

## Practical Discrete Mathematics (CSE 1402)

### MINOR ASSIGNMENT-5: COMPUTATIONAL ALGORITHMS IN LINEAR ALGEBRA

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1. Plot the following equations on a graph using `matplotlib` and find their point of intersection:

$$x + y = 5$$

$$x - y = 1$$

2. Visualize the 3D linear system using `matplotlib` (as planes):

$$x + y + z = 6$$

$$x - y + z = 2$$

$$2x + y - z = 3$$

3. Write a Python program to determine whether the following system of linear equations is **dependent** (i.e., has infinitely many solutions):

$$2x + 3y = 6$$

$$4x + 6y = 12$$

4. Visualize the system given in Question 3 using `matplotlib`.
5. Generate a  $4 \times 3$  matrix with random integers using `np.random.randint`. Display its transpose using NumPy.
6. Define a  $2 \times 2$  matrix. Calculate its determinant using `np.linalg.det()` and find its inverse using `np.linalg.inv()` (if it exists).
7. Input a  $3 \times 3$  matrix and write a program to check whether it is invertible or not.
8. Using the determinant method, check whether a given system of equations is consistent or inconsistent.
9. Input two matrices and find their element-wise product using NumPy.
10. Plot the line  $y = 2x + 1$  using `matplotlib`.
11. Plot the line  $y = 3x$  using `matplotlib`. (Note: Correct from “vertical line”.)
12. Use NumPy to convert the following system to Row Reduced Echelon Form (RREF):

$$\begin{bmatrix} 1 & 2 & 1 \\ 2 & 4 & 0 \\ 3 & 6 & 3 \end{bmatrix}$$

13. Without using Gaussian elimination directly, solve the following system of equations using NumPy:

$$\begin{bmatrix} 2 & -6 & 6 \\ 2 & 3 & -1 \\ 4 & -3 & -1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} -8 \\ 15 \\ 19 \end{bmatrix}$$

14. Use NumPy to solve a  $5 \times 5$  linear system generated with random integers using `np.random.randint`. Create a random  $5 \times 1$  constant vector and solve using `np.linalg.solve()`.
15. Generate a  $10 \times 10$  linear system using the random module and solve it using NumPy.