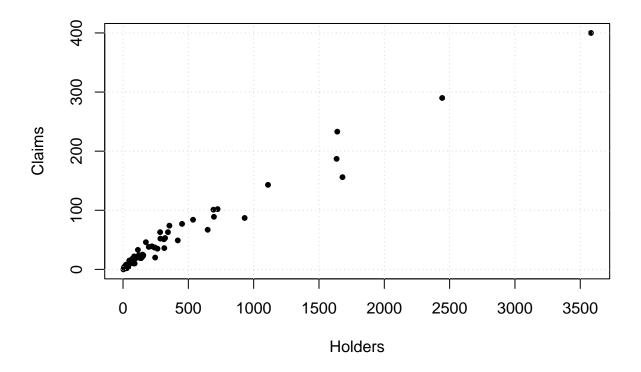
Modelling insurance claims Problem 4

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Let's load the dataset and plot a graph of the concerned variables:



Model 1: Linear regression with normally distributed errors

Let's fit this model to the Insurance dataset.

Model 2: Linear regression with Laplace distributed errors

```
NLL_Model2 <- function(theta, y, X)
{
  beta_0 = theta[1]
  beta_1 = theta[2]
  sigma = exp(theta[3]) # variance of error terms</pre>
```

```
n = length(data)
# Log likelihood function of Laplace distribution
l = -(n*log(2*sigma) + 1/sigma*sum(abs(y - beta_0 - beta_1*X)))
return(-1)
}
```

Let's fit this model to the Insurance dataset.

[1] "Estimated sigma: 371.708118099566"

Model 3: Linear regression for log-normally distributed data

```
NLL_Model3 <- function(theta, y, X)
{
  beta_0 = theta[1]
  beta_1 = theta[2]
  sigma = exp(theta[3]) # variance of error terms

n = length(data)
# -ve log likelihood function of log-normal distribution
# Mean is given in question

l = 0
for (i in 1:n)
{
  if (y[i] != 0)
  {
</pre>
```

Let's fit this model to the Insurance dataset.

[1] "Estimated sigma: 1.50358387830253e-15"

BIC analysis

The Bayesian information criterion (BIC) is a criterion for model selection among a finite set of models. It is based, in part, on the likelihood function and it is closely related to the Akaike information criterion (AIC).

Suppose that we have a statistical model of some data. Let k be the number of estimated parameters in the model. Let L be the maximized value of the likelihood function for the model and n be the total number of data points. Then the BIC value of the model is the following:

$$BIC = k \ln(n) - 2 \ln L$$

Given a set of candidate models for the data, models with lower BIC are generally preferred.

Let's define the BIC function:

```
get_BIC <- function(optim_fit, data=Insurance) {
  log(nrow(data)) * length(optim_fit$par) + 2 * optim_fit$value
}</pre>
```

Let's calculate BIC:

```
library(dplyr)
BIC_scores <- tibble(
    BIC_model1 = get_BIC(fit_1),
    BIC_model2 = get_BIC(fit_2),
    BIC_model3 = get_BIC(fit_3),
)

BIC_scores

## # A tibble: 1 x 3
## BIC_model1 BIC_model2 BIC_model3
## <dbl> <dbl> <dbl> <dbl>
## 1 511. 28.4 -46.7
```