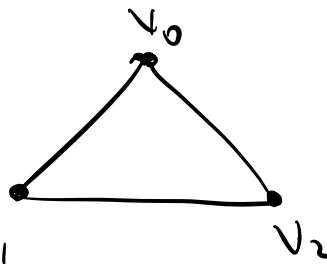


$$\sigma = v_0 v_1 v_2$$

$$K_\sigma = \{\text{faces of } \sigma\}$$



$$C_0(K_\sigma) = \{n_0 v_0 + n_1 v_1 + n_2 v_2 \mid n_i \in \mathbb{Z}\}$$

free abelian group generated by
0 simplices

$$\cong \mathbb{Z}_3$$

$$C_1(K_\sigma) = \left\{ \begin{array}{l} n_0 [v_0, v_1] + n_1 [v_1, v_0] + n_2 [v_0, v_2] \\ + n_3 [v_2, v_0] + n_4 [v_1, v_2] + n_5 [v_2, v_1] \end{array} \right. \\ \text{st } n_i \in \mathbb{Z}$$

$$\left\langle [v_0, v_1] + [v_1, v_0], [v_1, v_2] + [v_2, v_1], [v_0, v_2] + [v_2, v_0] \right\rangle$$

$$\text{in } C_2(K_\sigma) \quad [v_0, v_1] = -[v_1, v_0]$$

$$C_1(K_\sigma) \cong \mathbb{Z}^3 \quad \text{a basis}$$

$$\{[v_0, v_1], [v_0, v_2], [v_1, v_2]\} \quad C_2(K_\sigma) \cong \mathbb{Z}$$