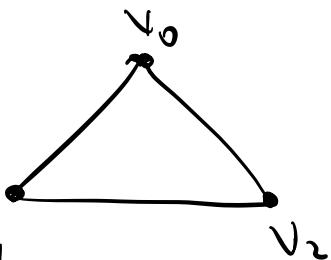


$$\sigma = v_0 v_1 v_2$$



$$K_\sigma = \{ \text{faces of } \sigma \} \cup \{v_1, v_2\}$$

$$C_0(K_\sigma) = \{ n_0 v_0 + n_1 v_1 + n_2 v_2 \mid n_i \in \mathbb{Z} \}$$

free abelian group generated by
8 simplices

$$\cong \mathbb{Z}_3$$

$$C_1(K_\sigma) = \underbrace{\left\{ n_0 [v_0, v_1] + n_1 [v_1, v_0] + n_2 [v_0, v_2] + n_3 [v_2, v_0] + n_4 [v_1, v_2] + n_5 [v_2, v_1] \right.}_{\text{if } n_i \in \mathbb{Z}}$$

$$\left\langle [v_0, v_1] + [v_1, v_0], [v_1, v_2] + [v_2, v_1], [v_0, v_2] + [v_2, v_0] \right\rangle$$

$$\text{in } C_2(K_\sigma) \quad [v_0, v_1] = -[v_1, v_0]$$

$$C_1(K_\sigma) \cong \mathbb{Z}^3 \quad \text{and} \quad b_{\text{tors}}$$

$$\{ [v_0, v_1], [v_0, v_2], [v_1, v_2] \} \quad C_2(K_\sigma) \cong \mathbb{Z}$$