

CoCaLab
Causality
Copenhagen





Causality for Distributional Robustness

DSTS 50 year anniversary

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Using Causality for Distributional Robustness

- The road from full to partial exogeneity 
- Some detours about our work 

Perfect exogeneity: Randomized experiments

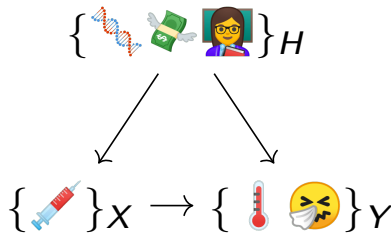
Goal: Learn effect X on Y .

$$\{\text{🪡}\}_X \rightarrow \{\text{🌡️ 🤒}\}_Y$$

Perfect exogeneity: Randomized experiments

Goal: Learn effect X on Y .

Problem: Latent confounding factors H .

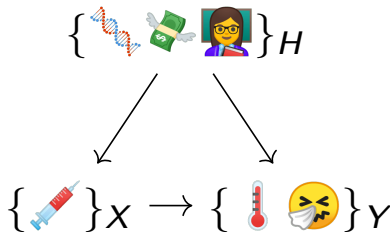


Perfect exogeneity: Randomized experiments

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Problem: Latent confounding factors H .

Solution: Use randomization to break confounding.



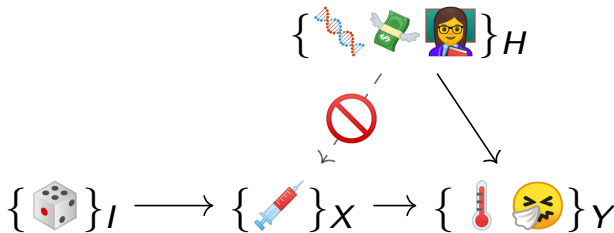
Why care about causal instead of confounded effect? **Generalization!**

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Why care about causal instead of confounded effect? **Generalization!**

Enough exogeneity: Instrumental variables

We can't always randomize:

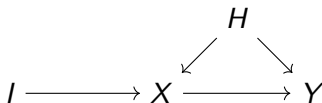
- Allocation unethical (e.g. smoking  or seatbelts )
- Interventions hard to define (e.g. data is pixels of image )

Enough exogeneity: Instrumental variables

We can't always randomize:

- Allocation unethical (e.g. smoking 🚬 or seatbelts 🔥)
- Interventions hard to define (e.g. data is pixels of image 🖼️)

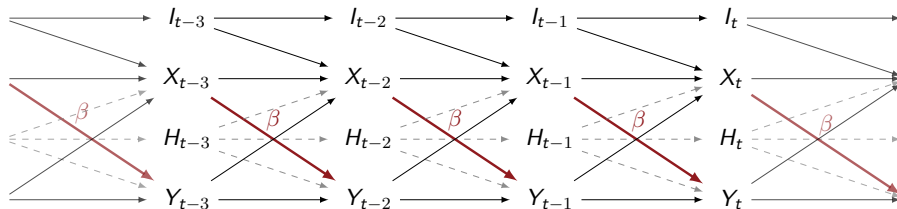
Instead: Instrumental variable (IV): I 1) independent of H and 2) only indirect effect on Y



OLS regression: $Y - X\hat{\beta} \perp\!\!\!\perp X \longrightarrow$ **IV** regression: $Y - X\hat{\beta} \perp\!\!\!\perp I$.

\rightarrow Causal effect β can still be estimated (Imbens and Rubin 2015) under assumptions, e.g. high rank I .

Detour 1: Instruments in time series



Currently, we are working on methods in systems with memory

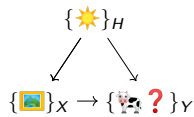
- Proper adjustment for memory
- Using also lagged instruments as instruments, to increase rank of instrument, (Thams et al. 2021).

Some exogeneity: Invariance

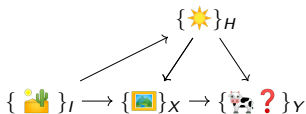


$$\{\text{🖼️}\}_X \rightarrow \{\text{🐮?}\}_Y$$

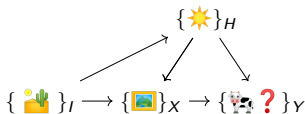
Some exogeneity: Invariance



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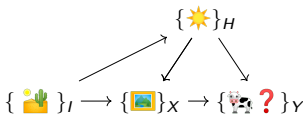


Some exogeneity: Invariance



- Causal solution: $Y - X\beta \perp\!\!\!\perp I$. IV require $\dim(I) \geq \dim(X)$.
Image data: $\dim(X) = 1024^2$.

Some exogeneity: Invariance

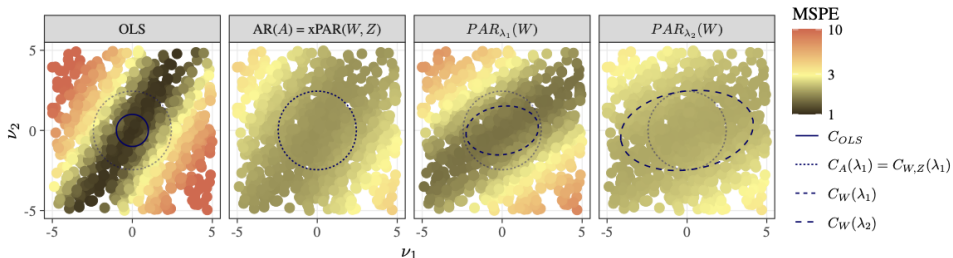


- Causal solution: $Y - X\beta \perp\!\!\!\perp I$. IV require $\dim(I) \geq \dim(X)$.
Image data: $\dim(X) = 1024^2$.
- Instead, we can penalize our regression

$$\hat{\beta} \in \arg \min_{\beta} \|Y - X\beta\|^2 + \lambda \|\text{cov}(Y - X\beta, I)\|^2,$$

Rothenhäusler et al. 2021 show that $\hat{\beta}$ **generalizes** well (but less than with full causal knowledge).

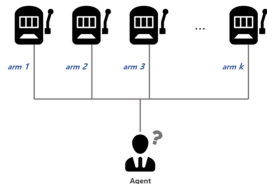
Detour 2: Generalization with proxy variables



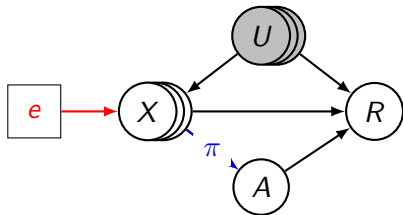
In Oberst et al. 2021, we show that

- If I is unobserved, but we have a noisy measurement (proxy) W of I , we still obtain generalization, although less.
- If we observe two proxies W, Z of I , we generalize as well as with I itself.

Detour 3: Using environments to generalize in decision making






Contextual (= covariates) + Bandits



In Saengkyongam et al. 2021,

- We develop **invariant policies**, that is policies that do not use confounded features.
- To do so, we use exogeneous environments, e.g. hospitals.
- Under assumptions, we generalize to new environments.

Conclusions

- If strong exogeneity is present, we can estimate causal effects 
- If weak exogeneity is present, we can not estimate causal effects, but still get methods that generalize better 
- We considered linear effects, but much can be generalized to non-linear functions  (Christiansen et al. 2021)

References I

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- Imbens, Guido W and Donald B Rubin (2015). *Causal inference in statistics, social, and biomedical sciences*. Cambridge University Press.
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- Oberst, Michael, Nikolaj Thams, Jonas Peters, and David Sontag (2021). “Regularizing towards Causal Invariance: Linear Models with Proxies”. In: *Proceedings of the 38th International Conference on Machine Learning*. Vol. 139. Proceedings of Machine Learning Research. PMLR, pp. 8260–8270.
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- Rothenhäusler, Dominik, Nicolai Meinshausen, Peter Bühlmann, and Jonas Peters (2021). “Anchor regression: Heterogeneous data meet causality”. In: *Journal of the Royal Statistical Society: Series B (Statistical Methodology)* 83.2, pp. 215–246.
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- Saengkyongam, Sorawit, Nikolaj Thams, Jonas Peters, and Niklas Pfister (2021). “Invariant Policy Learning: A Causal Perspective”. In: *arXiv preprint arXiv:2106.00808*.

References II



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Questions?