

Tutorial - 7

resistivity of Al at room temp is 2.62×10^{-8} ohm. Calculate the drift velocity, mobility, relaxation time and mean free path of conduction e⁻ on the basis of classical free e⁻ theory in an applied field of 50 V/m. The density and atomic weight of trivalent Al are 2700 kg/m³ and 26.98 kg respectively.

Ans

$$\text{no. of free e}^-/\text{unit volume} = \frac{\text{Valency (z)} \times \text{density (d)} \times \text{Avogadro No (N}_A\text{)}}{\text{Atomic wt. (M)}}$$

$$n = \frac{z \times d \times N_A}{M}$$

$$n = \frac{3 \times 2700 \times 6.026 \times 10^{26}}{26.98}$$

$$n = 18.08 \times 10^{28} \text{ m}^{-3}$$

$$\sigma = \frac{1}{\rho} = \frac{n e^2 \tau}{m}$$

$$\tau = \frac{m}{\rho n e^2} = \frac{9.1 \times 10^{-31}}{2.62 \times 10^{-8} \times 18.08 \times 10^{28} \times (1.6 \times 10^{-19})^2}$$

$$\tau = 7.508 \times 10^{-15} \text{ s}$$

$$v_d = \frac{e E \tau}{m} = \frac{1.6 \times 10^{-19} \times 50 \times 7.508 \times 10^{-15}}{9.1 \times 10^{-31}}$$

$$= 6.593 \times 10^2 \text{ m/s}$$

$$\mu = \frac{v_d}{E} = 1.319 \times 10^3 \text{ m}^2 \text{ V}^{-1} \text{ A}^{-1}$$

$$\lambda = v_d \tau$$

$$v_{th} = \sqrt{\frac{3kT}{m}}$$

$$T = 300K$$

$$v_{th} = 1.16 \times 10^5 \text{ m/s}$$

$$\lambda_F = 1.16 \times 10^5 \times 7.508 \times 10^{-15}$$

$$= 8.77 \times 10^{-10} \text{ m}$$

Conductivity state its form if scattering is

- R: A copper wire whose diameter is 0.16 cm carries a steady current of 10A. Assuming one free e/atom, calculate the density of e. Density of Cu is 8900 kg/m³, atomic mass is 63.54 kg and resistivity is 1.7×10^{-8} nm. Calculate the drift velocity and mean free path according to CFE theory

Ans

$$d = 0.16 \times 10^{-2} \text{ m} \quad I = 10 \text{ A}$$

$$r = 0.08 \times 10^{-2} \text{ m} \quad \rho = 1.7 \times 10^{-8} \text{ nm}$$

$$n = \frac{Z \times d \times N_A}{M} = \frac{1 \times 8900 \times 6.023 \times 10^{26}}{63.54}$$

$$= 8.44 \times 10^{28} / \text{m}^3$$

$$\tau = \frac{m}{\rho n e^2} = \frac{9.1 \times 10^{-31}}{1.7 \times 10^{-8} \times 8.44 \times 10^{28} \times (1.6 \times 10^{-19})^2}$$

$$= 2.477 \times 10^{-14} \text{ s}$$

$$I = A n e v_d$$

$$v_d = \frac{I}{A n e} = \frac{10}{3.14 \times (0.08 \times 10^{-2})^2 \times 8.44 \times 10^{28} \times 1.6 \times 10^{-19}}$$

$$= 3.684 \times 10^{-4} \text{ m/s}$$

$$A = v_{th} \tau$$

$$= 1.16 \times 10^5 \times 2.477 \times 10^{-14} = 2.897 \times 10^{-9} \text{ m}$$

$$v_{th} = \sqrt{\frac{3kT}{m}}$$

$$T = 300K$$

$$v_{th} = 1.16 \times 10^5 \text{ m/s}$$

$$\lambda_F = 1.16 \times 10^5 \times 7.508 \times 10^{-15}$$

$$= 8.77 \times 10^{-10} \text{ m}$$

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Scattering
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- Q. A copper wire whose diameter is 0.16 cm carries a steady current of 10A. Assuming one free electron/atom, calculate the density of e-. Density of Cu is 8900 kg/m³, atomic mass is 63.54 kg and resistivity is 1.7 × 10⁻⁸ Ωm. Calculate the drift velocity and mean free path according to CFE theory.

Ans

$$d = 0.16 \times 10^{-2} \text{ m}$$

$$I = 10 \text{ A}$$

$$r = 0.08 \times 10^{-2} \text{ m}$$

$$\rho = 1.7 \times 10^{-8} \text{ Ωm}$$

$$n = \frac{Z \times d \times N_A}{M} = \frac{1 \times 8900 \times 6.026 \times 10^{26}}{63.54}$$

$$= 8.44 \times 10^{28} / \text{m}^3$$

$$\tau = \frac{m}{\rho n e^2} = \frac{9.1 \times 10^{-31}}{1.7 \times 10^{-8} \times 8.44 \times 10^{28} \times (1.6 \times 10^{-19})^2}$$

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$$A = v_{th} \tau$$

$$= 1.16 \times 10^5 \times 2.477 \times 10^{-14} = 2.897 \times 10^{-9} \text{ m}$$

conducting rod contains $8.5 \times 10^{28} e^-/m^3$. calculate its resistivity and mobility of e^- at room temp if the mean free collision time for e^- scattering is $2 \times 10^{-14} s$.

Ans $n = 8.5 \times 10^{28} / m^3$

$$\tau = 2 \times 10^{-14} s$$

$$\sigma = \frac{1}{\rho} = \frac{n e^2 \tau}{m}$$

$$\rho = \frac{m}{n e^2 \tau} = \frac{9.1 \times 10^{-31}}{8.5 \times 10^{28} \times (1.6 \times 10^{-19})^2 \times 2 \times 10^{-14}}$$

$$= 2.09 \times 10^8 \Omega m$$

$$\mu = \frac{v_d}{E} = \frac{e \tau}{m} = \frac{e \tau}{m}$$

$$= 3.516 \times 10^3 \text{ m}^2 \text{ V}^{-1} \text{ A}^{-1}$$

4. Fermi energy of silver is 5.5 eV. calculate the probability of occupancy of state which is
- 0.1 eV below Fermi level
 - 0.1 eV above Fermi level
 - kT above Fermi level
 - $4kT$ above Fermi level at temp of 300K.

Ans

$$f(E) = \frac{1}{e^{\frac{E-E_F}{kT}} + 1}$$

- (i) 0.1 eV below Fermi level
 $\therefore E - E_F = -0.1 \text{ eV}$

$$f(E) = \frac{1}{e^{\frac{-0.1 \times 1.6 \times 10^{-19}}{1.38 \times 10^{-23} \times 300} + 1}} = \frac{1}{e^{-3.8647} + 1}$$

$$= 0.979$$

(ii) 0.1 ev above E_F
 $\text{so } E-E_F = 0.1 \text{ eV}$

$$f(E) = \frac{1}{e^{\frac{0.1 \times 1.6 \times 10^{19}}{1.38 \times 10^{-23} \times 300} + 1}} = 0.0205$$

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probabilities
0.01.

(iii) kT above E_F , so $E-E_F = kT$

$$f(E) = \frac{1}{e^{\frac{kT}{kT} + 1}} = \frac{1}{e+1} = 0.2689$$

(iv) At 4K above E_F , so $E-E_F = 4kT$

$$f(E) = \frac{1}{e^{\frac{4kT}{kT} + 1}} = \frac{1}{e^4 + 1} = 0.01798$$

5 Find the temperature at which there is 1% probability that a state lying above 0.5 eV above E_F will be occupied

$$E-E_F = 0.5 \text{ eV}$$

$$f(E) = \frac{1}{e^{\frac{E-E_F}{kT} + 1}}$$

$$e^{\frac{E-E_F}{kT} + 1} = \frac{1}{f(E)}$$

$$e^{\frac{E-E_F}{kT}} = \frac{1}{f(E)} - 1$$

$$\frac{E-E_F}{kT} = \ln \left[\frac{1}{f(E)} - 1 \right]$$

$$T = \frac{E-E_F}{k \ln \left[\frac{1}{f(E)} - 1 \right]} = \frac{0.5 \times 1.6 \times 10^{19}}{1.38 \times 10^{-23} \ln \left[\frac{1}{0.01} - 1 \right]}$$

$$T = 1261.5 \text{ K}$$

The Fermi level in silver is 5.5 eV.
 What are the energies for which the probabilities of occupancy at 300 K are 0.99 & 0.01.

Ans $f(E) = \frac{1}{e^{\frac{E-E_F}{kT}} + 1}$

$$\frac{E-E_F}{kT} = \ln \left[\frac{1}{f(E)} - 1 \right]$$

$$E = E_F + kT \ln \left[\frac{1}{f(E)} - 1 \right]$$

$$T = 300 \text{ K} \quad \text{when } f(E) = 0.99$$

$$E = 5.5 \times 1.6 \times 10^{-19} + 1.38 \times 10^{-23} \ln \left[\frac{1}{0.99} - 1 \right]$$

$$= 8.61 \times 10^{-19} \text{ J}$$

$$= 5.38 \text{ eV}$$

$$\text{when } f(E) = 0.01$$

$$E = 5.5 \times 1.6 \times 10^{-19} + 1.38 \times 10^{-23} \ln \left[\frac{1}{0.01} - 1 \right]$$

$$= 5.61 \text{ eV}$$

7. Determine the temperature at which there is 1% probability that an energy state 0.3 eV below Fermi level is empty.

$$\text{Given } E_F = 6.25 \text{ eV}$$

Ans $T = \frac{E-E_F}{k \ln \left[\frac{1}{f(E)} - 1 \right]}$

$$E - E_F = -0.3 \text{ eV}$$

$$1 - f(E) = 1\% \quad \left[\begin{array}{l} \text{Probability for unoccupation} \\ \text{of state} = 1 - f(E) \end{array} \right]$$

$$f(E) = 0.99$$

$$f(E) = T = \frac{-0.3 \times 1.6 \times 10^{-19}}{1.38 \times 10^{-23} \ln \left[\frac{1}{0.99} - 1 \right]}$$

$$T = 756.96 \text{ K}$$

8. The Fermi energy of sodium is 3 eV at 0 K. Calculate electron density & Fermi velocity.

Ans

$$E_F(0) = \frac{\hbar^2}{8m} \left(\frac{3n}{\pi} \right)^{2/3}$$

$$E_F(0) = 5.85 \times 10^{-38} n^{2/3}$$

$$3 \times 1.6 \times 10^{-19} = 5.85 \times 10^{-38} n^{2/3}$$

$$n = \left[\frac{3 \times 1.6 \times 10^{-19}}{5.85 \times 10^{-38}} \right]^{3/2}$$

$$n = 2.35 \times 10^{28} / \text{m}^3$$

$$v_F = \sqrt{\frac{\partial E_F}{m}} = \sqrt{\frac{3 \times 1.6 \times 10^{-19}}{9.1 \times 10^{-31}}} \\ = 1.027 \times 10^6 \text{ m/s}$$

9. Calculate the density of states between 0 and 2 eV in Cu cube of dimension 1 cm.

$$\frac{g(E)}{dE} = \frac{8\sqrt{2}\pi m^{3/2}}{h^3} E^{1/2} dE$$

$$g(E) = \frac{8\sqrt{2}\pi m^{3/2}}{h^3} \times \int_0^E E^{1/2} dE$$

$$= \frac{8\sqrt{2}\pi \times 3.14 \times (9.1 \times 10^{-31})^{3/2}}{(6.63 \times 10^{-34})^3} \frac{2}{3} \left[E^{3/2} \right]_0^{2 \times 1.6 \times 10^{-19}}$$

$$= 1.063 \times 10^{56} \times \frac{2}{3} (2 \times 1.6 \times 10^{-19})^{3/2}$$

$$= 1.28 \times 10^{28} / \text{m}^3$$

$$= \frac{1.28 \times 10^{28}}{10^6} / \text{cm}^3$$

$$= 1.28 \times 10^{22} / \text{cm}^3$$

10. The relaxation time of e^- in trivalent Al is $7.3 \times 10^{-15} \text{ s}$ and atomic wt. and density are 26.98 kg and 2700 kg/m^3 respectively. Calculate the Fermi energy, Fermi vel. & mean free path acc to QFE theory.

$$\tau = 7.3 \times 10^{-15} \text{ s}$$

$$M = 26.98 \text{ kg}$$

$$d = 2700 \text{ kg/m}^3$$

$$n = \frac{2 \times d \times N_A}{M} = \frac{2 \times 2700 \times 6.026 \times 10^{26}}{26.98}$$
$$= 18.08 \times 10^{28} \text{ m}^{-3}$$

$$E_F(0) = -\frac{\hbar^2}{8m} \left(\frac{3n}{\pi}\right)^{2/3}$$
$$= 5.85 \times 10^{-38} n^{2/3}$$
$$= 5.85 \times 10^{-38} (18.08 \times 10^{28})^{2/3}$$
$$= 1.87 \times 10^{-18} \text{ J}$$
$$= 11.69 \text{ eV}$$

$$v_F = \sqrt{\frac{2E_F}{m}} = 2.027 \times 10^6 \text{ m/s}$$

$$\lambda = \tau v_F$$
$$= 7.3 \times 10^{-15} \times 2.027 \times 10^6$$
$$= 1.479 \times 10^{-8} \text{ m}$$

Tutorial - 8

Semiconductors

1. The effective density of states for e^- and holes in Si at 300K are $2.8 \times 10^{19}/\text{cm}^3$ and $1.04 \times 10^{19}/\text{cm}^3$ respectively. If the energy gap of Si is 1.1eV, calculate the intrinsic carrier concentration.

Ans

$$n_i = \sqrt{N_c N_v} e^{-\frac{E_g}{2kT}}$$

$$= \sqrt{2.8 \times 10^{19} \times 1.04 \times 10^{19}} e^{-\frac{1.1 \times 1.6 \times 10^{-19}}{2 \times 1.38 \times 10^{-23} \times 300}}$$

$$= 1.706 \times 10^{19} \times 5.869 \times 10^{-10}$$

$$= 1.001 \times 10^{10}/\text{cm}^3$$

$\frac{g_1}{g_0} = 1.12 \text{ eV}$
 then $n_i = 6.803 \times 10^{13}/\text{cm}^3$
 $= 6.803 \times 10^{15}/\text{m}^3$

2. The following data corresponds to 300K

	$N_c(\text{cm}^3)$	$N_v(\text{cm}^3)$	m_e^*/m_0	m_h^*/m_0	Energy gap (eV)
Si	2.8×10^{19}	1.04×10^{19}	1.08	0.56	1.12
GeAs	4.7×10^{17}	7×10^{18}	0.067	0.49	1.42
Ge	1.04×10^{19}	6×10^{18}	0.55	0.37	0.67

- (i) Calculate the intrinsic carrier concentration for Si at 400K
- (ii) Calculate the intrinsic carrier concentration for Ge at 300K
- (iii) Calculate the concentration of holes & e^- at 300K for GeAs.

$$\begin{aligned}
 & \text{(i)} \quad n_i = \sqrt{N_c N_v} e^{-\frac{E_g}{kT}} \\
 & N_c \propto T^{3/2} = \sqrt{2.8 \times 10^9 \times \left(\frac{f_{500}}{f_{400}}\right)^{1/2} \times 1.04 \times 10^{19} \left(\frac{N_{300}}{N_{400}}\right)^{1/2}} e^{-\frac{1.12 \times 1.6 \times 10^{-19}}{2 \times k \times 1.38 \times 10^{-23} \times T}} \\
 & \frac{N_c(400)}{N_c(300)} = \left(\frac{400}{300}\right)^{3/2} = \sqrt{2.8 \times 10^9 \times 1.04 \times 10^{19}} e^{-\frac{1.12 \times 1.6 \times 10^{-19}}{2 \times 1.38 \times 10^{-23} \times T}} \\
 & N_c(400) = \left(\frac{400}{300}\right)^{3/2} \times N_c(300) = 1.706 \times 10^{19} \times \frac{1.57 \times 9.5}{8.9244} \times 10^{-8} \times 10^{15.396} \\
 & N_c(300) = \left(\frac{400}{300}\right)^{3/2} N_c(300) = n_i = 2.344 \times 10^{12} / \text{cm}^3
 \end{aligned}$$

$$\begin{aligned}
 & \text{(ii)} \quad n_i = \sqrt{N_c N_v} e^{-\frac{E_g}{kT}} \\
 & = \sqrt{1.04 \times 10^9 \times 6 \times 10^8} e^{-\frac{0.67 \times 1.6 \times 10^{-19}}{2 \times 1.38 \times 10^{-23} \times 300}} \\
 & = 7.899 \times 10^{18} \times 2.383 \times 10^{-6} \\
 & = 1.882 \times 10^{12} / \text{cm}^3
 \end{aligned}$$

$$\begin{aligned}
 & \text{(iii)} \quad n = N_c e^{-\frac{E_g}{kT}} \\
 & n = N_c e^{-\frac{E_g}{kT}} - \frac{1.42 \times 1.6 \times 10^{-19}}{2 \times 1.38 \times 10^{-23} \times 300} \\
 & = 4.7 \times 10^{17} e^{-\frac{1.2109 \times 10^{-12}}{2 \times 1.38 \times 10^{-23} \times 300}} \\
 & = 5.69 \times 10^{15} / \text{cm}^3
 \end{aligned}$$

$$\begin{aligned}
 p &= N_v e^{-\frac{E_g}{kT}} \\
 &= 7 \times 10^{18} e^{-\frac{1.42 \times 1.6 \times 10^{-19}}{2 \times 1.38 \times 300}} \\
 &= 7 \times 10^{18} \times 1.2109 \times 10^{-12} \\
 &= 8.476 \times 10^6 / \text{cm}^3
 \end{aligned}$$

$$\begin{aligned}
 \text{(i)} \quad n_{i,400K} &= \sqrt{\lambda_{c_{400K}} N_{v_{400K}}} e^{\frac{-E_g}{2kT}} = \sqrt{2.8 \times 10^{19} \times \left(\frac{400}{300}\right)^{3/2} \times 1.04 \times 10^9 \left(\frac{400}{300}\right)^{3/2}} e^{\frac{-1.12 \times 1.6 \times 10^{-19}}{2 \times 1.38 \times 10^{-23} \times 400}} \\
 N_c \propto T^{3/2} &\quad \Rightarrow N_c(400K) = \left(\frac{400}{300}\right)^{3/2} N_c(300K) \\
 N_c(400K) &= \left(\frac{400}{300}\right)^{3/2} N_c(300K) \\
 N_v(400K) &= \left(\frac{400}{300}\right)^{3/2} N_v(300K) \\
 N_c(300K) &= \left(\frac{400}{300}\right)^{3/2} N_c(300K) \\
 N_v(300K) &= \left(\frac{400}{300}\right)^{3/2} N_v(300K) \\
 n_i &= 1.706 \times 10^{11} \times \frac{1.53395}{8.9244} \times 10^{-8} \times 1.5396 \quad 2.34 \times 10^{12} / \text{cm}^3
 \end{aligned}$$

$$\begin{aligned}
 \text{(ii)} \quad n_i &= \sqrt{N_c N_v} e^{\frac{-E_g}{2kT}} \\
 &= \sqrt{1.04 \times 10^9 \times 6 \times 10^8} e^{\frac{-0.67 \times 1.6 \times 10^{-19}}{2 \times 1.38 \times 10^{-23} \times 300}} \\
 &= 7.899 \times 10^{18} \times 2.383 \times 10^{-6} \\
 &= 1.889 \times 10^{18} / \text{cm}^3
 \end{aligned}$$

$$\text{(iii)} \quad n = N_c e^{\frac{-(E_c - E_F)}{kT}}$$

$$\begin{aligned}
 n &= N_c e^{\frac{-E_g}{2kT}} \\
 &= 4.7 \times 10^{17} e^{\frac{-1.42 \times 1.6 \times 10^{-19}}{2 \times 1.38 \times 10^{-23} \times 300}} \\
 &= 4.7 \times 10^{17} \times 1.2109 \times 10^{-12} \\
 &= 5.69 \times 10^{5} / \text{cm}^3
 \end{aligned}$$

$$\begin{aligned}
 b &= N_v e^{\frac{-E_g}{2kT}} \\
 &= 7 \times 10^{18} e^{\frac{-1.42 \times 1.6 \times 10^{-19}}{2 \times 1.38 \times 300}} \\
 &= 7 \times 10^{18} \times 1.2109 \times 10^{-12} \\
 &= 8.476 \times 10^6 / \text{cm}^3
 \end{aligned}$$

③ Calculate the electron and hole concentration in Si at 300K for the case when the fermi level is 0.22 eV below the conduction band energy E_c .

$$n = N_c e^{-\frac{E_c - E_F}{kT}}$$

$$= 2.8 \times 10^{19} e^{\frac{-0.22 \times 1.6 \times 10^{-19}}{1.38 \times 10^{-23} \times 300}}$$

$$= 2.8 \times 10^{19} \times 2.029 \times 10^{-4}$$

$$\cdot = 5.683 \times 10^{15} / \text{cm}^3$$

$$p = 1.04 \times 10^{19} e^{\frac{-0.90 \times 1.6 \times 10^{-19}}{1.38 \times 10^{-23} \times 300}}$$

$$= 8.49 \times 10^3 / \text{cm}^3$$

4. Calculate the e- and hole concentration in GaAs at 300K for the case when Fermi energy level is 0.3 eV above the valence band energy E_v .

$$E_F - E_v = 0.3 \text{ eV}$$

$$E_g = 1.42$$

$$E_c - E_F = 1.12 \text{ eV}$$

$$n = 4.7 \times 10^{17} e^{\frac{-1.12 \times 1.6 \times 10^{-19}}{1.38 \times 10^{-23} \times 300}}$$

$$= 4.7 \times 10^{17} \times 1.59 \times 10^{-19} = 7.475 \times 10^{-2} / \text{cm}^3$$

$$p = 7 \times 10^{18} \times e^{\frac{-0.3 \times 1.6 \times 10^{-19}}{1.38 \times 10^{-23} \times 300}}$$

$$= 7 \times 10^{18} \times 9.219 \times 10^{-6}$$

$$= 6.453 \times 10^{13} / \text{cm}^3$$

5. Determine the e^- & hole concentration in GaAs at 300 K for the case when

5. Calculate the density of states in conduction band of Si between E_c & $E_c + 3kT$ at 300 K.

Sol:

$$g_c dE = \frac{8\sqrt{2}\pi m_e^{3/2}}{h^3} (E - E_c)^{1/2} dE$$

$$\begin{aligned} g_c &= \frac{8\sqrt{2}\pi (1.08 \times m_0)^{3/2}}{(6.63 \times 10^{-34})^3} \int_{E_c}^{E_c + 3kT} (E - E_c)^{1/2} dE \\ &= (1.08)^{3/2} \times 1.063 \times 10^{56} \times \frac{2}{3} \left[(E - E_c)^{3/2} \right]_{E_c}^{E_c + 3kT} \\ &= (1.08)^{3/2} \times 1.063 \times 10^{56} \times \frac{2}{3} \times \int_{E_c}^{E_c + 3kT} (E_c + 3kT - E)^{3/2} dE \\ &= 1.1009 \times 10^{26} / m^3 \end{aligned}$$

* calculate the density of states in valence band of Si b/w E_v & $E_v - kT$ at 300 K

$$g_v dE = \frac{8\sqrt{2}\pi m_h^{3/2}}{h^3} \int_{E_v}^{E_v - kT} \sqrt{E_v - E} dE$$

$$\begin{aligned} g_v &= \frac{8\sqrt{2}\pi (0.56 m_0)^{3/2}}{h^3} \int_{E_v}^{E_v - kT} (E_v - E)^{1/2} dE \\ &= (0.56)^{3/2} \times 1.063 \times 10^{56} \times \frac{2}{3} \left[(E_v - E)^{3/2} \right]_{E_v}^{E_v - kT} \\ &= (0.56)^{3/2} \times 1.063 \times 10^{56} \times \frac{2}{3} \times (E_v - E_v + kT)^{3/2} \\ &= 7.91 \times 10^{24} / m^3 \end{aligned}$$

The mobilities of e^- & holes for Ge are $\mu_n = 0.39 \text{ m}^2/\text{V.s}$ & $\mu_h = 0.19 \text{ m}^2/\text{V.s}$. Calculate resistivity at 300 K.

$$\text{Given } n_i = 2.5 \times 10^{19} / \text{m}^3$$

$$\text{Ans } \sigma = e n_i (\mu_n + \mu_h)$$

$$= 1.6 \times 10^{-19} \times 2.5 \times 10^{19} (0.39 + 0.19)$$

$$= 2.32 / \text{nm}$$

$$\rho = \frac{1}{\sigma} = 0.431 \text{ nm}$$

7. The energy gap of Si is 1.1 eV. Its e^- and hole mobilities at room temp are 0.48 and $0.013 \text{ m}^2 \text{ V}^{-1} \text{ s}^{-1}$ respectively. Evaluate its conductivity at 300K.

$$\text{Ans } \sigma = e n_i (\mu_n + \mu_h)$$

$$n_i = \sqrt{N_c N_v} e^{-\frac{E_g}{2kT}}$$

$$= \frac{9.974 \times 10^{10}}{1.001} / \text{cm}^3 = 1.001 \times 10^{16} / \text{m}^3$$

$$\sigma = 1.6 \times 10^{-19} \times \frac{9.974 \times 1.001 \times 10^{16}}{(0.48 + 0.012)}$$

$$= \frac{7.895 \times 10^{14}}{5.36 \times 10^{-4}} / \text{nm} (1.1 \text{ eV})$$

$$(1.12 \text{ eV})$$

8. An n-type Ge sample has dimensions $10\text{ cm} \times \underline{5\text{ cm}} \times 1\text{ mm}$. The Hall voltage is measured across the width. The sample is placed in a magnetic field of strength 0.65 T and current density along the length is 250 A/m^2 . If the e⁻ concentration is 10^{21} m^{-3} , calculate the Hall field, Hall voltage and Hall coefficient.

Ans

Hall coefficient

$$R_H = \frac{1}{ne}$$

$$= \frac{1}{10^{21} \times 1.6 \times 10^{-19}}$$

$$= 6.25 \times 10^{-3} \text{ m}^3 \cdot \text{C}^{-1}$$

$$R_H = \frac{(E_H)_y}{(B)(J)_x}$$

$$E_H = B J R_H$$

$$= 0.65 \times 250 \times 6.25 \times 10^{-3}$$

$$= 1.015 \text{ V/m}$$

$$E_y = \frac{V_y}{d w} \quad [w=5\text{cm}]$$

$$V_y = i \omega E_y$$

$$= 5 \times 10^{-2} \times 1.015$$

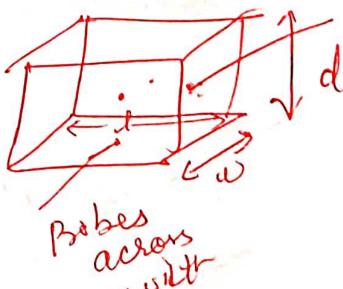
$$= 5.078 \times 10^{-2}$$

$$V_H = \frac{BI}{net}$$

$$= \frac{BJA}{net} = \frac{BJbt}{net}$$

$$= \frac{0.65 \times 250 \times 5 \times 10^{-2}}{10^{21} \times 1.6 \times 10^{-19}}$$

$$= 5.078 \times 10^{-2}$$



Flows across width

$$= 1.479 \times 10^{-10}$$

9. The resistivity of a n-doped Si sample is $8.9 \times 10^3 \text{ ohm}$. The Hall coefficient was measured to $3.6 \times 10^{-4} \text{ m}^3/\text{C}$. Assuming single carrier conduction, calculate mobility & density of charge carriers.

Ans

$$R_H = 3.6 \times 10^{-4}$$

$$R_H = \frac{1}{ne}$$

$$n = \frac{1}{eR_H} = \frac{1}{3.6 \times 10^{-4} \times 1.6 \times 10^{-19}}$$
$$= 1.736 \times 10^{22} \text{ m}^{-3}$$

$$\sigma = ne\mu$$

$$\mu = \frac{\sigma}{ne} = \frac{\sigma R_H}{\rho} \quad \leftarrow \mu_e = \sigma R_H = \frac{R_H}{\rho}$$

$$\mu = \frac{R_H}{\rho}$$

$$= \frac{3.6 \times 10^{-4}}{8.9 \times 10^{-3}}$$

$$= 4.044 \times 10^{-2} \text{ m}^2 \text{ V}^{-1} \text{ s}^{-1}$$