

TUTORIAL -7**UNIT-4: ELECTRICAL CONDUCTIVITY OF METALS**

($e = 1.6 \times 10^{-19} \text{C}$; $m = 9.1 \times 10^{-31} \text{kg}$; $k = 1.38 \times 10^{-23} \text{J/K}$; $N_A = 6.026 \times 10^{26} / \text{k.mol}$)

1. The resistivity of Aluminum at room temperature is $2.62 \times 10^{-8} \text{ohm-m}$. Calculate the drift velocity, mobility, relaxation time and mean free path of conduction electrons on the basis of classical free electron theory in an applied field of 50Vm^{-1} . The density and atomic weight of trivalent Al are 2700 kg/m^3 and 26.98 kg respectively.
2. A copper wire whose diameter is 0.16cm carries a steady current of 10A . Assuming one free electron/atom, calculate the density of electrons. Density of Cu is 8900 kg/m^3 , atomic mass is 63.54 kg and resistivity is $1.7 \times 10^{-8} \Omega \text{m}$. Calculate the drift velocity and mean free path according to classical free electron theory.
3. A conducting rod contains $8.5 \times 10^{28} \text{ electrons/m}^3$. Calculate its resistivity and mobility of electrons at room temperature if the mean collision time for electron scattering is $2 \times 10^{-14} \text{sec}$.
4. Fermi energy of silver is 5.5 eV . Calculate the probability of occupancy of a state which is (i) 0.1 eV below Fermi level, (ii) 0.1 eV above the Fermi level (iii) kT above Fermi level and (iv) $4kT$ above Fermi level, at a temperature of 300 K .
5. Find the temperature at which there is 1% probability that a state lying ~~above~~ 0.5 eV above Fermi energy will be occupied.
6. The Fermi level in silver is 5.5 eV . What are the energies for which the probabilities of occupancy at 300 K are 0.99 and 0.01 .
7. Determine the temperature at which there is a 1% probability that an energy state 0.3 eV below the Fermi level is empty. Given $E_F = 6.25 \text{ eV}$.
8. The Fermi energy of sodium is 3 eV at 0 K . Calculate the electron density, Fermi velocity.
9. ~~X~~ Calculate the density of states between 0 and 2 eV in a copper cube of dimension 1 cm .
10. The relaxation time of electrons in trivalent Al is $7.3 \times 10^{-15} \text{ s}$ and atomic weight and density are 26.98 kg and 2700 kg/m^3 respectively. Calculate the Fermi energy, Fermi velocity and mean free path according to quantum free electron theory.

1. The effective density of states for electrons and holes in silicon at 300 K are $2.8 \times 10^{19} \text{ cm}^{-3}$ and $1.04 \times 10^{19} \text{ cm}^{-3}$ respectively and the energy gap of Si is 1.1 eV. Calculate the intrinsic carrier concentration.

2. The following data corresponds to 300 K

	$N_c(\text{cm}^{-3})$	$N_v(\text{cm}^{-3})$	m_e^* / m_0	m_h^* / m_0	Energy gap (eV)
Silicon	2.8×10^{19}	1.04×10^{19}	1.08	0.56	1.12
Ga As	4.7×10^{17}	7.0×10^{18}	0.067	0.48	1.42
Germanium	1.04×10^{19}	6.0×10^{18}	0.55	0.37	0.67

- (i) Calculate the intrinsic carrier concentration for silicon at 400K.
 - (ii) Calculate the intrinsic carrier concentration for Germanium at 300 K.
 - (iii) Calculate the concentration of holes and electrons at 300 K for GaAs.
3. Calculate the electron and hole concentration in Si at 300K for the case when the Fermi level is 0.22eV below the conduction band energy E_c .
 4. Determine the electron and hole concentration in GaAs at 300K for the case when the Fermi level is 0.3eV above the valence band energy E_v .
 5. ✗ Calculate the density of states in conduction band of silicon between E_c and E_c+3kT at 300K.
 6. The mobilities of electrons and holes for Germanium are: $\mu_n = 0.39 \text{ m}^2/\text{Vs}$ and $\mu_h = 0.19 \text{ m}^2/\text{Vs}$. Calculate intrinsic conductivity at 300 K. Given $n_i = 2.5 \times 10^{19}/\text{m}^3$.
 7. The energy gap of Si is 1.1eV. Its electron and hole mobilities at room temperature are 0.48 and $0.013 \text{ m}^2 \text{V}^{-1} \text{s}^{-1}$ respectively. Evaluate its conductivity at 300K.
 8. An n-type Ge sample has dimensions $10\text{cm} \times 5\text{cm} \times 1\text{mm}$. The Hall voltage is measured across the width. The sample is placed in a magnetic field of strength 0.65 T and the current density along the length is 250 A/m^2 . If the electron concentration is 10^{21} m^{-3} , calculate the Hall field, Hall voltage, Hall coefficient.
 9. The resistivity of a n-doped Si sample is $8.9 \times 10^{-3} \Omega\text{m}$. The Hall coefficient was measured to be $3.6 \times 10^{-4} \text{ m}^3/\text{C}$. Assuming single carrier conduction, calculate the mobility and density of charge carriers.