

$$\mathcal{L}\left\{t^2 \int_0^t \sin(3u) du\right\}$$

$$\frac{d^2}{ds^2} \mathcal{L}\left\{\int_0^t \sin(3u) du\right\}$$

$$f(t) = \sin(3t) \quad g(t) = 1$$

$$\frac{d^2}{ds^2} (\mathcal{L}\{\sin(3t)\} \cdot \mathcal{L}\{1\})$$

$$\frac{d^2}{ds^2} \left(\frac{3}{s^2 + 3^2} \cdot \frac{1}{s} \right)$$

$$\frac{d^2}{ds^2} \left(\frac{3}{s(s^2 + 9)} \right)$$

$$= \frac{d}{ds} \left(\frac{(3)' \cdot (s^3 + 9s) - 3 \cdot (s^3 + 9s)'}{[s(s^2 + 9)]^2} \right) = \frac{d}{ds} \left(\frac{-3(3s^2 + 9)}{s^2(s^2 + 9)^2} \right)$$

$$= \frac{d}{ds} \left(\frac{-9s^2 - 27}{s^2(s^2 + 9)^2} \right) = \frac{[-9s^2 - 27]' \cdot [s^2(s^2 + 9)^2] - [-9s^2 - 27] \cdot [s^2(s^2 + 9)^2]'}{[s^2(s^2 + 9)^2]^2}$$

$$= \frac{[-18s][s^2(s^2 + 9)^2] - (-9s^2 - 27)(2s(s^2 + 9)^2 + 2s^2(s^2 + 9)[s^2 + 9])}{s^4(s^2 + 9)^4}$$

$$= \frac{-18s^3(s^2 + 9)^2 - (-9s^2 - 27)(2s(s^2 + 9)^2 + 4s^3(s^2 + 9))}{s^4(s^2 + 9)^4}$$

$$= \frac{2(-9s^2 - 27)}{s^3(s^2 + 9)^2} - \frac{18}{s(s^2 + 9)^2} - \frac{4(-9s^2 - 27)}{s(s^2 + 9)^3}$$

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$$\mathcal{L}^{-1} \left\{ \frac{e^{-3s}}{s^2+6s+13} + \ln \left(\frac{s^2+4}{s+1} \right) \right\}$$

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$$\mathcal{L}^{-1} \left\{ \frac{s+3-3}{(s+3)^2+4} \right\} + \frac{1}{t} \mathcal{L}^{-1} \left\{ -\frac{d}{ds} \left(\ln \left(\frac{s^2+4}{s+1} \right) \right) \right\}$$

$$\mathcal{L}^{-1} \left\{ \frac{s+3}{(s+3)^2+4} \right\} + \frac{1}{t} \mathcal{L}^{-1} \left\{ -\frac{d}{ds} \left[\ln(s^2+4) - \ln(s+1) \right] \right\}$$

$$e^{-3t} \left[\mathcal{L}^{-1} \left\{ \frac{s}{s^2+4} \right\} + \mathcal{L}^{-1} \left\{ \frac{3}{s^2+4} \right\} - \frac{1}{t} \mathcal{L}^{-1} \left\{ \frac{2s}{s^2+4} - \frac{2s}{s^2+1} \right\} \right]$$

$$e^{-3t} \left[\cos(2t) - \frac{3}{2} \sin(2t) \right] - \frac{1}{t} \left[2\cos(2t) - 2\cos(t) \right]$$

$$\left[e^{-3(t-3)} \cos(2(t-3)) - e^{-\frac{3}{2}(t-3)} \sin(2(t-3)) \right] u_3(t) - \frac{2}{t} \cos(2t) + \frac{2}{t} \cos(t)$$

pf