Implicit Differentiation - Finish solutions

Dylan: Woah! What's up with this?

Julia: I didn't know functions were explicit!

Dylan: The x and y are on the same side of the equation! I can't deal with

 $_{
m this}$

James: Functions can be explicit or implicit! And it not the way you're think-

ing Julia...

Introduction

So far we have dealt only with explicitly defined functions, where y = f(x). Functions where there are both x and y on one side or both sides of the equation are called implicit functions.

Guided Example

Question 1 Give an example of an explicit function and an implicit function, making sure your implicit function is not easily solvable for y.

Free Response:

Question 2 Take the implicit function you defined in part one, and graph it. What do you notice?

Graph of

Free Response:

Learning outcomes:

SAGE	
Free	Response:
	tion 4 Using the function(s) you found, find the slope of the tangent oint with two values on your graph.
Free	Response:
Imp	olicit Differentiation Using Substitution
Consi	der the equation $-x^2 * y^3 + y^5 - 32 = 0$.
Quest	Sion 1 Using the method shown in the previous section, evaluate the for y . Does this equation look easy to differentiate? No
don't a fun	d, let's treat our equation as an expression - because it equals zero have to worry about moving anything over. Now consider y as y ection of x , and differentiate with respect to x . Each y term will
$\frac{dx}{dx}$. The representation $\frac{dx}{dx}$ is $\frac{dx}{dx}$.	Then, set the expression equal to zero, and solve for $\frac{dy}{dx}$. What does ent?
Free	Response:
Quest	Sion 2 Using your result in the previous section, evaluate $\frac{dy}{dx}$ at $x=3$

Question 3 Using the same strategy, find the slope of $\sin(x^2) = \cos(xy^2)$ at any point.

Perpendicular at a Point

Julia: Wow, implicit differentiation is rough.

Dylan: You're telling me... I've been doing this for hours! I wish we could at least do a little more with it if I have to learn it.

James: Did I hear that you guys want to know more about using implicit differentiation?

Julia and Dylan: James! Tell us more!

James: Alright guys, you can use implicit differentiation with implicit functions to tell if two functions are perpendicular at a point!

Julia: But how?

Dylan: Yeah, I don't see how that helps.

James: It's easy - all we have to do is see if the tangent lines are perpendicular at that point, and if they are, then so are the curves!

Question 4 Graph $3x - 2y + x^3 - x^2y = 0$ and $x^2 - 2x + y^2 - 3y = 0$ on the same set of axes.

Graph of

Do they look perpendicular anywhere? Yes

Question 5 *Hint:* Remember, two perpendicular lines will have their slopes be the negative inverse of one another.

Prove the two curves are (or are not) perpendicular at the origin.

Free Response:

In Summary

There are two main methods to solve implicit equations

- (a) Solve for y and then differentiate.
- (b) Treat y as y(x) and differentiate for x, eventually solving for $\frac{dy}{dx}$ to give the value of the derivative at any point.