

## Transformadas de Laplace

$F(t)$	$\mathcal{L}\{F(t)\} = f(s)$
1	$\frac{1}{s}, s > 0$
t	$\frac{1}{s^2}, s > 0$
$t^n \quad n=1,2,3\dots$	$\frac{n!}{s^{n+1}}, s > 0$
$t^n \quad n > -1$	$\frac{\Gamma(n+1)}{s^{n+1}}, s > 0$
$\sqrt{t}$	$\frac{\sqrt{\pi}}{2} s^{-\frac{3}{2}}$
$\frac{1}{\sqrt{t}}$	$\sqrt{\pi} s^{-\frac{1}{2}}$
$e^{at}$	$\frac{1}{s-a}, s > a$
$\text{sen } at$	$\frac{a}{s^2 + a^2}, s > 0$
$\text{cos } at$	$\frac{s}{s^2 + a^2}, s > 0$
$\text{sen } h(at)$	$\frac{a}{s^2 - a^2}, s >  a $
$\text{cos } h(at)$	$\frac{s}{s^2 - a^2}, s >  a $
$e^{at} \text{sen}(wt)$	$\frac{w}{(s-a)^2 + w^2}, s > a$

$F(t)$	$\mathcal{L}\{F(t)\} = f(s)$
$e^{at} \cos(wt)$	$\frac{s-a}{(s-a)^2 + w^2}, s > a$
$t \sin(wt)$	$\frac{2ws}{(s^2 + w^2)^2}, s > 0$
$t \cos(wt)$	$\frac{s^2 - w^2}{(s^2 + w^2)^2}, s > 0$
$[F'(t)]$	$s \mathcal{L}[F(t)] - F(0)$
$[F''(t)]$	$s^2 \mathcal{L}[F(t)] - sF(0) - F'(0)$
$[F^n(t)]$	$s^n [F(t)] - s^{n-1} F(0) - s^{n-2} F'(0) - \dots - F^{n-1}(0)$

$$\mathcal{L}(F(t)) = f(s) \Rightarrow \frac{-d}{ds} F(s) = \mathcal{L}(t F(t))$$

$$f * g = \int_0^t f(u) g(t-u) du$$

$$\mathcal{L}\left(\int_0^t F(u) G(t-u) du\right) = f(s) \bullet g(s)$$

$$\mathcal{L}^{-1}[f(s) \bullet g(s)] = \int_0^t F(u) G(t-u) du = F * G$$

$$\mathcal{L}^{-1}\left[\frac{f(s)}{s}\right] = \int_0^t f(\theta) d\theta$$

### Escalón

$$\mathcal{L}[U_a(t)] = \frac{e^{-as}}{s}$$

### Segundo teorema de traslación

$$\mathcal{L}[f(t-a) \mu_a(t)] = e^{-as} F(s)$$

$$\mathcal{L}^{-1}[e^{-as} F(s)] = f(t-a) \mu_a(t)$$