

ReadMe

Programming Language Used: C++

Library Used: Bits/stdc++.h

Logic Used: 1. Standard input is taken in the form of ordered pairs like (1,1), (2,2) etc.

2. Relation is represented in the form of the matrix and $a[i][j]=1$ if (i,j) belongs to the relation R, else $a[i][j]=0$.

3. If relation is reflexive (all diagonal elements are 1), antisymmetric (if $a[i][j]=1$ then $a[j][i]=0$), and transitive ($a[i][j]=1$ and $a[j][k]=1$ then $a[i][k]$ is also 1) then it is a poset.

4. If every 2 elements of poset have LUB and GLB then it is a lattice.

5. For every 2 elements of a poset to have LUB and GLB they must be comparable. If they are incomparable, they can't have LUB and GLB.

How to compile- Copy the given code as it is on any online C++ compiler and run the program and give the inputs. Link for one online compiler is- https://www.onlinegdb.com/online_c++_compiler

OR

Copy the code on any IDE with C++ compiler installed on your computer. Build the program and run.

Code Screen Shot-

```
//Amogh Garg-2020UC01688
#include<bits/stdc++.h>
using namespace std;

int main(){
    //Entering number of ordered pairs
    int N;
    cout<<"Enter the number of ordered pairs:";
    cin>>N;
    //Creating a 2-D matrix for representing relation
    int arr[4][4]={0}; //Initially all elements of matrix are 0
    //Domain set A={0,1,2,3}
    //Entering the ordered pairs and storing them in matrix
    for(int i=0;i<N;i++){
        int a,b;
        cout<<"Enter the elements of ordered pair:";
        cin>>a;
        cin>>b;
        arr[a][b]=1; //Representing relation in the matrix
    }
    //Checking for Poset
    //1.Reflexivity
    bool isreflexive= true;
    for(int i=0;i<4;i++){
        if(arr[i][i] == 0){ //If (a,a) not in matrix -> Not reflexive
            isreflexive= false;
            break;
        }
    }
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    }
}
if(isreflexive){
    cout<<"The relation is Reflexive!"<<endl;
}
else{
    cout<<"The relation is NOT Reflexive!"<<endl;
}
//2.Anti-Symmetry
bool isantisymm= true;
for(int i=0;i<4;i++){
    for(int j=0;j<4;j++){
        if(i!=j && arr[i][j]==1 && arr[j][i]==1){ //If (a,b) in R then (b,a) in R only if a=b
            isantisymm=false;
            break;
        }
    }
}
if(isantisymm){
    cout<<"The relation is AntiSymmetric!"<<endl;
}
else{
    cout<<"The realtion is NOT AntiSymmetric!"<<endl;
}
//3.Transitivity
bool istransitive= true;
for(int i=0;i<4;i++){
    for(int j=0;j<3;j++){
        for(int i=0;i<4;i++){
            for(int j=0;j<3;j++){
                for(int k=j+1;k<4;k++){
                    //If (a,b) in R and (b,c) in R then (a,c) also in R
                    if(arr[i][j]==1 && arr[j][k]==1 && arr[i][k] != 1){
                        istransitive= false;
                    }
                }
            }
        }
    }
}
if(istransitive){
    cout<<"The relation is Transitive!"<<endl;
}
else{
    cout<<"The relation is NOT Transitive!"<<endl;
}
// If all conditions are true then it is POSET
if(istransitive && isantisymm && isreflexive){
    cout<<"The set is a POSET!"<<endl;
}
//If set is not POSET then it is not a LATTICE also
else{
    cout<<"The set is neither POSET nor LATTICE!"<<endl;
    //End program
    return 0;
}
//Checking for LATTICE-> Every 2 elements must be comparable
//Checking whether every 2 elements are comparable or not

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int l[4]={0},g[4]={0};
for(int i=0;i<4;i++){
    for(int j=0;j<4;j++){
        if(arr[i][j]==1){
            switch(i){
                case 0:l[0]++;break;
                case 1:l[1]++;break;
                case 2:l[2]++;break;
                case 3:l[3]++;break;
            }
            switch(j){
                case 0:g[0]++;break;
                case 1:g[1]++;break;
                case 2:g[2]++;break;
                case 3:g[3]++;break;
            }
        }
    }
}
//Check condition
bool x=false,y=false;
for(int i=0;i<4;i++){
    if(l[i]==4){
        x=true;
    }
    if(g[i]==4){
        y=true;
    }
}
//Printing

```

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    x=true;
}
if(g[i]==4){
    y=true;
}
}
//Printing
if(x && y){ //If x and y both are true->All elements are comparable pairwise
    cout<<"The given poset is LATTICE"<<endl;
}
else{
    cout<<"The given poset is NOT A LATTICE!"<<endl;
}

return 0;
}

```

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