

# A very Simple

Anders Kinch

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## 1

**Definition.** *1.1 Fields*

**Definition.** *1.2 Vector spaces*

**Definition.** *1.4 Subspaces*

**Definition 1.** *1.5 Linear combination*

**Definition 2.** *1.7 Span*

**Definition 3.** *1.9 Linear dependence*

**Definition 4.** *1.12 Basis*

**Definition 5.** *1.14 Coordinate*

## 2 2. Linearity

**Definition 6.** *2.1 Linear map*

**Definition 7.** *2.4 Null-space and Range*

**Definition 8.** *2.6 Isomorphisms*

**Definition 9.** *2.13 Quotient space*

**Definition 10.** *2.15 Quotient map*

**Definition 11.** *2.16 Invariant*

**Definition 12.** *2.18 Nullity and rank*

**Definition 13.** *2.21 Matrix*

**Definition 14.** *2.23 Product*

**Definition 15.** *2.24 Algebra (bilinear map)*

### 3 3. Duality

**Definition 16.** *3.1 Dual space*

**Definition 17.** *3.3  $i$ 'th coordinate functional*

**Definition 18.** *3.7 Annihilator*

**Definition 19.** *3.12 Adjoint*

**Definition 20.** *3.19 Double dual*

**Definition 21.** *3.21 Natural correspondence*

### 4 4. Bilinear maps

**Definition 22.** *4.1 Bilinear map*

**Definition 23.** *4.3 Multilinear map*

**Definition 24.** *4.6 Symmetry and skew-symmetry*

**Definition 25.** *4.7 Alternating*

**Definition 26.** *4.9 Quadratic form*

**Definition 27.** *4.11 Orthogonal*

**Definition 28.** *4.14 non-degenerate*

**Definition 29.** *4.15 Symplectic*

**Definition 30.** *4.17 Positive and negative definite*

**Definition 31.** *4.19 Quadrics and conics*

## 5 5. Sums and products

**Definition 32.** *5.1 Direct sum*

**Definition 33.** *5.5 Complement*

**Definition 34.** *5.9 (external) Direct sum*

**Definition 35.** *5.10 Projection*

**Definition 36.** *5.12 idempotent*

**Definition 37.** *5.14 Tensor product*

**Definition 38.** *5.18 Pair*

## 6 6. Eigendecomposition

**Definition 39.** *6.1 Eigenspace*

**Definition 40.** *6.2 Spectrum and (geometric) multiplicity*

**Definition 41.** *6.3 Polynomial*