

$$\mathcal{L}\{e^{2t} \sinh 3t - t^2 e^{-4t} + e^t \cos 4t\}$$

$$= \mathcal{L}\{e^{2t} \sinh 3t\} - \mathcal{L}\{t^2 e^{-4t}\} + \mathcal{L}\{e^t \cos 4t\}$$

$$= \mathcal{L}\{\sinh 3t\} \Big|_{s \rightarrow s-2} - \mathcal{L}\{t^2\} \Big|_{s \rightarrow s+4} + \mathcal{L}\{\cos 4t\} \Big|_{s \rightarrow s-1}$$

$$= \frac{3}{s^2 - 9} \Big|_{s \rightarrow s-2} - \frac{2}{s^3} \Big|_{s \rightarrow s+4} + \frac{s}{s^2 + 16} \Big|_{s \rightarrow s-1}$$

$$= \frac{3}{(s-2)^2 - 9} - \frac{2}{(s+4)^3} + \frac{s-1}{(s-1)^2 + 16}$$