### Differentiation Rules

**Julia:** Hmm...I don't think differentiation rules, it takes so long and I hate using that long limit definition!

**Dylan:** No no Julia, it's differentiation *rules*!

Julia: Ohhhh, that makes more sense!

#### The Power Rule

Julia: I hate how long it takes to differentiate powers!

**Dylan:** Yeah, it takes forever! I feel like there was some sort of pattern to it though. I couldn't figure anything out though.

James: Sounds like you guys need my help again?

Julia and Dylan: Help us James!

James: There is a pattern! Check out this table I made!

$$\begin{array}{c|cc}
f(x) & f'(x) \\
\hline
x^2 & 2x^1 \\
x^3 & 3x^2 \\
x^4 & 4x^3
\end{array}$$

**Question 1** This is the model solution  $\boxed{7}$ 

**Question 2 Free Response:** This is the model solution

# The Constant Rule

Dylan: Wow! That's neat!

**Julia:** I wish we could use rules like this all over the place though, it would really save me time.

**James:** There are plenty of places with rules like this! Why don't we look at a function like y = 3?

**Question 3** Question goes here!

Free Response: This is the model solution

Using what you found in the previous problem, compute the following derivatives:

- (a) f(x) = 2
- (b) f(x) = 100
- (c) f(x) = 0

### The Constant Multiple Rule

**Julia:** James! Show us more! These things are going to save me so much time on my homework!

**James:** Alright alright, calm down Julia. We can look at a function like y=3x next.

Consider y = kx, where k is some arbitrary constant.

- (a) Derive this function using the limit definition. What does your answer mean?
- (b) Using what you found in the previous problem, compute the following derivatives:
  - (i) f(x) = 4x
  - (ii) f(x) = 10x
  - (iii)  $f(x) = \frac{1}{5}x$

#### The Sum and Difference Rules

**Dylan:** Wow, this stuff is awesome! Is there any way to put it all together? Like, is there an easy way to tell what the derivative of f(x) = 3x + 4 is?

**James:** There is Dylan!

Consider the differentiable functions f(x) and g(x). We will define a function j(x) = f(x) + g(x).

(a) Take the derivative of j(x) using the limit definition. What does your answer mean? Hint: In j(x+h), the (x+h) will replace x in the component functions as well.

(b) Using what you found in the previous problem, compute the following derivatives:

(i) 
$$f(x) = 3x^2 - 5x + 2$$
,  $g(x) = x^2 + 3x$ 

(ii) 
$$f(x) = x^2 - 4x + 2$$
,  $g(x) = -4x^2 + 3$ 

(iii) 
$$f(x) = 5x^3 + 3x$$
,  $g(x) = 2x^2 - 13x$ 

(c) Julia wonders if a similar rule exists for j(x) = f(x) - g(x). Using the limit definition of derivative, determine if there is a pattern. Then, if there is a rule, use it to solve the 1a, 1b, and 1c. If there is not, do them using the limit definition.

## In Summary

We've covered a lot of differentiation rules in this lab, to help you out we've made the following table.

Power Rule	$\frac{d}{dx}(x^n) = n * x^{(n-1)}$ , where $n$ is any real number besides 0.
Constant Rule	$\frac{d}{dx}(c) = 0$
Constant Multiple Rule	$\frac{d}{dx}(cf(x)) = c\frac{d}{dx}f(x)$
Sum Rule	$\frac{d}{dx}(f(x) + g(x)) = \frac{d}{dx}f(x) + \frac{d}{dx}g(x)$
Difference Rule	$\frac{d}{dx}(f(x) - g(x)) = \frac{d}{dx}f(x) - \frac{d}{dx}g(x)$