

# Multivariate Normal Distribution

Also called **Multivariate Gaussian Distribution** which just a generalization of the **one-dimensional normal distribution**, It models **joint Distributions** of multiple continuous  $X$  variables :

$$\frac{1}{(2\pi)^{d/2} |\Sigma|^{1/2}} e^{-\frac{1}{2}(X-\mu)^T \Sigma^{-1} (X-\mu)}$$

- $d$  is the dimension of the vectors
- $\Sigma$  the covariance matrix **generalization** of  $\sigma^2$  the variance, its consist of the **Covariances and Variances** of the predictors  $X$
- We take the **determinant** of  $\Sigma$  cause it gives us the factor by which arrays are scaled by this **Covariance Matrix**
- $X^T X = \text{Scalar value}$
- $\Sigma^{-1}$  cause in the **one-dim** normal distribution we divide by  $\frac{1}{2\sigma^2}$
- $\mu$  is a vector of the expected values for each  $X_i$