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In [1]: import numpy as np
        # Load data set and code labels as 0 = 'NO', 1 = 'DH', 2 = 'SL'
        labels = [b'NO', b'DH', b'SL']
        data = np.loadtxt('spine-data.txt', converters={6: lambda s: labels.index(s)})

In [2]: X, y = data[:, :6], data[:, 6]

In [3]: from sklearn.model_selection import train_test_split
        X_train, X_test, y_train, y_test = train_test_split(X, y, train_size = 250, test

In [5]: ## Computes squared Euclidean distance between two vectors.
        def l2_dist(x,y):
            return np.sum(np.square(x-y))

In [6]: def l1_dist(x,y):
        return np.sum(np.abs(x-y))

In [7]: ## Takes a vector x and returns the index of its nearest neighbor in X_train
        def find_NN(x, dist="l2"):
            if(dist=="l2"):
                # Compute distances from x to every row in train_data
                distances = [l2_dist(x,X_train[i,]) for i in range(len(y_train))]
            else:
                distances = [l1_dist(x,X_train[i,]) for i in range(len(y_train))]
            return np.argmin(distances)

        ## Takes a vector x and returns the class of its nearest neighbor in X_train
        def NN_classifier(x, distance="l2"):
            # Get the index of the nearest neighbor
            if(distance=="l2"):
                index = find_NN(x, "l2")
            else:
                index = find_NN(x, "l1")
            # Return its class
            return y_train[index]

```

2 a) What error rates do you get on the test set for each of the two distance functions?

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In [8]: ## Predict on each test data point with l2 distance
        test_predictions_l2 = [NN_classifier(X_test[i,], "l2") for i in range(len(y_test))

        ## Predict on each test data point with l1 distance
        test_predictions_l1 = [NN_classifier(X_test[i,], "l1") for i in range(len(y_test))

In [9]: ## Compute the error with l2 distance
        err_positions = np.not_equal(test_predictions_l2, y_test)
        error = float(np.sum(err_positions))/len(y_test)

        print("Error of nearest neighbor classifier with l2 distance: ", error)

```

Error of nearest neighbor classifier with l2 distance: 0.23333333333333334

In [10]:

```
## Compute the error with l1 distance
err_positions = np.not_equal(test_predictions_l1, y_test)
error = float(np.sum(err_positions))/len(y_test)

print("Error of nearest neighbor classifier with l1 distance: ", error)
```

Error of nearest neighbor classifier with l1 distance: 0.21666666666666667

2 b) For each of the two distance functions, give the confusion matrix of the NN classifier.

In [11]:

```
import numpy as np

#initializing 10x10 matrix with just zeroes.
dimensions = (3, 3)
confusion_matrix_l2 = np.zeros(dimensions)
#Looping through original test labels and test predictions to create confusion m
for a, b in zip(y_test, test_predictions_l2):
    confusion_matrix_l2[int(a)][int(b)] = confusion_matrix_l2[int(a)][int(b)] +
    #print(str(a)+" "+str(b))

#printing the 10x10 confusion matrix
print("Confusion matrix with l2 distance:")
confusion_matrix_l2
```

Confusion matrix with l2 distance:

Out[11]:

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array([[12.,  1.,  3.],
       [ 9.,  9.,  0.],
       [ 1.,  0., 25.]])
```

For l2 distance :

- label 0 i.e NO (Normal) was misclassified 4 times
- label 1 i.e DH (herniated disk) was misclassified 9 times
- label 2 i.e SL (spondilololsthesis) was misclassified 1 time

In [12]:

```
import numpy as np

#initializing 10x10 matrix with just zeroes.
dimensions = (3, 3)
confusion_matrix_l1 = np.zeros(dimensions)
#Looping through original test labels and test predictions to create confusion m
for a, b in zip(y_test, test_predictions_l1):
    confusion_matrix_l1[int(a)][int(b)] = confusion_matrix_l1[int(a)][int(b)] +
    #print(str(a)+" "+str(b))

#printing the 10x10 confusion matrix
print("Confusion matrix with l1 distance:")
confusion_matrix_l1
```

Confusion matrix with l1 distance:

Out[12]:

```
array([[14.,  0.,  2.],
       [ 9.,  9.,  0.],
       [ 1.,  1., 24.]])
```

For l1 distance :

- label 0 i.e NO (Normal) was misclassified 2 times
- label 1 i.e DH (herniated disk) was misclassified 9 times
- label 2 i.e SL (spondilololsthesis) was misclassified 2 times

In []: