Implicit Differentiation - Finish solutions

Dylan: Woah! What's up with this?

Julia: I didn't know functions were explicit!

Dylan: The x and y are on the same side of the equation! I can't deal with

 $_{
m this}$

James: Functions can be explicit or implicit! And it not the way you're think-

ing Julia...

Introduction

So far we have dealt only with explicitly defined functions, where y = f(x). Functions where there are both x and y on one side or both sides of the equation are called implicit functions.

Guided Example

Question 1 Give an example of an explicit function and an implicit function, making sure your implicit function is not easily solvable for y.

Free Response:

Question 2 Take the implicit function you defined in part one, and graph it. What do you notice?

Graph of

Free Response:

Learning outcomes:

var('s t')	SAGE
Val (2 0)	
Free Response:	
Question 4 Using that a point with two v	e function(s) you found, find the slope of the tangent line values on your graph.
Free Response:	
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-	erentiation Using Substitution $1 - x^{2} * y^{3} + y^{5} - 32 = 0.$
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Question 3 Using the same strategy, find the slope of $\sin(x^2) = \cos(xy^2)$ at any point.

Perpendicular at a Point

Julia: Wow, implicit differentiation is rough.

Dylan: You're telling me... I've been doing this for hours! I wish we could at least do a little more with it if I have to learn it.

James: Did I hear that you guys want to know more about using implicit differentiation?

Julia and Dylan: James! Tell us more!

James: Alright guys, you can use implicit differentiation with implicit functions to tell if two functions are perpendicular at a point!

Julia: But how?

Dylan: Yeah, I don't see how that helps.

James: It's easy - all we have to do is see if the tangent lines are perpendicular at that point, and if they are, then so are the curves!

Question 4 Graph $3x - 2y + x^3 - x^2y = 0$ and $x^2 - 2x + y^2 - 3y = 0$ on the same set of axes.

Graph of

Do they look perpendicular anywhere? Yes

Question 5 *Hint:* Remember, two perpendicular lines will have their slopes be the negative inverse of one another.

Prove the two curves are (or are not) perpendicular at the origin.

Free Response:

In Summary

There are two main methods to solve implicit equations

- (a) Solve for y and then differentiate.
- (b) Treat y as y(x) and differentiate for x, eventually solving for $\frac{dy}{dx}$ to give the value of the derivative at any point.