PP Pipeline

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- ✓ PP can be tuned to optimize for one or a combination of objectives.
 - ✓ Cost.
 - ✓ Fidelity.
 - ✓ Functionality.

Tuning PP Pipeline - Cost

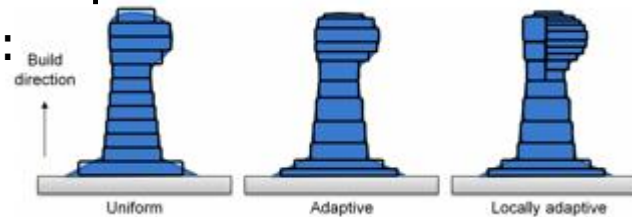
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- ✓ Minimize Pre-build Cost + Build Cost + Post-processing Cost.

Tuning PP Pipeline - Cost

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- ✓ Minimize Pre-build Cost + Build Cost + Post-processing Cost.
- ✓ Cost to turn a design into a set of printer instructions.
 - ✓ Efficient algorithms, e.g., slicing:
 - ✓ Reduced user interaction.
- ✓ Labor cost.
 - ✓ Load print material, e.g., powder.
 - ✓ Clean and warm up printer.
 - ✓ Deal with printer software, e.g., Cura.



Tuning PP Pipeline - Cost

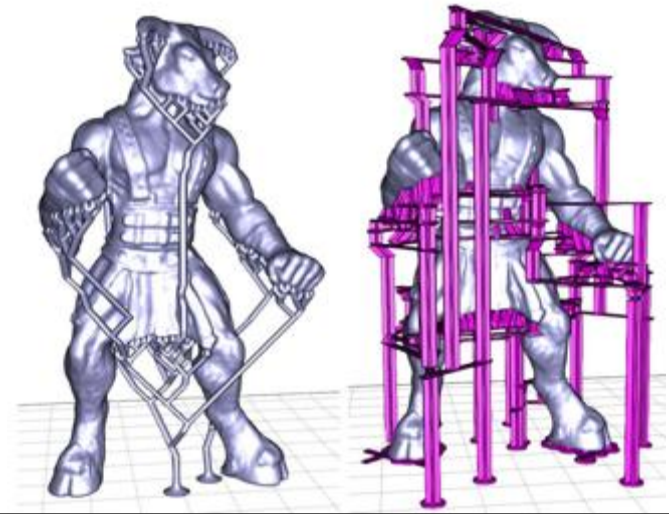
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- ✓ Minimize Pre-build Cost + Build Cost + Post-processing Cost.
- ✓ Printing time.
 - ✓ Efficient algorithms, e.g., orientation.
 - ✓ Reduced user interaction.
- ✓ Material cost.
 - ✓ Reduce material waste.
 - ✓ Structural strength may degrade to use less mat.: bad for industrial production.
- ✓ Support structure amount affects both printing time and material cost.
- ✓ Can be computed by the sum of the volumes of the prisms generated by extruding the down-facing triangles up to the building plate.

Tuning PP Pipeline - Cost


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- ✓ Minimize Pre-build Cost + Build Cost + Post-processing Cost.
- ✓ Printing time.
 - ✓ Efficient algorithms, e.g., orientation.
 - ✓ Reduced user interaction.
- ✓ Material cost.
 - ✓ Reduce material waste.
 - ✓ Structural strength may degrade to use less mat.: bad for industrial production.
- ✓ Support structure amount affects both printing time and material cost.
- ✓ Can be reduced by employing tree- or scaffold-based structures.



Tuning PP Pipeline - Cost

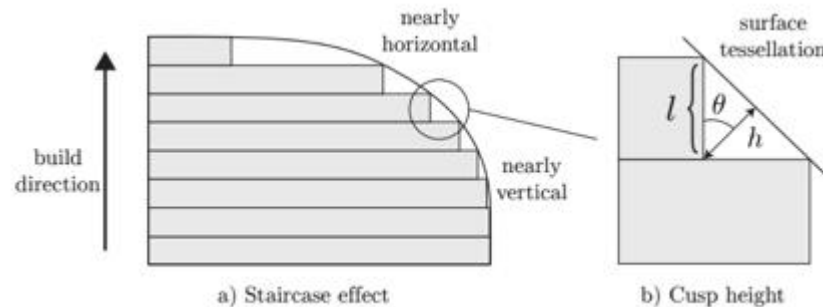
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- ✓ Minimize Pre-build Cost + Build Cost + Post-processing Cost.
 - ✓ Polishing time.
 - ✓ Detach supports.
 - ✓ Chemical, mechanical or manual surface finishing.
- 

Tuning PP Pipeline - Fidelity

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- ✓ How perfect the replica is?
- ✓ Form fidelity: difference in shape b/w design and production.



- ✓ Layers piled along building direction causes staircase effect → fidelity ↓
- ✓ Cusp-height error measures form fidelity.

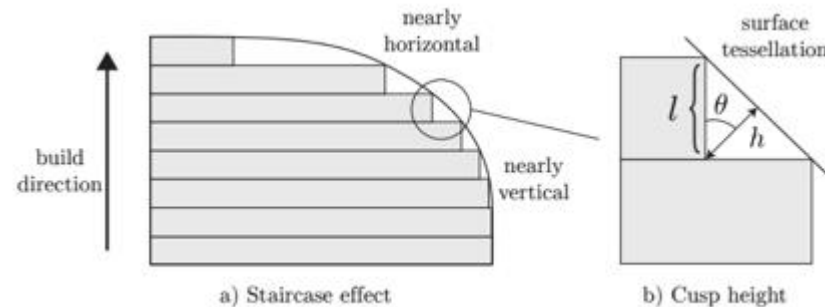
$$h = \begin{cases} l |\cos \theta| & \text{for } |\cos \theta| \neq 1 \\ 0 & \text{for } |\cos \theta| = 1 \end{cases}$$

- ✓ $|\cos \theta|$ grows as θ decreases (see nearly horizontal part above).

Tuning PP Pipeline - Fidelity

49 / 86

- ✓ How perfect the replica is?
- ✓ Form fidelity: difference in shape b/w design and production.



- ✓ Layers piled along building direction causes staircase effect → fidelity ↓
- ✓ Cusp-height error measures form fidelity.

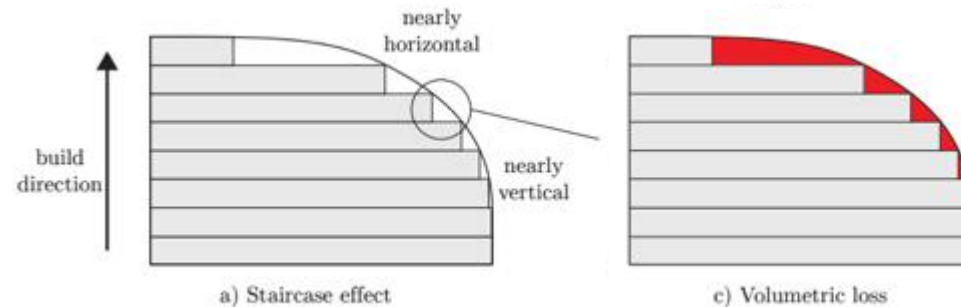
$$h = \begin{cases} l |\cos \theta| & \text{for } |\cos \theta| \neq 1 \\ 0 & \text{for } |\cos \theta| = 1 \end{cases}$$

- ✓ Integral of cusp-height before printing (build direction b): for each face w/ normal n , $|\cos \theta| = |b \cdot n|$. Add these errors (more for horizontal).

Tuning PP Pipeline - Fidelity

50 / 86

- ✓ How perfect the replica is?
- ✓ Form fidelity: difference in shape b/w design and production.



- ✓ Layers piled along building direction causes staircase effect → fidelity ↓
- ✓ Volumetric loss measures form fidelity.
- ✓ Red area above.
- ✓ Similar to cusp-height, compute before printing.

Tuning PP Pipeline - Fidelity

51 / 86

- ✓ How perfect the replica is?
- ✓ Texture fidelity: tiny local variations over the printed surface.
- ✓ Unlike form fidelity, computed after printing (using sampling schemes).
- ✓ Aka surface finish.
- ✓ To obtain better fidelity, meniscus smoothing or support hiding popular.

Tuning PP Pipeline - Fidelity

52 / 86

- ✓ How perfect the replica is?
- ✓ Texture fidelity: tiny local variations over the printed surface.
- ✓ Unlike form fidelity, computed after printing (using sampling schemes).
- ✓ Aka surface finish.
- ✓ To obtain better fidelity, meniscus smoothing or support hiding popular.
- ✓ Lift the solidified layer above the upper surface of the resin tank to stretch a meniscus of liquid b/w each layer → smoother transition.

Tuning PP Pipeline - Fidelity

53 / 86

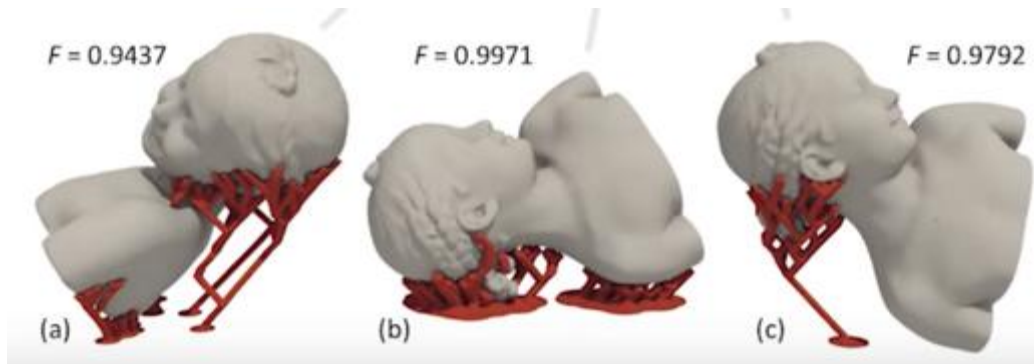
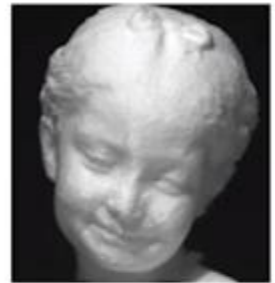
- ✓ How perfect the replica is?
- ✓ Texture fidelity: tiny local variations over the printed surface.
- ✓ Unlike form fidelity, computed after printing (using sampling schemes).
- ✓ Aka surface finish.
- ✓ To obtain better fidelity, meniscus smoothing or support hiding popular.
- ✓ Place supports at the least salient parts so that removal artifacts are hidden.



Tuning PP Pipeline - Fidelity

54 / 86

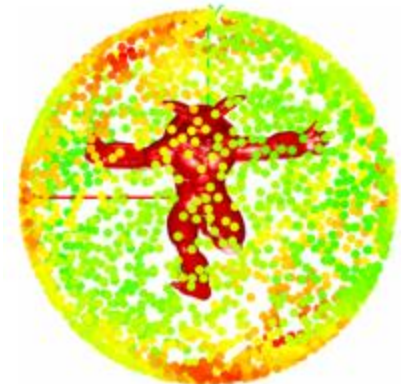
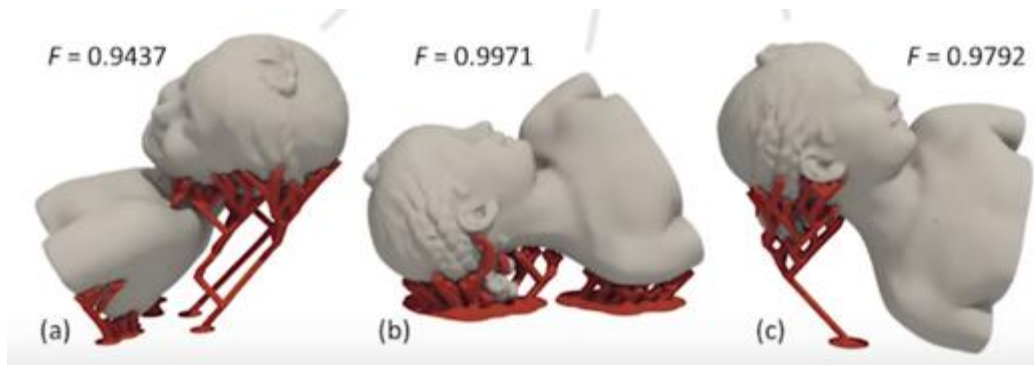
- ✓ How perfect the replica is?
- ✓ Texture fidelity: tiny local variations over the printed surface.
- ✓ Unlike form fidelity, computed after printing (using sampling schemes).
- ✓ Aka surface finish.
- ✓ To obtain better fidelity, meniscus smoothing or support hiding popular.
- ✓ Place supports at the least salient parts so that removal artifacts are hidden.



Tuning PP Pipeline - Fidelity

55 / 86

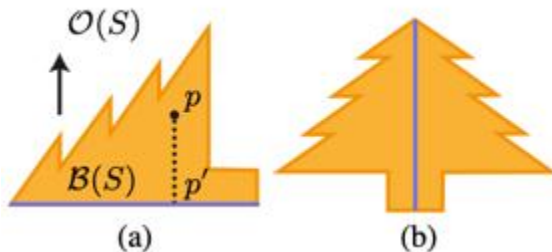
- ✓ How perfect the replica is?
- ✓ Texture fidelity: tiny local variations over the printed surface.
- ✓ Unlike form fidelity, computed after printing (using sampling schemes).
- ✓ Aka surface finish.
- ✓ To obtain better fidelity, meniscus smoothing or support hiding popular.
- ✓ To find building direction: i) consider a small # of candid orientations (predefined or computed on convex hull), ii) shortlist from a regular sampling of orientations.



Tuning PP Pipeline - Fidelity

56 / 86

- ✓ How perfect the replica is?
 - ✓ Texture fidelity: tiny local variations over the printed surface.
 - ✓ Unlike form fidelity, computed after printing (using sampling schemes).
 - ✓ Aka surface finish.
 - ✓ To obtain better fidelity, meniscus, support hiding, or self-supports.
- ←
- ✓ Split model into approximately pyramidal parts that support themselves.



Tuning PP Pipeline - Functionality

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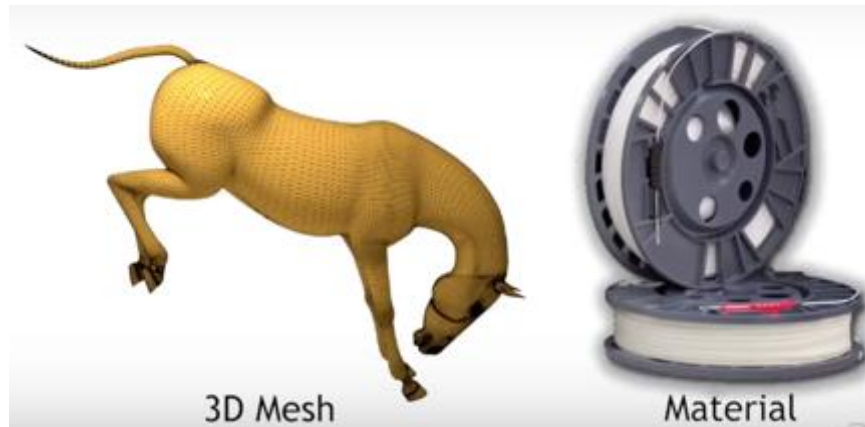
- ✓ Optimize shape to comply with some functional requirements.
 - ✓ Robustness: insensitive to known or unknown forces.
 - ✓ Mass distribution: achieve static or dynamic equilibrium.
 - ✓ Light/sound propagation: guide light/sound inside the object.

Tuning PP Pipeline - Functionality

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- ✓ Optimize shape to comply with some functional requirements.
 - ✓ Robustness: insensitive to known or unknown forces.

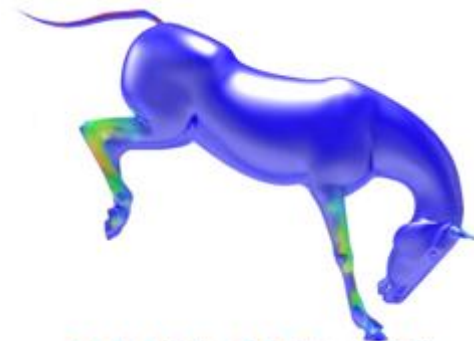
Input:



&



Output: probability of failure/fraction & location of common point of failures.

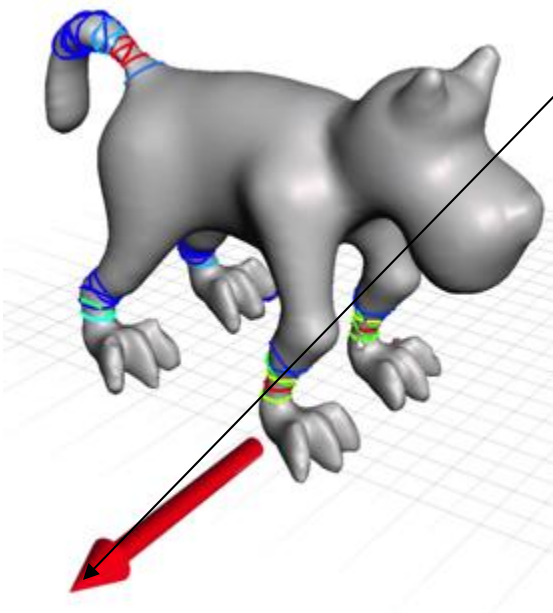


Tuning PP Pipeline - Functionality

59 / 86

- ✓ Optimize shape to comply with some functional requirements.
 - ✓ Robustness: insensitive to known or unknown forces.

Optimal orientation that will result in an as-strong-as-possible 3D print. Weak sections are identified and up direction for printing is determined accordingly.

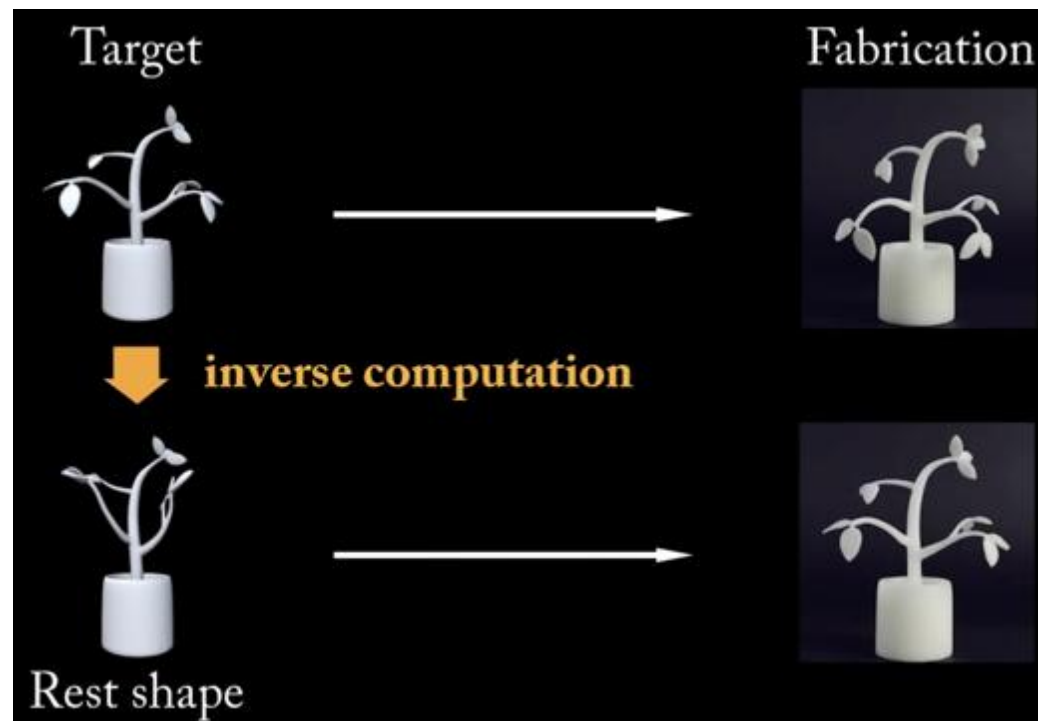


Tuning PP Pipeline - Functionality

60 / 86

- ✓ Optimize shape to comply with some functional requirements.
 - ✓ Robustness: insensitive to known or unknown forces.

Elastic objs deform under gravity after printing. Take this into account beforehand.

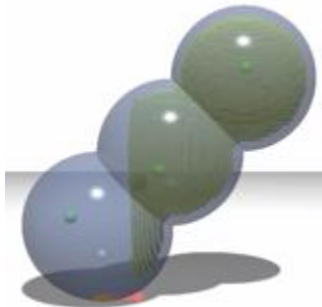


Tuning PP Pipeline - Functionality

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- ✓ Optimize shape to comply with some functional requirements.
 - ✓ Mass distribution: achieve static or dynamic equilibrium.

Make an object stand, spin, or float after fabrication by distributing cavities inside.



Tuning PP Pipeline - Functionality

62 / 86

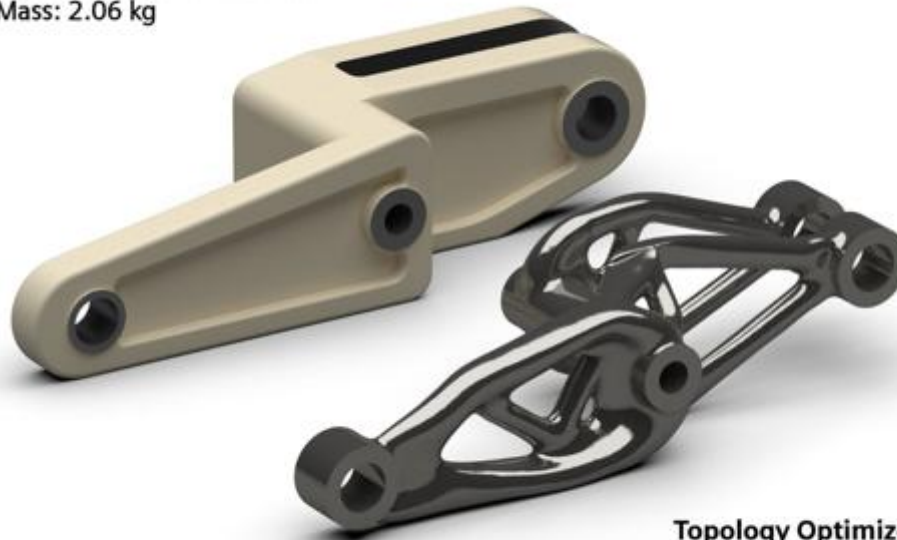
- ✓ Optimize shape to comply with some functional requirements.
 - ✓ Mass distribution: achieve static or dynamic equilibrium.

Topology optimization to get low weight to strength ratios, e.g., for aerospace.

Original Part

Volume: 263,346 cubic mm

Mass: 2.06 kg



Topology Optimized Part

Volume: 97,884 cubic mm

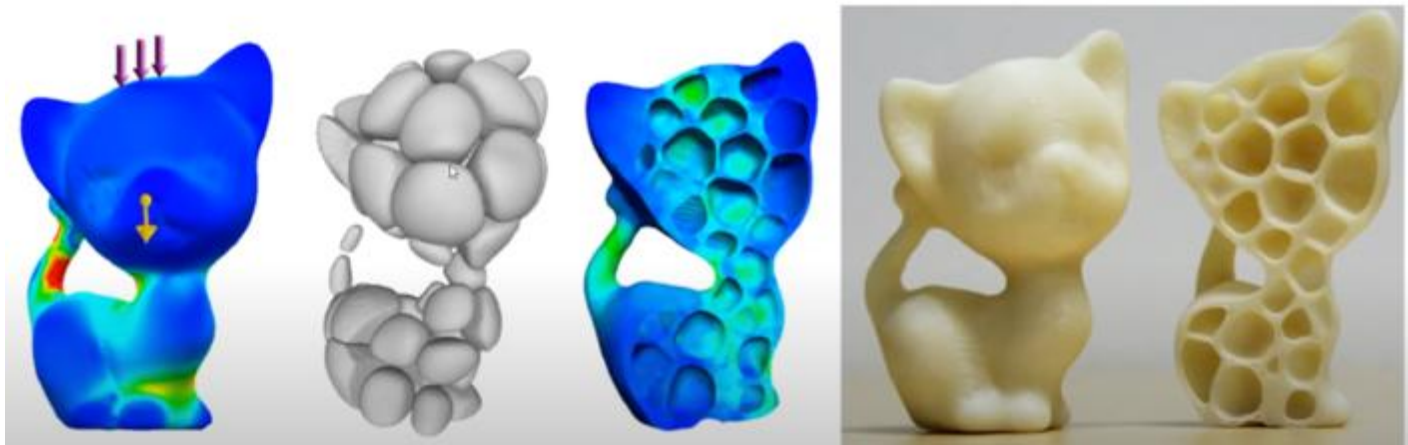
Mass: 0.766 kg

Tuning PP Pipeline - Functionality

63 / 86

- ✓ Optimize shape to comply with some functional requirements.
 - ✓ Mass distribution: achieve static or dynamic equilibrium.

Topology optimization to get low weight to strength ratios, e.g., for aerospace.



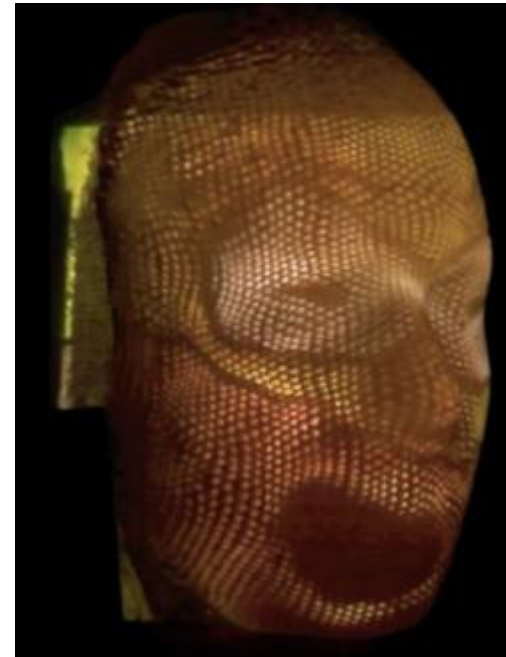
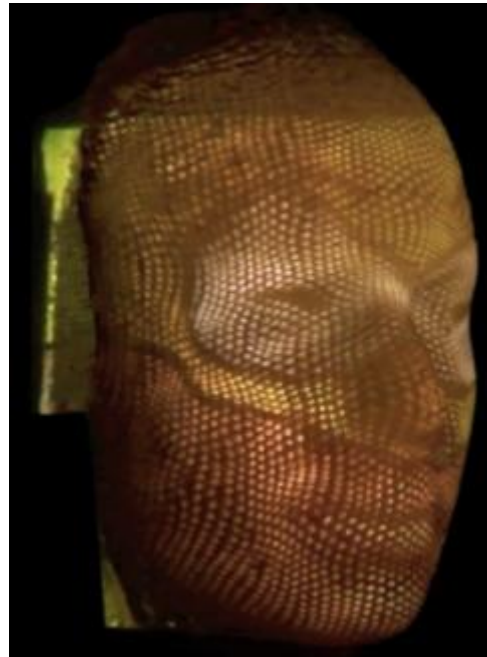
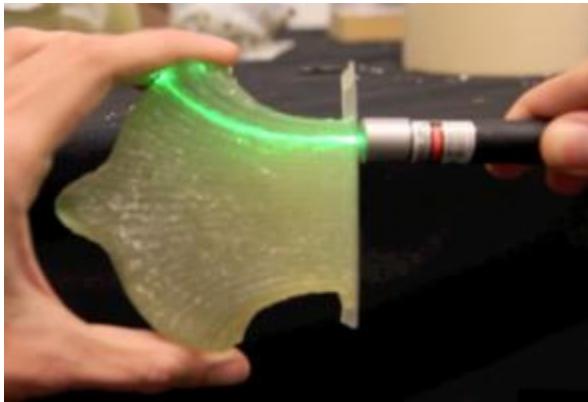
More interior Voronoi sites around the weaker regions (non-blue) would lead to more Voronoi cells/edges to be printed on those vulnerable parts. Regions that don't carry lot of stress (blue) aren't prone to break so larger cells there (less sites).

Tuning PP Pipeline - Functionality

64 / 86

- ✓ Optimize shape to comply with some functional requirements.
 - ✓ Light/sound propagation: guide light/sound inside the object.

Multi-material printing to fabricate curved displays w/ embedded optical fibers.



Tuning PP Pipeline - Functionality

65 / 86

- ✓ Optimize shape to comply with some functional requirements.
 - ✓ Light/sound propagation: guide light/sound inside the object.

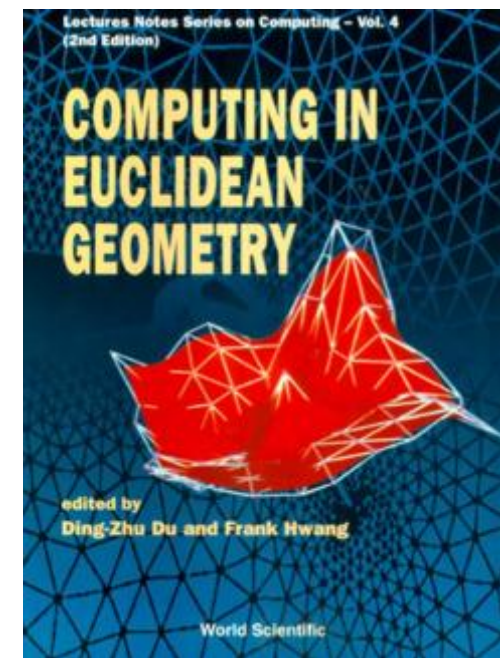
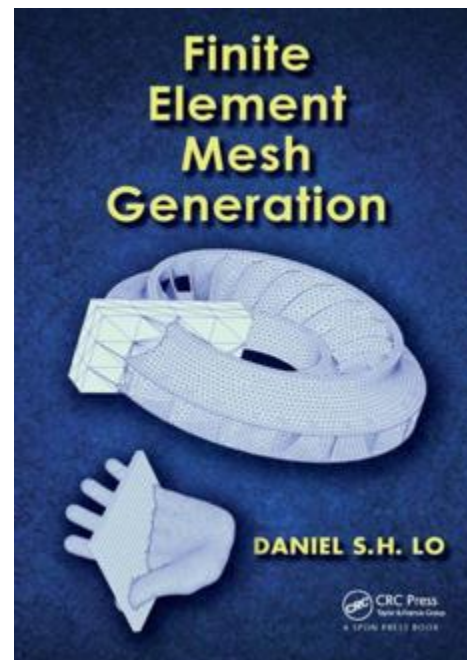
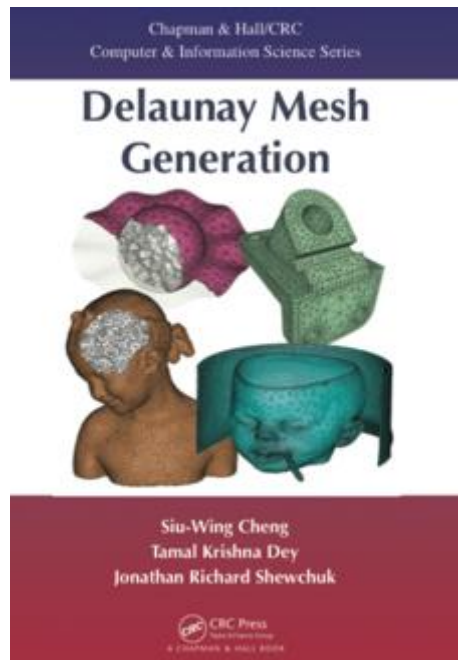
Natural frequency optimization to make object sound in a controlled manner.



Input Requirements

66 / 86

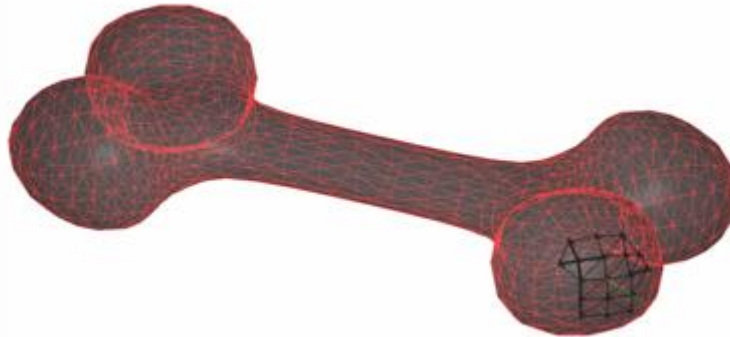
- ✓ Printing technology is for solid objects: tessellation.
- ✓ A raw point cloud, e.g. 3D scan result, must be tessellated into a mesh.
- ✓ There exist books on the subject. See also Surface Reconstruction lect.



Input Requirements

67 / 86

- ✓ Printing technology is for solid objects: tessellation.
- ✓ A raw point cloud, e.g. 3D scan result, must be tessellated into a mesh.
- ✓ Here is a simple algorithm:

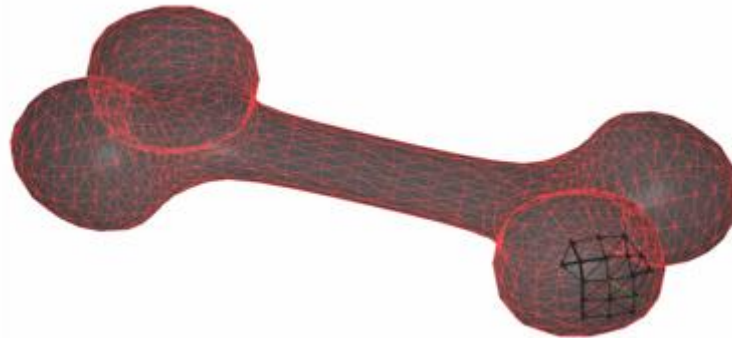


- ✓ Find local neighborhood L_i of each point p_i in the 3D point cloud input.
 - ✓ Closest k points (using a k-d tree).
- ✓ For each L_i compute tangent plane using PCA.
- ✓ Project all points in L_i to the tangent plane and compute their 2D Delaunay triangulation D_i .

Input Requirements

68 / 86

- ✓ Printing technology is for solid objects: tessellation.
- ✓ A raw point cloud, e.g. 3D scan result, must be tessellated into a mesh.
- ✓ Here is a simple algorithm:

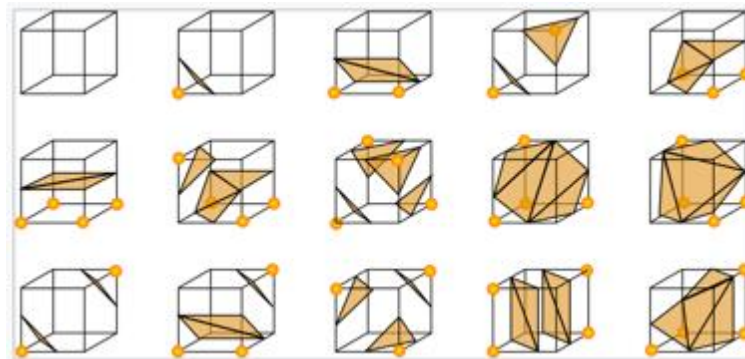
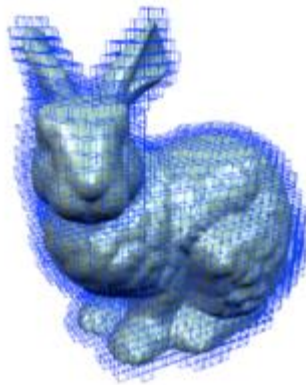


- ✓ D_i is a set of edges: $D_i = \{e_i^1, e_i^2, \dots, e_i^{noe(i)}\}$ where $noe(i)$ is the number of edges of the i^{th} Delaunay triangulation.
- ✓ Final triangulation is the composition of all N local triangulations:
$$D = \bigcup_1^N \{e_i^1, e_i^2, \dots, e_i^{noe(i)}\}.$$
- ✓ Note that global D not necessarily a 2-manifold. Set $k = 0.02n$ and restrict value to $[8, 12]$.

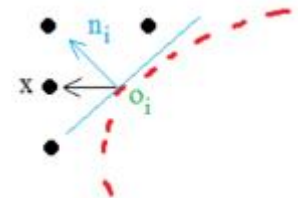
Input Requirements

69 / 86

- ✓ Printing technology is for solid objects: tessellation.
- ✓ A raw point cloud, e.g. 3D scan result, must be tessellated into a mesh.
- ✓ Here is a popular algorithm:



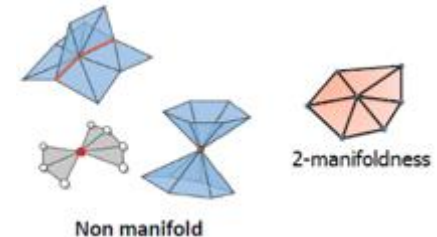
- ✓ Previous algorithm performed an explicit reconstruction.
- ✓ Marching cubes is an implicit method that extracts the zero-set of a scalar function, commonly a signed distance function $F(\mathbf{x}) = (\mathbf{x} - \mathbf{o}_i) \cdot \mathbf{n}_i$



Input Requirements

70/
86

- ✓ Printing technology is for solid objects: watertight meshes.
- ✓ Manifold meshes: keep things simple.
 - ✓ Images: assume every pixel has 4 neighbors. Likewise, assume meshes are manifold. It keeps formulas simple and leads to fewer special cases in code.
 - ✓ Edges are contained in at most 2 polygonal faces.
 - ✓ Vertices are contained in disk of triangles.



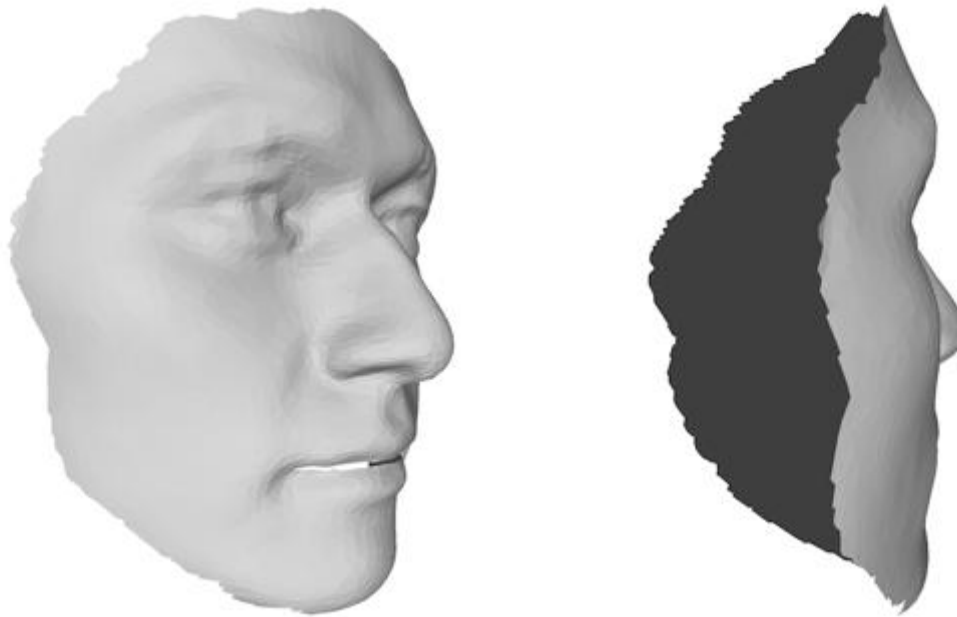
- ✓ Watertight meshes are 2-manifold meshes w/o boundary edges.
- ✓ No holes or non-manifold structures.
- ✓ Closed mesh (no boundary edges).
- ✓ Imagine filling the inside of the mesh w/ water, would anything leak out? If not, then chances are the mesh is watertight.



Input Requirements

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- ✓ Printing technology is for solid objects: watertight meshes.
- ✓ Thicken sheet-like structures to make them printable: surface-to-solid.
 - ✓ Extrude each vertex along its normal direction (both positive and negative) by a default offset defining the shell thickness.

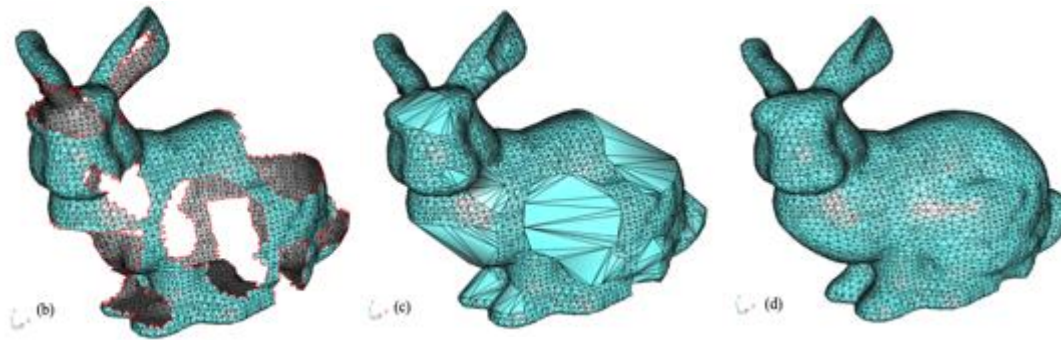


Input Requirements

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- ✓ Printing technology is for solid objects: watertight meshes.
- ✓ Fill holes to ensure that the resulting mesh encloses a solid.





- ✓ Printing technology is for solid objects: watertight meshes.
- ✓ Filling Holes in Meshes, 2003.
 - ✓ Triangulate (coarse).
 - ✓ n vertex $\rightarrow n-2$ triangles (dynamic programming (DP)).
 - ✓ Refine.
 - ✓ Subdivide triangles to reduce edge lengths to avg edge length at the hole boundary.
 - ✓ Flip interior edges if flipping maximizes min angle (Delaunay).
 - ✓ Smooth.
 - ✓ Mesh fairing.

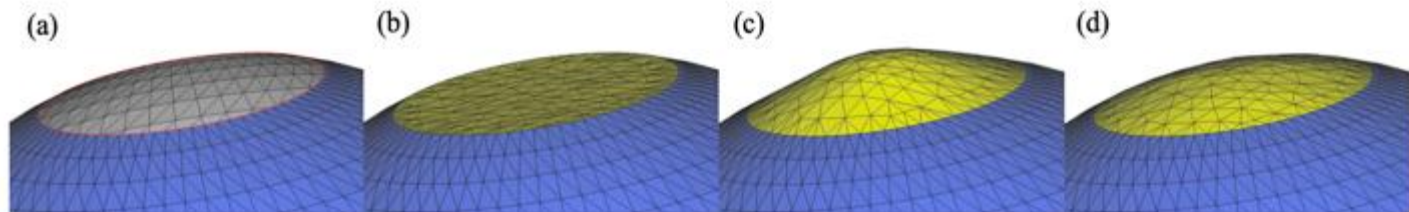
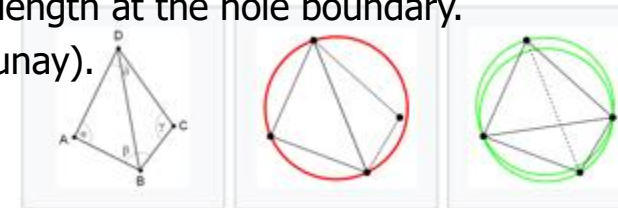


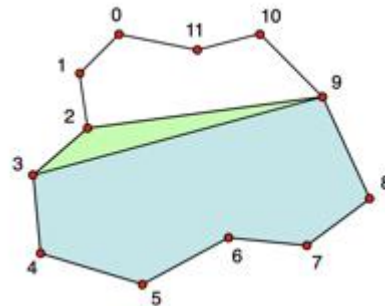
Figure 6: (a) Hole at the top of a sphere (inside of sphere is gray). (b) Patching mesh (yellow), before fairing. (c) Patching mesh (yellow) after uniform fairing. (d) Patching mesh (yellow) after scale-dependent fairing.

Input Requirements

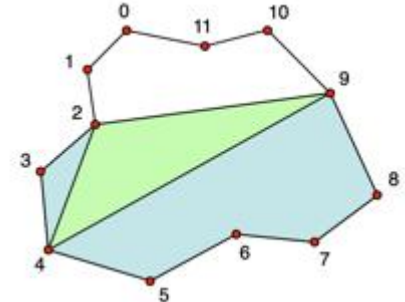
74 / 86

- ✓ Printing technology is for solid objects: watertight meshes.
- ✓ Coarse triangulation T that minimizes area sum + max dihedral angle.
- ✓ Let $w[a,c]$ be the min weight/cost that can be achieved in triangulating the polygon $a, a+1, \dots, c$. Final output by $w[0, n-1]$. To get there, intermediate steps like $w[2,9]$ will be filled and stored in the DP table.

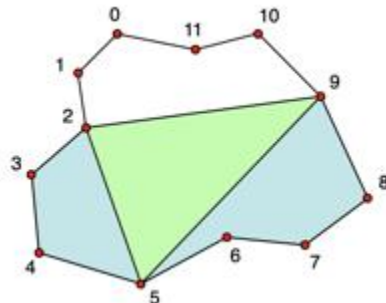
$$w[2,9] = \min(\begin{aligned} &w(\Delta(2,3,9)) + w[3,9], \\ &w[2,4] + w(\Delta(2,4,9)) + w[4,9], \\ &w[2,5] + w(\Delta(2,5,9)) + w[5,9], \end{aligned})$$



$$w[2,9] = \min(\begin{aligned} &w(\Delta(2,3,9)) + w[3,9], \\ &w[2,4] + w(\Delta(2,4,9)) + w[4,9], \\ &w[2,5] + w(\Delta(2,5,9)) + w[5,9], \end{aligned})$$



$$w[2,9] = \min(\begin{aligned} &w(\Delta(2,3,9)) + w[3,9], \\ &w[2,4] + w(\Delta(2,4,9)) + w[4,9], \\ &w[2,5] + w(\Delta(2,5,9)) + w[5,9], \end{aligned})$$



..... next slide →

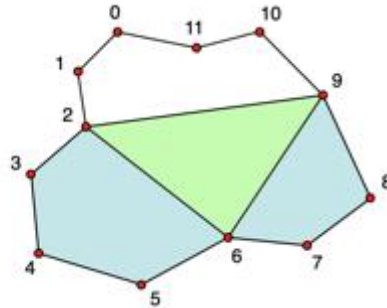
Input Requirements

75 / 86

- ✓ Printing technology is for solid objects: watertight meshes.
- ✓ Coarse triangulation T that minimizes area sum + max dihedral angle.
- ✓ Let $w[a,c]$ be the min weight/cost that can be achieved in triangulating the polygon $a, a+1, \dots, c$.

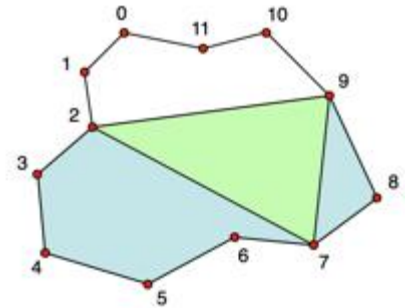
$$w[2,9] = \min($$

$$\begin{aligned} &w(\Delta(2,3,9)) + w[3,9], \\ &w[2,4] + w(\Delta(2,4,9)) + w[4,9], \\ &w[2,5] + w(\Delta(2,5,9)) + w[5,9], \\ &w[2,6] + w(\Delta(2,6,9)) + w[6,9], \end{aligned}$$



$$w[2,9] = \min($$

$$\begin{aligned} &w(\Delta(2,3,9)) + w[3,9], \\ &w[2,4] + w(\Delta(2,4,9)) + w[4,9], \\ &w[2,5] + w(\Delta(2,5,9)) + w[5,9], \\ &w[2,6] + w(\Delta(2,6,9)) + w[6,9], \\ &w[2,7] + w(\Delta(2,7,9)) + w[7,9], \end{aligned}$$

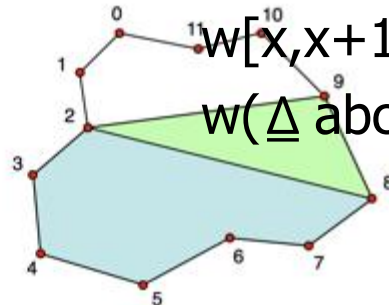


$$w[a,c] = \min w[a,b] + w(\triangle abc) + w[b,c]$$

$$w[2,9] = \min($$

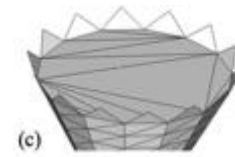
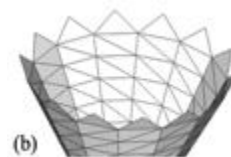
$$\begin{aligned} &w(\Delta(2,3,9)) + w[3,9], \\ &w[2,4] + w(\Delta(2,4,9)) + w[4,9], \\ &w[2,5] + w(\Delta(2,5,9)) + w[5,9], \\ &w[2,6] + w(\Delta(2,6,9)) + w[6,9], \\ &w[2,7] + w(\Delta(2,7,9)) + w[7,9], \\ &w[2,8] + w(\Delta(2,8,9)) \end{aligned}$$

$$)$$



$$w[x,x+1] = 0$$

$$w(\triangle abc) = \text{area}(a,b,c) \text{ yields min area } T.$$



crenellation triangles duplicated ☹.

Sharp folds and non-manifold edges.

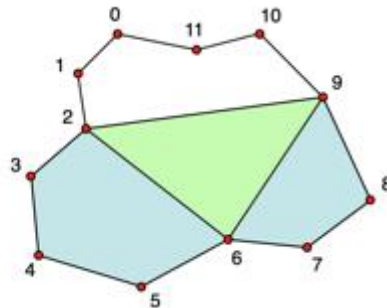
Input Requirements

76 / 86

- ✓ Printing technology is for solid objects: watertight meshes.
- ✓ Coarse triangulation T that minimizes area sum + max dihedral angle.
- ✓ Let $w[a,c]$ be the min weight/cost that can be achieved in triangulating the polygon $a, a+1, \dots, c$.

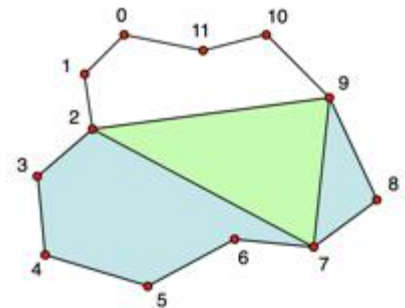
$$w[2,9] = \min($$

$$\begin{aligned} &w(\Delta(2,3,9)) + w[3,9], \\ &w[2,4] + w(\Delta(2,4,9)) + w[4,9], \\ &w[2,5] + w(\Delta(2,5,9)) + w[5,9], \\ &w[2,6] + w(\Delta(2,6,9)) + w[6,9], \end{aligned}$$



$$w[2,9] = \min($$

$$\begin{aligned} &w(\Delta(2,3,9)) + w[3,9], \\ &w[2,4] + w(\Delta(2,4,9)) + w[4,9], \\ &w[2,5] + w(\Delta(2,5,9)) + w[5,9], \\ &w[2,6] + w(\Delta(2,6,9)) + w[6,9], \\ &w[2,7] + w(\Delta(2,7,9)) + w[7,9], \end{aligned}$$

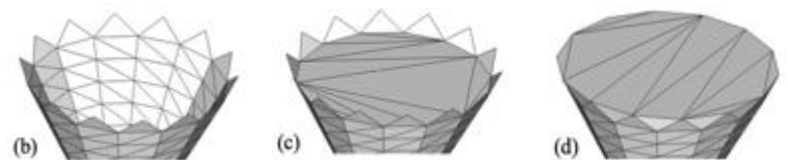
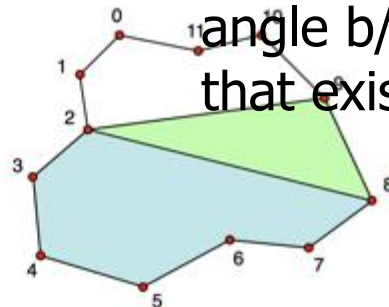


$w(\triangle abc) = \text{area}(a,b,c) \text{ plus max dihedral angle b/w } a,b,c \text{ and existing adj. triangles that exist at the time of evaluation.}$

$$w[2,9] = \min($$

$$\begin{aligned} &w(\Delta(2,3,9)) + w[3,9], \\ &w[2,4] + w(\Delta(2,4,9)) + w[4,9], \\ &w[2,5] + w(\Delta(2,5,9)) + w[5,9], \\ &w[2,6] + w(\Delta(2,6,9)) + w[6,9], \\ &w[2,7] + w(\Delta(2,7,9)) + w[7,9], \\ &w[2,8] + w(\Delta(2,8,9)) \end{aligned}$$

$$)$$

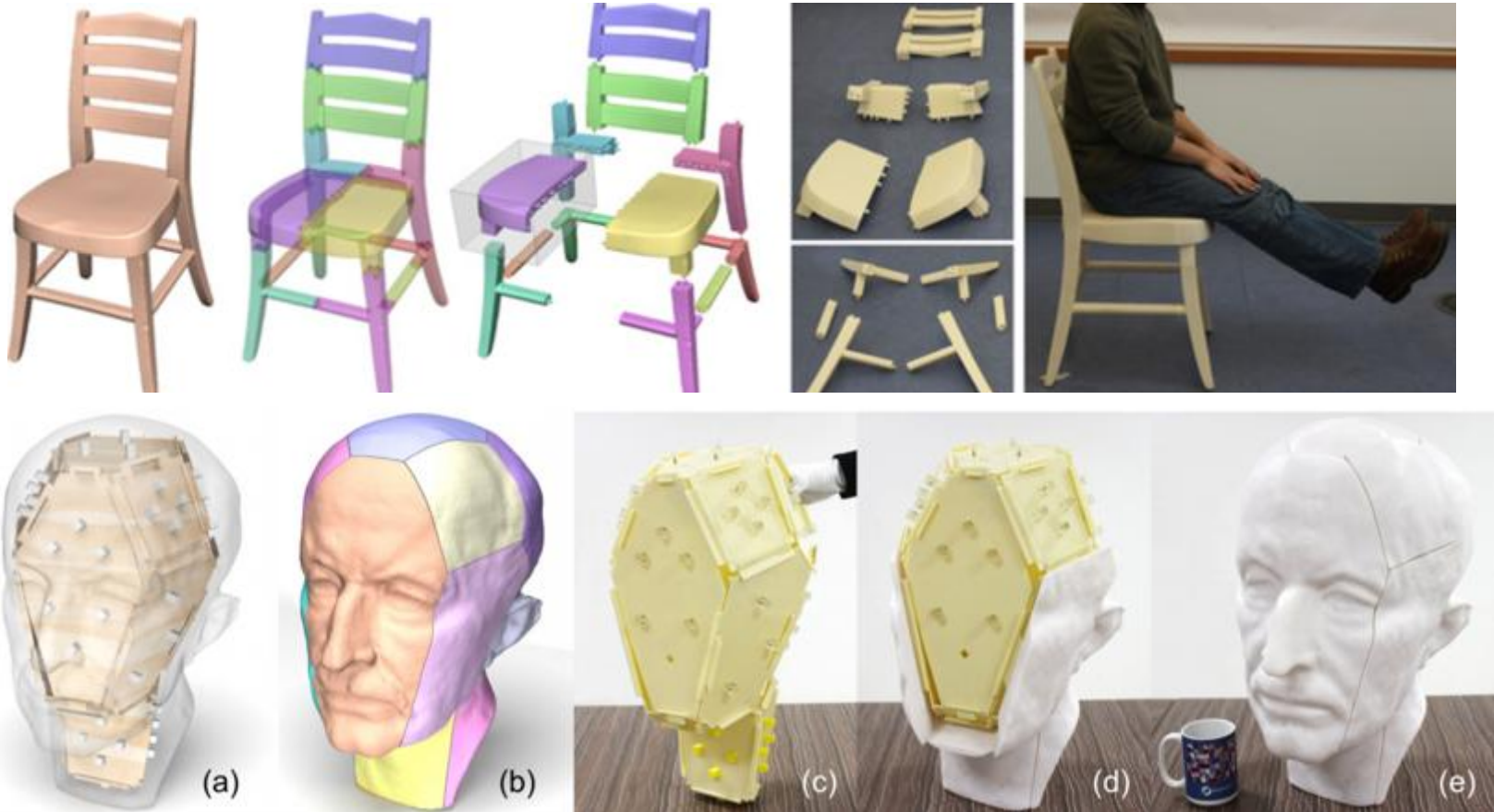


dihedral: $\cos \phi_{AB} = \mathbf{n}_A \cdot \mathbf{n}_B$

Shape Requirements

77 / 86

- ✓ Printing technology is for moderate-size shapes that fits into chamber.
- ✓ Split big model into parts that can be printed separately & assembled.



Shape Requirements

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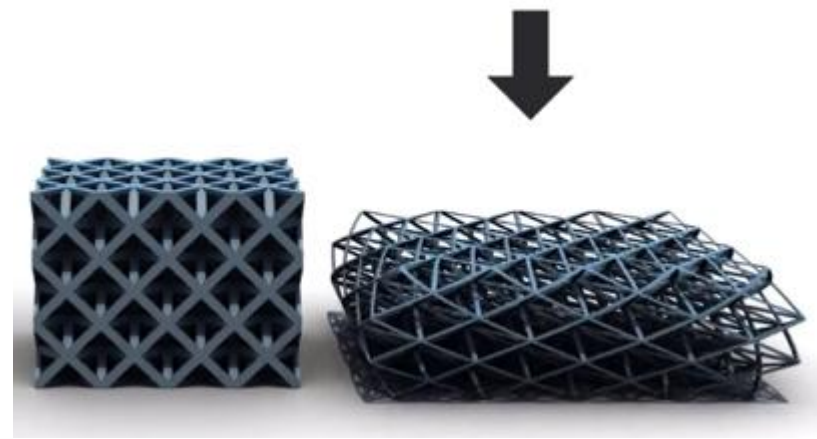
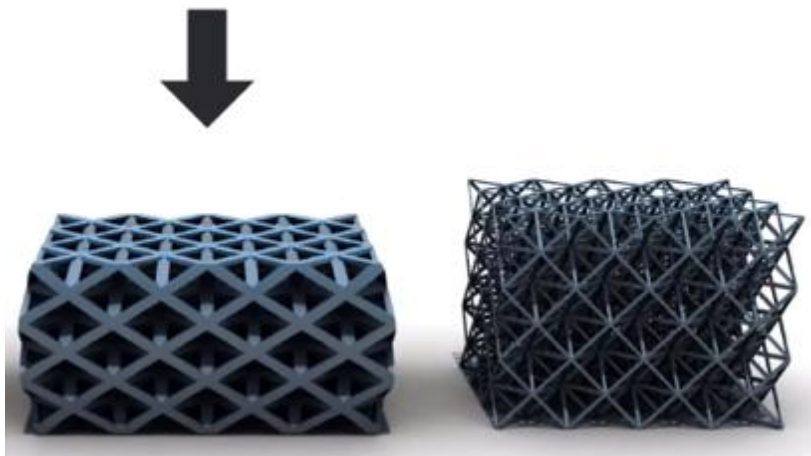
- ✓ Printing technology is for moderate-size shapes that fits into chamber.
- ✓ A related issue is to compute the tight arrangement of the parts within a container to be shipped for reassembly in the destination.



Shape Interior

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- ✓ Is a key factor regarding material use and print time.
- ✓ Inner volume grows to the cube of scaling factor, e.g., doubling object size multiplies its volume by $2^3=8$.
 - ✓ This explains interior's impact on material use and print time.
 - ✓ Varying elasticity can be achieved, e.g., by using different interior microstructs.



Shape Interior

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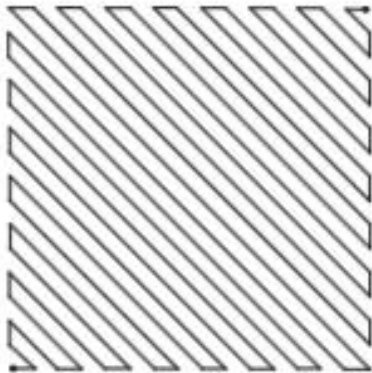


Microstructures to Control Elasticity in 3D Printing, 2015.

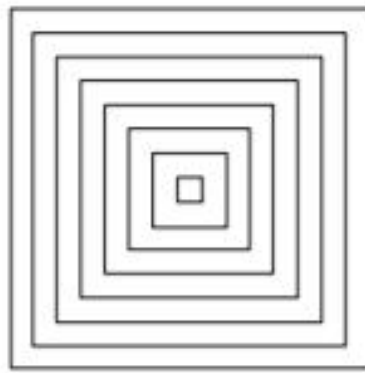
Shape Interior

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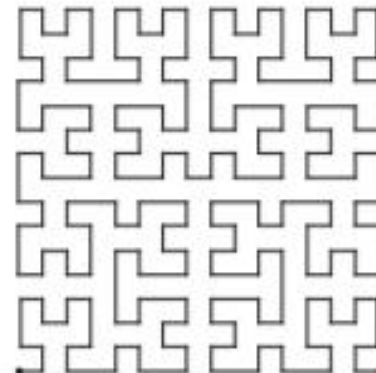
- ✓ Is a key factor regarding material use and print time.
- ✓ Aka interior support, infill.
- ✓ Raster device: produce an image of the filled layer contour; project it.
- ✓ Vector device: trickier. Nozzle/laser must follow a space filling curve when depositing/solidifying material.



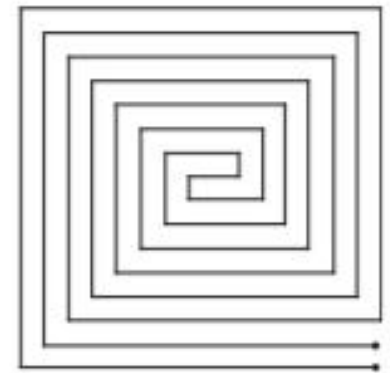
Direction parallel



Contour parallel



Hilbert curve



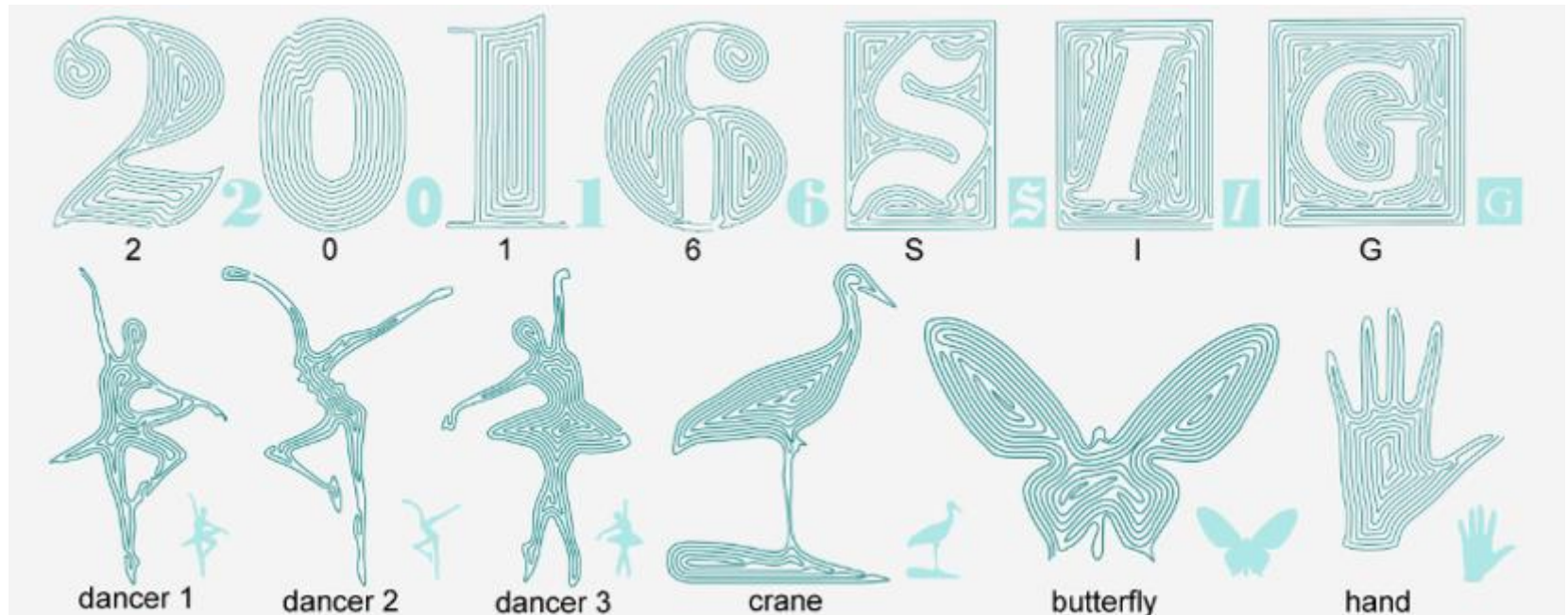
Fermat spiral

- ✓ Fermat spiral: Reduce # of sharp turns to enable faster motions and remove vibrations (beats the most common Dir parallel and Hilbert). Continuous to prevent stops and restarts (beats Con parallel).

Shape Interior

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- ✓ Is a key factor regarding material use, print time, mechanical props.
- ✓ Aka interior support, infill.
- ✓ Raster device: produce an image of the filled layer contour; project it.
- ✓ Vector device: trickier. Nozzle/laser must follow a space filling curve when depositing/solidifying material.

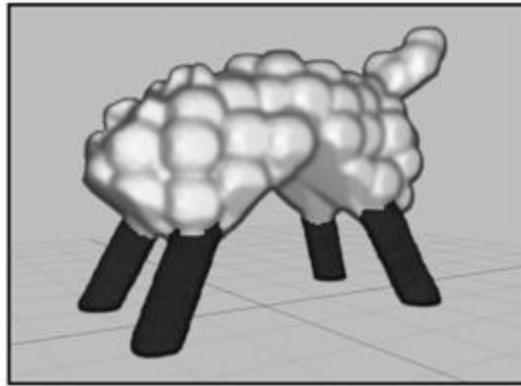
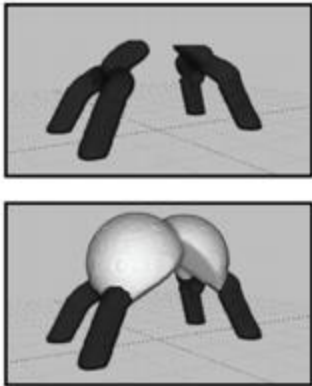


Connected Fermat spirals for layered fabrication, 2016. 17th century idea in 21st century.

Potential Project Topics / Future Work

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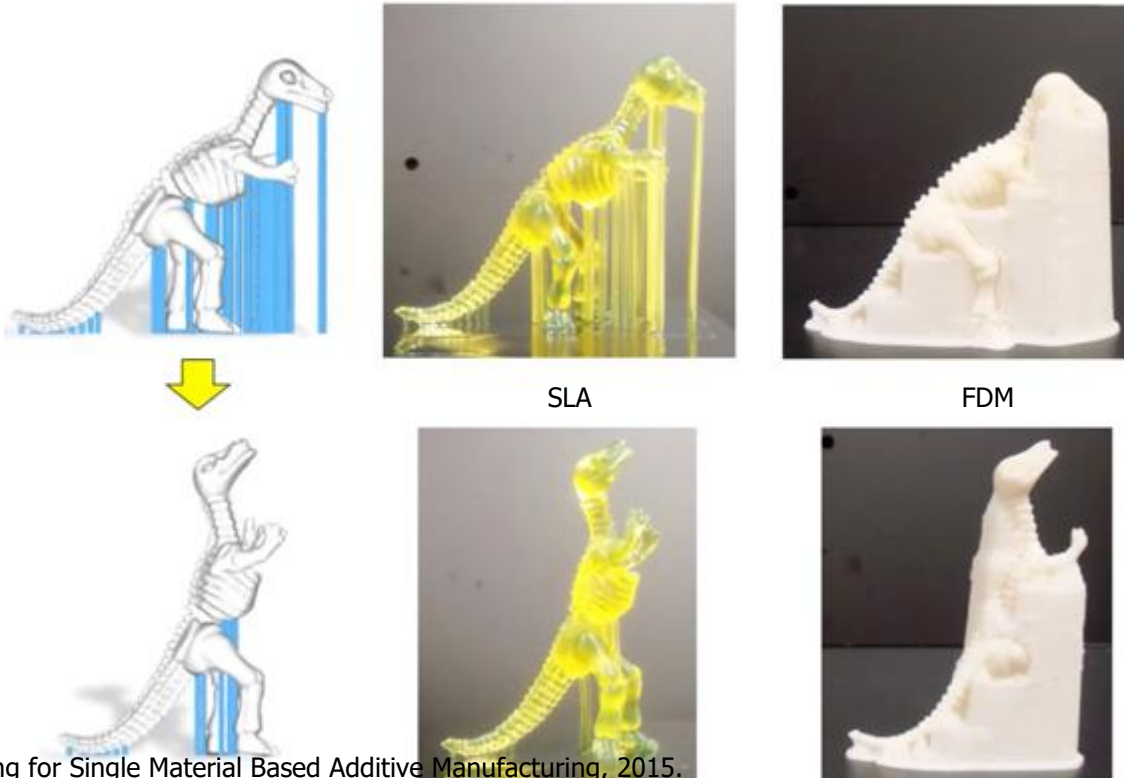
- ✓ An important open question: can we ***design*** shapes with AM in mind?
- ✓ 3D printing algorithms work on a 3D shape that is designed without AM in mind and aim to find the best way to print it to match one or some of the criteria: Cost, Fidelity, Functionality.
- ✓ It'd be better if we consider these issues during 3D design, not after.



Potential Project Topics / Future Work

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- ✓ An important open question: **design** shapes with AM in mind?
- ✓ 3D printing algorithms work on a 3D shape that is designed without AM in mind and aim to find the best way to print it to match one or some of the criteria: Cost, Fidelity, Functionality.



Potential Project Topics / Future Work

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- ✓ An important open question: put structures **on** to the surface?
- ✓ For esthetic, stability, fast prototyping.
- ✓ Current work: manual, labor-intensive, skill-based, curve primitives.
- ✓ Future work: extract patterns directly from the existing mesh facets?



Potential Project Topics / Future Work

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- ✓ An important open question: **4D** printing?
- ✓ Metamaterials that are able to morph into a target shape after being printed (4th dimension: time).

