

Julia: What does it mean for a graph to be discontinuous? I don't get it!

Dylan: I think it's like when there's a hole in the graph or something.

James: Actually there are different kinds of discontinuities, but it's hard to visualize so let's take a look!

Altogether: LET'S DIVE IN!

Introduction

Question 1 A function f is said to be continuous at a point $x = a$ if which three conditions are satisfied?

Select All Correct Answers:

(a) $f(a)$ is defined ✓

(b) $f(a) \neq 0$

(c) $\lim_{x \rightarrow a} f(x)$ exists ✓

(d) $\lim_{x \rightarrow a} f(x) = f(a)$ ✓

(e) $f(x)$ is linear

(f) $f(x) \neq f(a)$

Example

Take the function $f(x) = \frac{(1-x)^2}{1-x}$.

$$\text{Graph of } (1,0), y = \frac{(x-1)^2}{x-1}$$

Through some simple elimination, we can easily see that this function is equivalent to $1-x$, where $x \neq 1$. Thus, there is one point on the original function we should pay close attention to: $x = 1$