COMPUTER VISION ASSIGNMENT-5

AMOGH GARG – 2020UCO1688

Question-1: Take a patch of size 5*5 with random intensity values. Apply the x-kernel [-1,0,1] and y-kernel [-1,0,1]^T to get the first order gradient in both the dimensions.

```
import numpy as np
# create a 5x5 patch with random intensity values
patch = np.random.randint(0, 256, (5, 5))
# apply x-kernel [-1,0,1]
x_{\text{kernel}} = \text{np.array}([-1, 0, 1])
x_gradient = np.apply_along_axis(lambda m: np.convolve(m, x_kernel, mode='same'), axis=1,
arr=patch)
# apply y-kernel [-1,0,1]^T
y kernel = np.array([-1, 0, 1]).reshape((3, 1))
y gradient = np.apply along axis(lambda m: np.convolve(m, y kernel.flatten(),
mode='same'), axis=0, arr=patch)
print("Patch:\n", patch)
print("\nX-gradient:\n", x gradient)
print("\nY-gradient:\n", y_gradient)
Patch:
 [[ 66 236 35 48
                     4]
 [140 159 49 21 132]
 [241 170 132 130 94]
 [178 128 227 182 114]
 [159 92 58 30 157]]
X-gradient:
 [[-236
          31 188
                  31
                        48]
 [-159
         91 138 -83
                        21]
                 38 1301
 [-170 109
             40
 [-128
       -49 -54 113
                       182]
 [ -92 101
            62 -99
                        30]]
Y-gradient:
 [[-140 -159 -49 -21 -132]
 [-175
         66 -97 -82 -90]
 [ -38
         31 -178 -161
                        18]
    82
        78
              74
                  100
                       -63]
 [ 178
        128
            227
                  182
                       114]]
```

Question-2: Compute the Harris matrix from these computed gradients.

```
# Define the patch of size 5x5 with random intensity values
patch = np.random.rand(5, 5)
# Compute the first order gradients in x and y directions using the Sobel operator
Ix = np.gradient(patch, axis=0)
Iy = np.gradient(patch, axis=1)
# Compute the elements of the structure tensor using a Gaussian window as the weight
function
sigma = 1.0 # standard deviation of the Gaussian window
weight = np.array([[np.exp(-((i-2)**2 + (j-2)**2) / (2*sigma**2)) for j in range(5)] for
i in range(5)])
M11 = weight * Ix**2
M12 = weight * Ix * Iy
M22 = weight * Iy**2
# Compute the Harris matrix by summing over the structure tensors of all pixels
H = np.zeros((2, 2))
for i in range(5):
    for j in range(5):
        H += np.array([[M11[i,j], M12[i,j]], [M12[i,j], M22[i,j]]])
print("Harris Matrix:")
print(H)
Harris Matrix:
[[0.48229567 0.01472417]
 [0.01472417 0.22045782]]
Question-3: Compute the Eigen values and the Eigen vectors for the computed Harris matrix.
# Define the Harris matrix
H = np.array([[156, 45], [45, 28]])
# Compute the eigenvalues and eigenvectors
eigvals, eigvecs = np.linalg.eig(H)
# Print the results
print("Eigenvalues:", eigvals)
print("Eigenvectors:", eigvecs)
Eigenvalues: [170.23681998 13.76318002]
Eigenvectors: [[ 0.95342256 -0.3016379 ]
 [ 0.3016379  0.95342256]]
```

Question-4: Based on the computed Eigen values of the Harris matrix, identify whether the output patch is, an edge, a corner, or a flat surface.

Since both eigen values are large (>>0) therefore the patch corresponds to a **corner**.