CS410 Advanced Functional Programming 2015/16 Session

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Chapter 1

Introduction

1.1 Language and Tools

For the most part, we'll be using the experimental language, Agda Norell [2008], which is a bit like Haskell (and implemented in Haskell), but has a more expressive type system and a rather fabulous environment for typed programming. Much of what we learn here can be ported back to Haskell with a bit of bodging and fudging (and perhaps some stylish twists), but it's the programming environment that makes it worth exploring the ideas in this class via Agda.

The bad news, for some of you at any rate, is that the Agda programming environment is tightly coupled to the Emacs editor. If you don't like Emacs, tough luck. You may have a job getting all this stuff to work on whatever machines you use outside the department, but the toolchain all works fine on departmental machines.

Teaching materials, exercise files, lecture scripts, and so on, will all pile up in the repository https://github.com/pigworker/CS410-15, so you'll need to get with the git programme. You should each keep your own version of the repository, with your solutions, in a *private* repository (e.g., at https://bitbucket.org/) and invite the class staff (pigworker and jmchapman) as collaborators. Your repository is your portfolio of coursework: we will add our written feedback to it directly, in your presence. The class is small enough that we can see you each individually for a bit of a chat and some marking relatively frequently.

These notes are a work in progress. Perhaps, one day, they will be a textbook.

1.2 Lectures, Labs, Office Hours

Monday: Lecture, 11am–12pm, JA326; Office Hour, 2–3pm, LT1317; Lab, 3–5pm LT1301

Tuesday: Office Hour, 2–3pm, LT1317; Lecture, 4–5pm, LT209

Friday: Lab, 1–2pm, LT1301

Lectures are where we introduce new ideas, usually livecoding in Agda, but although we'll be as interactive as possible, lectures can be a bit of a passive experience, like television. The real learning happens in labs, where you have to turn your

understanding into stuff, so you find the gaps in your understanding and ask the questions which get you to make progress from where you are. That is why we have lots of scheduled lab time. Office hours, divided into ten minute slots with signup sheets on the door of LT1317, are your opportunity to get some one-to-one supervision, as well has the marking of your assignments. Our feedback policy is 'Come and get it!'.

We should add that the existence of designated office hours does not mean that you are otherwise unwelcome in LT1317 (or LT1310, where you can also find many Agda experts). If you turn up on spec at LT1317, the worst that can happen is that you find nobody home and then sign up for a slot.

1.3 Twitter @CS410afp

This class has a twitter feed. Largely, this is so that I can post pictures of the whiteboard. I don't use it for essential communications about class business, so you need neither join twitter nor follow this user. You can access all the relevant stuff just by surfing into http://twitter.com/CS410afp. This user, unlike my personal account, will follow back all class members who follow it, unless you ask it not to.

1.4 Hoop Jumping

CS410 Advanced Functional Programming is a level 4 class worth 20 credits. It is assessed *entirely* by coursework. Departmental policy requires class convenors to avoid deadline collisions by polite negotiation, so I've agreed the following dates for handins, as visible on the 4th year noticeboard.

A deadline officially on Friday means work submitted before we get to it on Monday is acceptable.

- Friday week 2
- Friday week 5
- Friday week 9
- Friday week 12
- Friday week 15
- Semester 2 assignment, issued immediately after fourth year project deadline, to be submitted as late as I consider practicable before the exam board

As mentioned above, marking will happen 'live' and one-to-one, in office hours on a sign-up basis.

In the 2015/16 session, final year project submission is in week 11 of semester 2, which is the last week before the Spring break. We shall be sure to arrange an orientation session for the final assignment after the project deadline but before the break. You are not expected to work in your break, but want to make sure that it can at least be useful if you do.

Semester 1 assignments are each worth 15% and marked out of 15. The semester 2 assignment is worth 25% and marked out of 25. CS410 students can thus observe directly their accumulation of marks towards their degree. It is possible to bag the 20 credits by doing the first three assignments very well, and it is not unusual to finish semester 1 in a very healthy position.

1.5 Getting Agda Going on Departmental Machines

Note that these instructions are brittle and easily broken by software 'upgrades'. We'll keep them under review and try to make them as accurate as possible.

Step 1. Use Linux. Get yourself a shell. (It's going to be that sort of a deal, all the way along. Welcome back to the 1970s.)

Step 2 for bash users. Ensure that your PATH environment variable includes the directory where Haskell's cabal build manager puts executables. Under normal circumstances, this is readily achieved by ensuring that your .profile file contains the line:

```
export PATH=$HOME/.cabal/bin:$PATH
```

After you've edited .profile, grab a fresh shell window before continuing.

Step 2 for tcsh users. Ensure that your path environment variable includes the directory where Haskell's cabal build manager puts executables. Under normal circumstances, this is readily achieved by ensuring that your .cshrc file contains the line:

```
set path = ($home/.cabal/bin $path)
```

After you've edited .cshrc, grab a fresh shell window before continuing.

Step 3. Ensure that you are in sync with the Haskell package database by issuing the command:

cabal update

Step 4. Install Agda by issuing the command:

cabal install agda

Yes, that's a lower case 'a' in 'agda'. In some situations, it may not manage the full installation in one go, delivering an error message about which package or version it has failed to install. We've found that it's sometimes necessary to do cabal install cpphs, cabal install happy, and cabal install alex separately.

Step 5. Wait.

Step 6. Wait some more.

Step 7. Assuming all of that worked just fine, set up the Emacs interactive environment with the command:

agda-mode setup; agda-mode compile

Step 8. Get this repository. Navigate to where in your file system you want to keep it and do

git clone https://github.com/pigworker/CS410-15.git

Step 9. Navigate into the repo.

cd CS410-15

Step 10. Start an emacs session involving an Agda file, e.g., by the command:

emacs Hello.agda &

The file should appear highlighted, and the mode line should say that the buffer is in Agda mode. In at least one case, this has proven problematic. To check what is going on, load the configuration file ~/.emacs and find the LISP command which refers to agda-mode locate. Try executing that command: select it with the mouse, then type ESC x, which should get you a prompt at which you can type eval-region, which will execute the selected command. If you get a message about not being able to find agda-mode, then edit the LISP command to give agda-mode the full path returned by asking which agda-mode in a shell. And if you get a bad response to which agda-mode, go back to step 2.

Step 11. When you're done, please confirm by posting a message on the class discussion forum.

1.6 Making These Notes

The sources for these notes are included in the repo (in the subdirectory imaginatively called notes) along with everything else. They're built using the excellent lhs2TeX tool, developed by Andres Löh and Ralf Hinze. This, also, can be summoned via the Haskell package manager.

cabal install lhs2tex

With that done, the default action of make is to build these notes as CS410-notes.pdf at the top level. Naughtily, we also keep the notes in the repository, so they have a steady url: github.com/pigworker/CS410-15/raw/master/CS410-notes.pdf.

1.7 Your Private Repo

You will need to keep your own private version of this repository, with your solutions. We find Bitbucket works well for this purpose: feel free to find another way to host your work, as long as we can access it. Below, we'll explain how to do it the Bitbucket way, once you have an account there.

Suppose, as per instructions that you have already cloned the class repo from GitHub. Surf into bitbucket.org/repo/import and fill in 'URL' with https://github.com/pigworker/CS410-15.git, then click import. Bitbucket will set up your private copy. Visit it and copy the download link the site offers you.

Now navigate into your local copy of the class repo. To tell it that it also has a Bitbucket version, issue the command

git remote add private $(pasted\ download\ link)$

and you should find that you can do

- git pull origin to pull from the class repo
- git pull private master to pull from your private repo
- git push private to push to your private repo

1.8 What's in Hello.agda?

It starts with a module declaration, which should and does match the filename.

```
module Hello where
```

Then, as in Haskell, we have comments-to-end-of-line, as signalled by -- with a space.

```
-- Oh, you made it! Well done! This line is a comment.
```

```
-- In the beginning, Agda knows nothing, but we can teach it about numbers.
```

Indeed, this module has not imported any others, and unlike in Haskell, there is no implicit 'Prelude', so at this stage, the only thing we have is the notion of a Set. The following data declaration creates three new things—a new Set, populated with just the values generated by its constructors.

```
data Nat : Set where
  zero : Nat
  suc : Nat -> Nat
```

We see some key differences with Haskell. Firstly, *one* colon means 'has type', rather than 'list cons'. Secondly, rather than writing 'templates' for data, we just state directly the types of the constructors. Thirdly, there's a lot of space: Agda has very simple rules for splitting text into tokens, so space is often necessary, e.g., around: or ->. It is my habit to use even more space than is necessary for disambiguation, because I like to keep things in alignment.

Speaking of alignment, we do have the similarity with Haskell that indentation after where indicates subordination, showing that the declarations of the zero and suc value constructors belong to the declaration of the Nat type constructor.

Another difference is that I have chosen to begin the names of zero and suc in lower case. Agda enforces no typographical convention to distinguish constructors from other things, so we can choose whatever names we like. It is conventional in Agda to name data-like things in lower case and type-like things in upper case. Crucially, zero, suc, Nat and Set all live in the same namespace. The distinction between different kinds of things is achieved by referring back to their declaration, which is the basis for the colour scheme in the emacs interface.

The declaration of Nat tells us exactly which values the new set has. When we declare a function, we create new *expressions* in a type, but *no new values*. Rather, we explain which value should be returned for every possible combination of inputs.

```
-- Now we can say how to add numbers.
```

```
_+N_ : Nat -> Nat -> Nat

m +N zero = m

m +N suc n = suc m +N n
```

What's in a name? When a name includes *underscores*, they stand for places you can put arguments in an application. The unspaced _+_ is the name of the function,

and can be used as an ordinary identifier in prefix notation, e.g. _+_ m n for m + n. When we use + as an infix operator (with arguments in the places suggested by the underscores), the spaces around it are necessary. If we wrote m+n by accident, we would find that it is treated as a whole other symbol.

Meanwhile, because there are no values in Nat other than those built by zero and suc, we can be sure that the definition of + covers all the possibilities for the inputs. Moreover, or rather, lessunder, the recursive call in the suc case has as its second argument a smaller number than in the pattern on the left hand side, so the recursive call is strictly simpler. Assuming (rightly, in Agda), that *values* are not recursive structures, we must eventually reach zero, so that every addition of values is bound to yield a value.

```
-- Now we can try adding some numbers.

four : Nat
four = (suc (suc zero)) + (suc (suc zero))

-- To make it go, select "Evaluate term to normal form" from the
-- Agda menu, then type "four", without the quotes, and press return.

-- Hopefully, you should get a response
-- suc (suc (suc (suc zero)))
```

Evaluation shows us that although we have enriched our expression language with things like 2+2, the values in Nat are exactly what we said they were: there are no new numbers, no error cases, no 'undefined's, no recursive black holes, just the values we declared.

That is to say, Agda is a language of *total* programs. You can approach it on the basis that things mean what they say, and—unusually for programming languages—you will usually be right.

1.9 Where are we going?

Agda is a language honest, expressive and precise. We shall use it to explore and model fundamental concepts in computation, working from concrete examples to the general structures that show up time and time again. We'll look at examples like parsers, interpreters, editors, and servers. We'll implement algorithms like arithmetic, sorting, search and unification. We'll see structures like monoids, functors, algebras and monads. The purpose is not just to teach a new language for instructing computers to do things, but to equip you with a deeper perception of structure and the articulacy to exploit that structure.

Chapter 2

Two, One, Zero, Blast Off!

The repository file CS410-Prelude. agda contains quite a lot of stuff that we'll need as we go along. Let us visit it selectively. In this chapter, we'll look at the types Two, One and Zero, which are each named after the number of values they contain.

2.1Two, the type of Boolean values

The type Two represents a choice between exactly two things, i.e., one bit of information. It is declared as follows.

```
data Two: Set where
 tt: Two
 ff: Two
```

Agda's : means 'is in', just like Haskell's ::, but shorter, that space around: is essential.

In Agda, we declare a data type with the keyword 'data', followed by an assertion which brings a type constructor into existence, in this case, Two. Specifically, we say Two: Set to mean 'Two is in Set'. Set is a built-in type in Agda: it is the type. Set is not an ordiof 'ordinary' types. The keyword 'where' introduces an indented block of further declarations, this time of data constructors, explaining which values exist in Two, namely tt and ff. In Haskell, this type is called Bool and has values True and False. I call the type Two to remind you how big it is, and I use ancient abbreviations for the constructors. We can see, clearly stated, what each of the new things is called and what types they have.

nary type. Set also has a type.

We can give more than one name the same type by listing them left of:, separated by spaces, so the whole declaration can fit on one line:

```
data Two: Set where tt ff: Two
```

Agda's cunning 'mixfix' syntax is not just for binary operators: it lets you rebuild familiar notations. We can write

```
\mathsf{if\_then\_else\_} \,:\, \big\{X \,:\, \mathsf{Set}\big\} \to \mathsf{Two} \to X \to X \to X
if b then t else f = ?
```

What have we done? We have declared the type and layout of the if-then-else construct, then given an incomplete definition of it. As in Haskell, \rightarrow associates to the right. Correspondingly, the type says that we expect to receive four inputs, an invisible Set called X, a visible element of Two, then two visible elements of X, before returning a value of type X. The invisibility of X is indicated by the braces in the type. The underscores in the name of the operator show us the places where the visible arguments go, and sure enough, there are three of them in our incomplete definition. Naming X allows us to refer to X later in the type: we say that the rest of the type depends on X. We could have named everything, writing

$$\mathsf{if_then_else_} \,:\, \{X\,:\, \mathsf{Set}\} \to (b\,:\, \mathsf{Two}) \to (t\,f\,:\, X) \to X$$

but it is often tidier to name only what is depended on.

Now hit C-c C-1 to load the file. We see that ? turns into a pair of highlighted braces (a 'hole') labelled 0,

Sometimes I call a hole a 'shed' because it's a private workspace.

if
$$b$$
 then t else $f = \{ \} \theta$

and that the other window shows the goal.

It's telling us that we must explain how to fill the braces with a value of type X: the dot is to remind us that X is not in scope. If you click between the braces and hit C-c C-comma, you will get information specific to that goal:

Goal:
$$.X$$

$$f : .X$$

$$t : .X$$

$$b : \mathsf{Two}$$

$$.X : \mathsf{Set}$$

We see the goal above the line, and the context below. The variables in scope, b, f and t, are given their types in the context. Meanwhile, we cannot see X on the left, so it is not in scope, hence its dot, but it is in the context, so types can refer to it. That tallies with the visibility information we gave in the type.

So, we need a value of type X and we have two to choose from: t and f. We can just guess. Try typing t in the hole

if
$$b$$
 then t else $f = \{t\}0$

and hit C-c C-space to say 'give the answer'. We get a completed program

if
$$b$$
 then t else $f = t$

but it probably doesn't do what we expect of if-then-else. Retreat by turning that answer back into ? and let's think again.

The role of a value in Two is to inform choices, so let us consider the value of b case by case. To inspect b, type b in the goal

if
$$b$$
 then t else $f = \{b\}0$

and hit C-c C-c. Now we have

if tt then
$$t$$
 else $f = \{ \}0$
if ff then t else $f = \{ \}1$

One line has become two, and in each, b has been replaced by one of its possible values. If you click in the lower hole, you can try another trick: hit C-c C-a. Suddenly, Agda writes some code for you.

```
if tt then t else f = \{ \}0
if ff then t else f = f
```

That keystroke is a bit like 'I feel lucky' on Google: it gives you the first well typed thing the system can find. Sadly, if you do the same thing in the top hole, you also get f. Fortunately, the C-c C-a technology can be persuaded to work a little harder Lindblad and Benke [2004]. Try typing -1 in the hole

1 for 'list'

```
if tt then t else f = \{-1\}\theta
```

and hitting C-c C-a. The other window shows a list of solutions. Now, if you type -s1 in the hole

s for 'skip', 1 for how many to skip

```
if tt then t else f = \{-s \ 1\}0
```

and hit C-c C-a, you get the finished definition:

```
if_then_else_ : \{X: \mathsf{Set}\} \to \mathsf{Two} \to X \to X \to X if tt then t else f=t if ff then t else f=f
```

Of course, you could have given the answer directly, just by typing

```
if tt then t else f = \{t\}\theta
```

and hitting C-c C-space, but in more complex situations, type-based search can really cut down effort. Moreover, the more precise a type, the more likely it is that type-based search will choose good solutions.

Let's see that for real, by defining the case analysis principle for Two.

The invisible argument is a *function*, P, from Two to Set, which means that each of P tt and P ff is a Set, so they can be used as the types of the visible arguments t and f. The rest of the function type says that whichever b: Two we get, we can deliver a value in P b. Now, if we try

```
caseTwo t f b = \{t\}0
```

and C-c C-space, it does not work! To give t, we would need to know that b is tt , and we do not. It seems there is no choice but to look at b, and no choice about the solutions in each case when we do. So, try typing $-\mathsf{c}$ in the hole

c for 'case analysis

```
\mathsf{caseTwo}\ t\ f\ b\ =\ \{\mathsf{-c}\}\theta
```

and hit C-c C-a. Literally, Agda writes the program at a stroke.

```
caseTwo : \{P: \mathsf{Two} \to \mathsf{Set}\} \to P \ \mathsf{tt} \to P \ \mathsf{ff} \to (b: \mathsf{Two}) \to P \ b caseTwo t \ f \ \mathsf{tt} = t caseTwo t \ f \ \mathsf{ff} = f
```

Think for a moment about what just happened. The type of if_then_else_ did not distinguish the type of 'what to do with tt' from 'what to do with ff', but the whole point of tt and ff is to be different from each other. Moreover, the types of the branches are the same as the types of the whole application, when the point of a conditional construct is to learn something useful. It is a type preserving transformation to swap over the 'then' and 'else' branches of every conditional in a program, or to replace the whole conditional by one of its branches: type preserving but meaning destroying! By contrast, the type of caseTwo says 'if we have a problem involving some b: Two, it is enough to consider two special cases where we know what b is'.

2.2 One, the dullest type in the universe

The type which Haskell calls () is what we will call One. Let us declare it:

```
record One : Set where constructor \langle \rangle
```

Agda has a special syntax to declare a data type with *exactly one* constructor: it is not compulsory to name the **constructor**, but here I have done so. We think of such a type as a **record**. One is the degenerate case of records where there are *no fields*. We shall have more interesting records later. The syntax **record** $\{\}$ is also permitted for the value in One.

Now, you might well be wondering why we don't use this variant:

```
data OneD: Set where (): OneD
```

and the reason is a little bit subtle.

We are permitted to write

```
caseOne : \{P: \mathsf{One} \to \mathsf{Set}\} \to P\ \langle \rangle \to (x: \mathsf{One}) \to P\ x caseOne p|x|=p
```

but it is forbidden to write

```
\begin{array}{l} \mathsf{caseOneD} \,:\, \{\,P\,:\, \mathsf{OneD} \to \mathsf{Set}\,\} \to P\,\,\langle\rangle \to (x\,:\, \mathsf{OneD}) \to P\,\,x \\ \mathsf{caseOneD}\,\, p\,\, x\,\,=\,\, p \quad -\, \mathsf{error}\,\,\langle\rangle \,\,! = x\,\,\mathsf{of}\,\,\mathsf{type}\,\,\mathsf{OneD} \end{array}
```

When the typechecker tests equality between expressions in a **data** type, it compares their normal forms: above in OneD , both $\langle\rangle$ and x cannot compute any further, and they are different, so we have a mismatch. But when the typechecker tests equality between expressions in a **record** type, it compares the normal forms of each field separately: One has no fields, so all the fields match! That is, we choose a **record** type over a **data** type whenever we can, because the typechecker is more generous when testing that records match. It is essential that Two is a **data** type, because the whole point is that its values may vary, but for One , we can treat all expressions as equal because we know there is only one value they can take.

2.3 Zero, the type of the impossible

You have seen a **record** type with no fields, where it is easy to give a value to each field: your work is over as soon as it starts. You might wonder whether it makes sense to define a **data** type with no constructors, like this:

data Zero: Set where

That definition is accepted, provided you remember to write the 'where', even though you put nothing there. We have given no constructors, so it is *impossible* to construct a value in Zero. Why is this useful?

If you're given a value in the Zero type, you are a very lucky person. You can trade it in for a value in any type you want. Let's try it.

```
\begin{array}{ll} \operatorname{magic} \ : \ \{X \ : \ \operatorname{Set}\} \to \operatorname{Zero} \to X \\ \operatorname{magic} \ z \ = \ \boxed{\{\ \}\theta } \end{array}
```

Now what happens if we do case analysis on z. Type z in the hole

$$\mathsf{magic}\; z \; = \; \{z\}\theta$$

and hit C-c C-c. When we did case analysis on Two, one line turned into two, so we might perhaps expect one line to vanish, but that would make the program invisible. What actually happens is this:

```
\mathsf{magic} \,:\, \{X\,:\, \mathsf{Set}\} \to \mathsf{Zero} \to X \mathsf{magic}\; ()
```

The program has no right-hand side! Instead, the symbol (), which you can pronounce 'impossible', points out why there is *no problem to solve*. Instead of explaining how to make an output, we explain why the function will never need to: nobody can produce its input!

In Haskell, () is the one value in the one-valued type, also (). Agda's () is rather the opposite.

Say 'impossible' or blow a raspberry!

You will find Zero useful in Exercise 1, to get out of tricky situations unscathed. You just say 'This can't be happening to me!', and all of a sudden, it isn't.

Bibliography

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16 BIBLIOGRAPHY

Appendix A

Agda Mode Cheat Sheet

I use standard emacs keystroke descriptions. E.g., 'C-c' means control-c. I delimit keystrokes with square brackets, but don't type the brackets or the spaces between the individual key descriptions.

A.1 Managing the buffer

[C-c C-l] load buffer

This keystroke tells Agda to resynchronize with the buffer contents, typechecking everything. It will also make sure everything is displayed in the correct colour.

[C-c C-x C-d] deactivate goals

This keystroke deactivates Agda's goal machinery.

[C-c C-x C-r] restart Agda

This keystroke restarts Agda.

A.2 Working in a goal

The following apply only when the cursor is sitting inside the braces of a goal.

[C-c C-,] what's going on?

If you select a goal and type this keystroke, the information buffer will tell you the type of the goal and the types of everything in the context. Some things in the context are not in scope, because you haven't bound them with a name anywhere. These show up with names Agda chooses, beginning with a dot: you cannot refer to these things, but they do exist.

[C-c C-.] more on what's going on?

This is a variant of the above which in addition also shows you the type of the expression currently typed into the hole. This is useful for trying different constructions out before giving/refining them!

[C-c C-spc] give expression

If you think you know which expression belongs in a goal, type the expression between its braces, then use this keystroke. The expression can include ? symbols, which become subgoals.

[C-c C-c] case split

If your goal is immediately to the right of =, then you're still building your program's decision tree, so you can ask for a case analysis. Type the name of a variable in the goal, then make this keystroke. Agda will try to split that variable into its possible constructor patterns. Amusingly, if you type several variables names and ask for a case analysis, you will get all the possible combinations from splitting each of the variables.

[C-c C-r] refine

If there's only one constructor which fits in the hole, Agda deploys it. If there's a choice, Agda tells you the options.

[C-c C-a] ask Agsy (a.k.a. I feel lucky)

If you make this keystroke, Agda will use a search mechanism called 'Agsy' to try and guess something with the right type. Agsy may not succeed. Even if it does, the guess may not be the right answer. Sometimes, however, there's obviously only one sensible thing to do, and then Agsy is your bezzy mate! It can be an incentive to make your types precise!

A.3 Checking and Testing things

$[C-c\ C-d]$ deduce type of expression

If you type this keystroke, you will be prompted for an expression. If the expression you supply makes sense, you will be told its type.

If you are working in a goal and have typed an expression already, Agda will assume that you want the type of that expression.

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[C-c C-n] normalize expression

If you type this keystroke, you will be prompted for an expression. If the expression you supply makes sense, you will be told its value.

If you are working in a goal and have typed an expression already, Agda will assume that you want to normalize (i.e. compute as far as possible) that expression. The normal form might not be a value, because there might be some variables in your expression, getting in the way of computation. When there are no free variables present, the normal form is sure to be a value.

A.4 Moving around

[C-c C-f]/[C-c C-b] move to next/previous goal

A quick way to get to where the action is to use these two keystrokes, which takes you to the next and previous goal respectively.

[M-.] go to definition

If you find yourself wondering what the definition of some identifier is, then you can put the cursor at it and use this keystroke – it will make Agda take you there.