

# Linear Regression with One Variable

TOTAL POINTS 5

1. Consider the problem of predicting how well a student does in her second year of college/university, given how well she did in her first year.1 point

Specifically, let  $x$  be equal to the number of "A" grades (including A-, A and A+ grades) that a student receives in their first year of college (freshmen year). We would like to predict the value of  $y$ , which we define as the number of "A" grades they get in their second year (sophomore year).

Refer to the following training set of a small sample of different students' performances (note that this training set may also be referenced in other questions in this quiz). Here each row is one training example. Recall that in linear regression, our hypothesis is  $h_{\theta}(x) = \theta_0 + \theta_1 x$ , and we use  $m$  to denote the number of training examples.

x	y
3	4

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For the training set given above, what is the value of  $m$ ? In the box below, please enter your answer (which should be a number between 0 and 10).

4

2. Many substances that can burn (such as gasoline and alcohol) have a chemical structure based on carbon atoms; for this reason they are called hydrocarbons. A chemist wants to understand how the number of carbon atoms in a molecule affects how much energy is released when that molecule combusts (meaning that it is burned). The chemist obtains the dataset below. In the column on the right, "kJ/mol" is the unit measuring the amount of energy released.1 point

Name of molecule	Number of hydrocarbons in molecule (x)	Heat release when burned (kJ/mol) (y)
methane	1	-890

cyclopropane	3	-2091
butane	4	-2878
pentane	5	-3537
benzene	6	-3268
cyclohexane	6	-3920
hexane	6	-4163
octane	8	-5471
naphthalene	10	-5157

You would like to use linear regression ( $h_{\theta}(x) = \theta_0 + \theta_1 x$ ) to estimate the amount of energy released ( $y$ ) as a function of the number of carbon atoms ( $x$ ). Which of the following do you think will be the values you obtain for  $\theta_0$  and  $\theta_1$ ? You should be able to select the right answer without actually implementing linear regression.

- ☐  $\theta_0 = -569.6, \theta_1 = 530.9$
- ☐  $\theta_0 = -1780.0, \theta_1 = 530.9$

3. Suppose we set  $\theta_0 = -2, \theta_1 = 0.5$  in the linear regression hypothesis from Q1. What is  $h_{\theta}(6)$ ?1 point

1

4. Let  $f$  be some function so that1 point

$f(\theta_0, \theta_1)$  outputs a number. For this problem,

$f$  is some arbitrary/unknown smooth function (not necessarily the

cost function of linear regression, so  $f$  may have local optima).

Suppose we use gradient descent to try to minimize  $f(\theta_0, \theta_1)$

as a function of  $\theta_0$  and  $\theta_1$ . Which of the

- ☐ Even if the learning rate  $\alpha$  is very large, every iteration of gradient descent will decrease the value of  $f(\theta_0, \theta_1)$ .
- ☐ If  $\theta_0$  and  $\theta_1$  are initialized so that  $\theta_0 = \theta_1$ , then by symmetry (because we do simultaneous updates to the two parameters), after one iteration of gradient descent, we will still have  $\theta_0 = \theta_1$ .
- ☒ If the learning rate is too small, then gradient descent may take a very long time to converge.
- ☒ If  $\theta_0$  and  $\theta_1$  are initialized at a local minimum, then one iteration will not change their values.

5. Suppose that for some linear regression problem (say, predicting housing prices as in the lecture), we have some training set, and for our training set we managed to find some  $\theta_0, \theta_1$  such that  $J(\theta_0, \theta_1) = 0$ .1 point

Which of the statements below must then be true? (Check all that apply.)

- ☒ For these values of  $\theta_0$  and  $\theta_1$  that satisfy  $J(\theta_0, \theta_1) = 0$ , we have that  $h_{\theta}(x^{(i)}) = y^{(i)}$  for every training example  $(x^{(i)}, y^{(i)})$
- ☐ This is not possible: By the definition of  $J(\theta_0, \theta_1)$ , it is not possible for there to exist  $\theta_0$  and  $\theta_1$  so that  $J(\theta_0, \theta_1) = 0$
- ☐ We can perfectly predict the value of  $y$  even for new examples that we have not yet seen. (e.g., we can perfectly predict prices of even new houses that we have not yet seen.)
- ☐ For this to be true, we must have  $\theta_0 = 0$  and  $\theta_1 = 0$  so that  $h_{\theta}(x) = 0$