

Applications of Maxima - Add Question Answers

Julia: I love optimization, but I can't really imagine where we could use it in real life.

Dylan: Yeah, it seems great for graphs, but for real world problems? No way.

Julia and Dylan:

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Julia: This is usually where James would chime in...

Dylan: Maybe he's running late?

James: Sorry guys, there was a traffic jam! I think it might be just perfect for our first illustration of the uses of optimization!

James' Traffic Jam

On the way back from Walmart, James ran into a traffic jam along the highway caused by an accident. While he was waiting in traffic, James decided to work on a function that roughly modeled the speed of the traffic over the day, using data from a surveyor who had been monitoring the accident. The equation he found was

$$t^3 - 11t^2 + 25t + 45$$

where t is in hours and $t = 0$ at 7 AM, and the function accurately models until 3 PM.

Question 1 *When is the traffic moving slowest?*

☐

At what speed is the traffic moving?

☐

Learning outcomes:

Question 2 *When is the traffic moving the most quickly?*

☐

At what speed?

☐

Dylan: Wow, I guess there are some uses for optimization!

Julia: Could we do something similar for the tree house I'm building for my cousin? It needs one side of screen to let air in and keep bugs out, but the rest should be wood. We want it to be 200 square feet.

James: Sure! Let's try and find the cheapest you could build it for.

Julia's Tree House

Julia is building a tree house for her younger cousin. She'd like one side to be a large screen to give a great view and airflow, without letting bugs pour in. The rest will be made of wood, with windows (which we will not account for). Unfortunately, to have the screen be sturdy enough for Julia to be comfortable, it will cost \$18 per foot, while the wood will cost only \$7 per foot. The height of the house has already been accounted for in the cost per foot. Given that she wants a 200 square foot tree house, how should she design it to minimize the cost?

Question 3 *Determine the dimensions and cost of the cheapest tree house.*

Dimensions (length x width): ☐

Cost (\$x): ☐

Julia: Wow, thanks James! That's going to be a real help!

James: Not a problem Julia.

Dylan: Could you help my little sister with her lemonade stand?

James: Sure, let's look at how she can maximize her profits!

Dylan's Lemonade Stand

Dylan's little sister is running a lemonade stand, selling a cup for 25 cents. On a typical day, she'll sell to 100 people. She'd like to increase her lemonade prices to profit more, and thinks that for every 25 cents she increases the price, 18 fewer people will purchase her product.

Question 4 *How should she price the lemonade to maximize her profit?*

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James: Excuse me for a second guys, I'm getting a call. Hello?... Yes, this is him... Sure, I'll get right on it!

Dylan: What was that about?

James: I just got a call from a small business that wanted me to help them figure out how to maximize their profits. Why don't you guys help me?

Julia and Dylan: Sounds good!

Handmade Paper Cups

James just got a call from a small company just north of Wooster which specializes in hand crafted paper cups. Every day, the company pays its workers \$2000, regardless of their productivity. Each cup costs \$2.15 to produce, as a result of the high quality paper which is used. Every day, new materials are ordered for $\frac{\$1500}{x}$, where x is the number of cups produced in a single day.

Question 5 *How many cups should the company produce every day in order to minimize costs?*

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