Functions of Linear Regression

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 $W_j = W_j - \frac{1}{n} \sum_{i=1}^{n} (H(X^i) - Y^i) X_j^i$

Given a data set $X = \{X_j^i | X_j^i \in \mathbb{R}^{n \times (m-1)}\}$ and a label set $Y = \{Y^i | Y^i \in \mathbb{R}^{n \times 1}\}$, where $1 \le i \le n$ and $2 \le j \le m$. For all X^i , insert $X_1^i = 1$ so that $X_j^i \in \mathbb{R}^{n \times m}$. Initialize weight matrix $W = \{W_j | W_j \in \mathbb{R}^{1 \times m}\}$.

Hypothesis function is defined in Equation (1).

$$H(X^{i}) = \sum_{j=1}^{m} W_{j} X_{j}^{i} \tag{1}$$

Loss function is defined in Equation (2).

$$C(X^i) = H(X^i) - Y^i \tag{2}$$

Cost function is defined in Equation (3).

$$J(W) = \frac{1}{2n} \sum_{i=1}^{n} C^{2}(X^{i})$$

$$= \frac{1}{2n} \sum_{i=1}^{n} (\sum_{j=1}^{m} W_{j} X_{j}^{i} - Y^{i})^{2}$$
(3)

The partial derivative of J(W) with respect to W_j is given as follows:

$$\begin{split} \frac{\partial J(W)}{\partial W_j} &= \frac{1}{2n} \sum_{i=1}^n \frac{\partial C^2(X^i)}{\partial W_j} \\ &= \frac{1}{2n} \sum_{i=1}^n \frac{\partial C^2(X^i)}{\partial C(X^i)} \cdot \frac{\partial C(X^i)}{\partial H(X^i)} \cdot \frac{\partial H(X^i)}{\partial W_j} \\ &= \frac{1}{2n} \sum_{i=1}^n 2C(X^i) \cdot 1 \cdot X_j^i \\ &= \frac{1}{n} \sum_{i=1}^n (H(X^i) - Y^i) X_j^i \end{split}$$

Thus, for all W_j , the update function is given as follows:

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