## LECTURE 19: DIFFERENCE-IN-DIFFERENCE MODELS

ECON 480 - ECONOMETRICS - FALL 2018

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Difference-in-Difference Models



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- · Often, we want to examine the consequences of a change, such as a law or policy
  - e.g. States that implemented law X saw a change in Y
  - Treatment: States that implement law X
  - Control: States that did not implement law X
  - If we have panel data with observations for all states before and after the change:
- Simple logic: compare difference in outcomes of treatment group (before and after treatment) with those of non-treated group (before and after same treatment period)

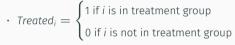


$$\widehat{Y_{it}} = \beta_0 + \beta_1 \text{Treated}_i + \beta_2 \text{After}_t + \beta_3 (\text{Treated}_i * \text{After}_t) + \epsilon_{it}$$



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$$= \begin{cases} 1 \text{ if } i \text{ is in treatment group} \end{cases}$$





$$\widehat{Y}_{it} = \beta_0 + \beta_1 \mathrm{Treated}_i + \beta_2 \mathrm{After}_t + \beta_3 (\mathrm{Treated}_i * \mathrm{After}_t) + \epsilon_{it}$$

$$\cdot \ \mathit{Treated}_i = \begin{cases} 1 \ \mathrm{if} \ i \ \mathrm{is} \ \mathrm{in} \ \mathrm{treatment} \ \mathrm{group} \\ 0 \ \mathrm{if} \ i \ \mathrm{is} \ \mathrm{not} \ \mathrm{in} \ \mathrm{treatment} \ \mathrm{group} \end{cases}$$

$$\cdot \ \mathit{After}_t = \begin{cases} 1 \ \mathrm{if} \ t \ \mathrm{is} \ \mathrm{after} \ \mathrm{treatment} \ \mathrm{period} \\ 0 \ \mathrm{if} \ t \ \mathrm{is} \ \mathrm{before} \ \mathrm{treatment} \ \mathrm{period} \end{cases}$$



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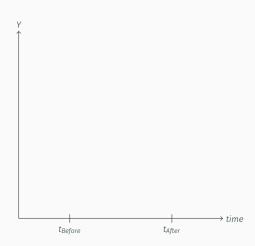
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Group Diff. $(\Delta Y_i)$	Treatment	Control	
$eta_1$	$\beta_0 + \beta_1$	$eta_{ exttt{0}}$	Before
$eta_1 + eta_3$	$\beta_0 + \beta_1 + \beta_2 + \beta_3$	$\beta_0 + \beta_2$	After
$eta_3$	$\beta_2 + \beta_3$	$eta_2$	Time Diff. $(\Delta Y_t)$

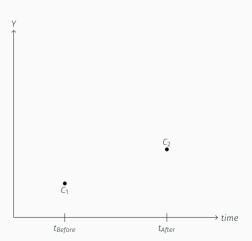






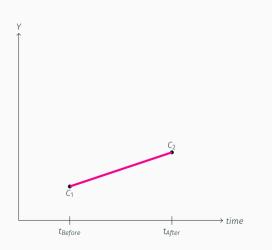








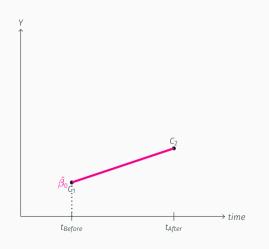
$$\widehat{Y_{it}} = \hat{eta}_0 + \hat{eta}_1 Treated_i + \hat{eta}_2 After_t + \hat{eta}_3 (Treated_i imes After_t) + \hat{\epsilon_{it}}$$







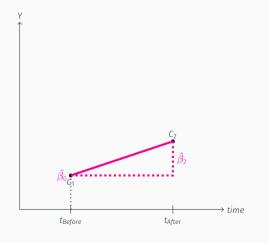
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- Control (Treated = 0) group
- $\cdot$   $\hat{eta}_0$ : value of Y for control before treatment



$$\widehat{Y_{it}} = \hat{\beta_0} + \hat{\beta}_1 \text{Treated}_i + \hat{\beta}_2 \text{After}_t + \hat{\beta}_3 (\text{Treated}_i \times \text{After}_t) + \hat{\epsilon_{it}}$$

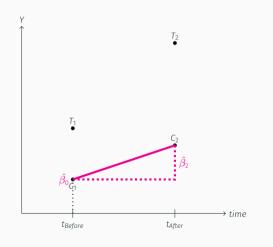


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 $\cdot$   $\hat{eta}_{ extsf{2}}$ : time difference (for control group)



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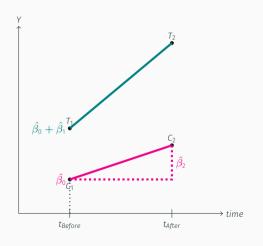


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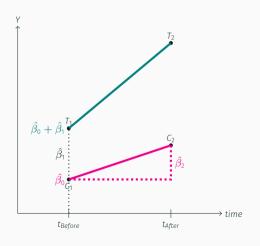


- Treatment (Treated = 1) group
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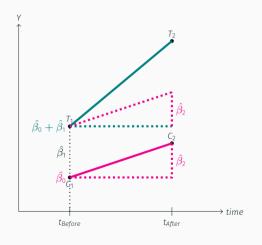
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Treated $_i + \hat{eta_2}$ After $_t + \hat{eta_3}$ (Treated $_i imes$  After $_t$ )  $+ \hat{\epsilon_{it}}$ 



- Treatment (Treated = 1) group
- Control (Treated = 0) group
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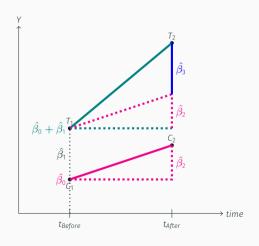
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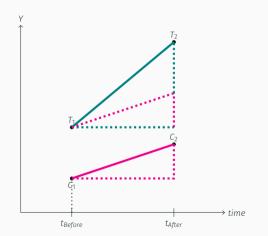
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- $\cdot$   $\hat{eta}_0$ : value of Y for control before treatment
- $\hat{eta}_1$ : difference between treatment and control (before treatment)
- $\hat{eta}_2$ : time difference (for control group)
- $\hat{eta}_3$ : difference-in-difference: effect of treatment

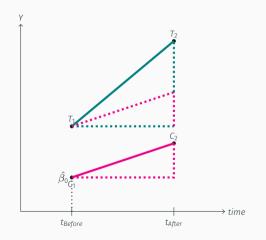


$$\widehat{Y_{it}} = \hat{eta}_0 + \hat{eta}_1 Treated_i + \hat{eta}_2 After_t + \hat{eta}_3 (Treated_i imes After_t) + \hat{\epsilon_{it}}$$





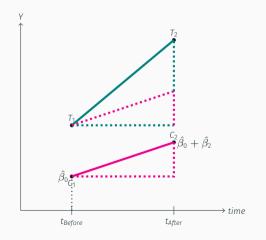
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 $\cdot$  Y for Control Group Before:  $\hat{eta_0}$ 



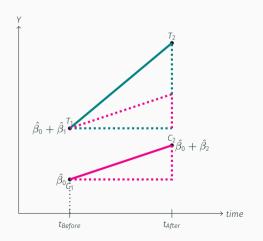
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- Y for Control Group Before:  $\hat{\beta}_0$
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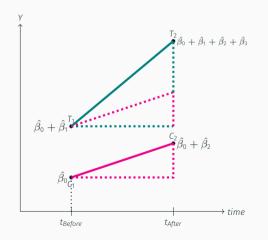
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- · Y for Control Group Before:  $\hat{eta_0}$
- $\cdot$  Y for Control Group After:  $\hat{eta}_0 + \hat{eta}_2$
- $\cdot$  Y for Treatment Group Before:  $\hat{eta_0}+\hat{eta_1}$



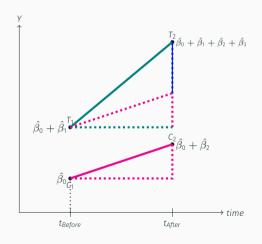
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- Y for Control Group Before:  $\hat{\beta}_0$
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- Y for Treatment Group Before:  $\hat{eta}_{ extsf{0}}+\hat{eta}_{ extsf{1}}$
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- $\cdot$  Treatment Effect:  $\hat{eta}_3$



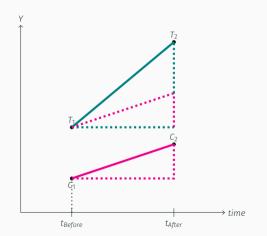
# COMPARING GROUP MEANS (AGAIN)

$$\widehat{Y_{it}} = \hat{\beta_0} + \hat{\beta_1} \text{Treated}_i + \hat{\beta_2} \text{After}_t + \hat{\beta_3} (\text{Treated}_i \times \text{After}_t) + \hat{\epsilon_{it}}$$

	Control	Treatment	Group Diff. $(\Delta Y_i)$
Before	$eta_{ exttt{0}}$	$eta_0 + eta_1$	$eta_1$
After	$\beta_0 + \beta_2$	$\beta_0 + \beta_1 + \beta_2 + \beta_3$	$eta_1+eta_3$
Time Diff. $(\Delta Y_t)$	$eta_2$	$\beta_2 + \beta_3$	$eta_3$
			Diff-in-diff $(\Delta_i \Delta_t Y)$

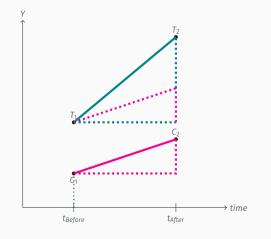


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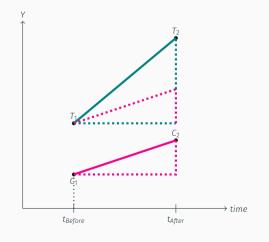
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Key assumption in DND models is that the time trend is parallel



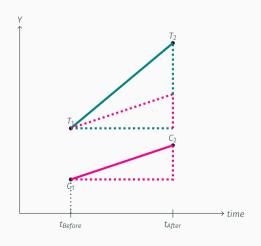
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- Treatment & control groups must be similar over time except for treatment

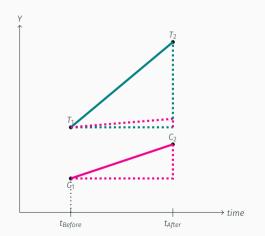


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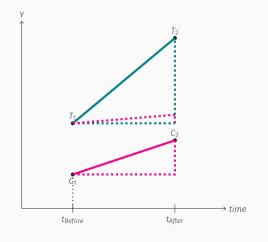
- Key assumption in DND models is that the time trend is parallel
- Treatment & control groups must be similar over time except for treatment
- Counterfactual if the treatment group were *not* treated, they would change the same as control group over time  $\hat{eta}_2$

$$\widehat{Y_{it}} = \hat{\beta_0} + \hat{\beta}_1 \text{Treated}_i + \hat{\beta}_2 \text{After}_t + \hat{\beta}_3 (\text{Treated}_i \times \text{After}_t) + \hat{\epsilon_{it}}$$





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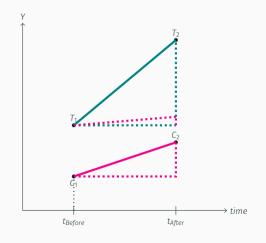


If time trend is different between treatment and control groups



# **KEY ASSUMPTION ABOUT COUNTERFACTUAL II**

$$\widehat{Y_{it}} = \hat{\beta_0} + \hat{\beta}_1 \text{Treated}_i + \hat{\beta}_2 \text{After}_t + \hat{\beta}_3 (\text{Treated}_i \times \text{After}_t) + \hat{\epsilon_{it}}$$



- If time trend is different between treatment and control groups
- Treatment effect may be over/under-estimated!



Example



#### Example

In 1993 Georgia initiated a HOPE scholarship program to let state residents with at least a B average in high school attend public college in Georgia for free. Did it increase college enrollment?

• Dynarski, Susan (2000), "Hope for Whom? Financial Aid for the Middle Class and Its Impact on College Attendance" micro-level data on 4,291 young individuals:



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$$\cdot \text{ After}_t = \begin{cases} 1 \text{ if } t \text{ is after 1992} \\ 0 \text{ if } t \text{ is after 1992} \end{cases}$$

• Note: With a dummy *dependent* variable (Y), coefficients estimate the probability Y = 1, i.e. the probability a person is enrolled in college



#### Example



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#### Example

- · We can use a diff-in-diff model to measure the effect of HOPE scholarship on enrollments
- $\cdot$  Georgia and nearby states: if not for HOPE, changes should be the same over time
- Treatment period: 1992
- · Treatment: Georgia



## Example

- · We can use a diff-in-diff model to measure the effect of HOPE scholarship on enrollments
- · Georgia and nearby states: if not for HOPE, changes should be the same over time
- Treatment period: 1992
- Treatment: Georgia

$$\Delta_{i}\Delta_{t}\textit{Enrolled} = \left(\mathsf{GA}_{\textit{after}} - \mathsf{GA}_{\textit{before}}\right) - \left(\mathsf{neighbors}_{\textit{after}} - \mathsf{neighbors}_{\textit{before}}\right)$$



# Example

- · We can use a diff-in-diff model to measure the effect of HOPE scholarship on enrollments
- · Georgia and nearby states: if not for HOPE, changes should be the same over time
- Treatment period: 1992
- · Treatment: Georgia

$$\Delta_{i}\Delta_{t} \textit{Enrolled} = (GA_{\textit{after}} - GA_{\textit{before}}) - (\text{neighbors}_{\textit{after}} - \text{neighbors}_{\textit{before}})$$

$$\widehat{\textit{Enrolled}}_{it} = \beta_{0} + \beta_{1} \textit{Georgia}_{it} + \beta_{2} \textit{After}_{it} + \beta_{3} \textit{Georgia}_{it} \times \textit{After}_{it}$$



```
DND<-lm(InCollege~Georgia+After+AfterGeorgia, data=HOPF)
summary(DND)
##
## Call:
## lm(formula = InCollege ~ Georgia + After + AfterGeorgia, data = HOPE)
##
## Residuals:
      Min
               10 Median
                              30
                                     Max
## -0.4058 -0.4058 -0.4013 0.5942 0.6995
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 0.40578
                        0.01092 37.146 < 2e-16 ***
## Georgia -0.10524
                        0.03778 -2.785 0.00537 **
                        0.01585 -0.281 0.77848
## After -0.00446
                          0.04889 1.827 0.06776 .
## AfterGeorgia 0.08933
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.4893 on 4287 degrees of freedom
## Multiple R-squared: 0.001872, Adjusted R-squared: 0.001174
## F-statistic: 2.681 on 3 and 4287 DF. p-value: 0.04528
```

 $\widehat{Enrolled}_{it} = 0.406 - 0.105 Georgia_i - 0.004 After_t + 0.08$ 



$$\widehat{\textit{Enrolled}}_{it} = 0.406 - 0.105 \textit{Georgia}_i - 0.004 \textit{After}_t + 0.089 \textit{Georgia}_i \times \textit{After}_t$$

 $\cdot$   $\beta_0$ : A non-Georgian before 1992 was 40.6% likely to be a college student



$$\widehat{\textit{Enrolled}}_{it} = 0.406 - 0.105 \textit{Georgia}_i - 0.004 \textit{After}_t + 0.089 \textit{Georgia}_i \times \textit{After}_t$$

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- $\cdot$   $\beta_{1}$ : Georgians are 10.5% less likely to be college students than neighboring states



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$$\widehat{Enrolled}_{it} = 0.406 - 0.105 Georgia_i - 0.004 After_t + 0.089 Georgia_i \times After_t$$

- $\cdot$   $\beta_0$ : A non-Georgian before 1992 was 40.6% likely to be a college student
- +  $eta_{
  m 1}$ : Georgians are 10.5% less likely to be college students than neighboring states
- $\cdot$   $\beta_2$ : After 1992, young Americans are 0.4% less likely to be college students
- $\cdot$   $\beta_3$ : After 1992, Georgians are 8.9% more likely to enroll in colleges than neighboring states
  - -Treatment effect: HOPE increased enrollment likelihood by 8.9%



$$\widehat{\textit{Enrolled}}_{it} = 0.406 - 0.105 \textit{Georgia}_i - 0.004 \textit{After}_t + 0.089 \textit{Georgia}_i \times \textit{After}_t$$

- A group mean for a dummy Y is E[Y=1], i.e. the probability a student is enrolled:



$$\widehat{\textit{Enrolled}}_{it} = 0.406 - 0.105 \textit{Georgia}_i - 0.004 \textit{After}_t + 0.089 \textit{Georgia}_i \times \textit{After}_t$$

- A group mean for a dummy Y is E[Y=1], i.e. the probability a student is enrolled:
  - · Non-Georgian enrollment probability pre-1992:  $\beta_0 = 0.406$



$$\widehat{Enrolled}_{it} = 0.406 - 0.105 Georgia_i - 0.004 After_t + 0.089 Georgia_i \times After_t$$

- A group mean for a dummy Y is E[Y=1], i.e. the probability a student is enrolled:
  - $\cdot$  Non-Georgian enrollment probability pre-1992:  $\beta_0=$  0.406
    - Georgian enrollment probability pre-1992:  $\beta_0+\beta_1=$  0.406 0.105 = 0.301



$$\widehat{Enrolled}_{it} = 0.406 - 0.105 Georgia_i - 0.004 After_t + 0.089 Georgia_i \times After_t$$

- A group mean for a dummy Y is E[Y=1], i.e. the probability a student is enrolled:
  - · Non-Georgian enrollment probability pre-1992:  $\beta_0 = 0.406$ 
    - Georgian enrollment probability pre-1992:  $\beta_0 + \beta_1 = 0.406 0.105 = 0.301$
    - · Non-Georgian enrollment probability post-1992:  $\beta_0+\beta_2=0.406-0.004=0.402$



$$\widehat{Enrolled}_{it} = 0.406 - 0.105 Georgia_i - 0.004 After_t + 0.089 Georgia_i \times After_t$$

- · A group mean for a dummy Y is E[Y=1], i.e. the probability a student is enrolled:
  - · Non-Georgian enrollment probability pre-1992:  $\beta_0 = 0.406$ 
    - Georgian enrollment probability pre-1992:  $\beta_0 + \beta_1 = 0.406 0.105 = 0.301$
    - · Non-Georgian enrollment probability post-1992:  $\beta_0 + \beta_2 = 0.406 0.004 = 0.402$
    - · Georgian enrollment probability post-1992:

$$\beta_0 + \beta_1 + \beta_2 + \beta_3 = 0.406 - 0.105 - 0.004 + 0.089 = 0.386$$



```
# group mean for non-Georgian before 1992
HOPE %>%
  filter(Georgia==0 & After==0) %>%
  summarize(prob=mean(InCollege))
##
          prob
  1 0.4057827
# group mean for Georgian before 1992
HOPE %>%
  filter(Georgia==1 & After==0) %>%
  summarize(prob=mean(InCollege))
          prob
## 1 0 3005464
```

```
# group mean for non-Georgian AFTER 1992
HOPE %>%
  filter(Georgia==0 & After==1) %>%
  summarize(prob=mean(InCollege))
```

```
## prob
## 1 0.401323
```

```
# group mean for Georgian AFTER 1992
HOPE %>%
filter(Georgia==1 & After==1) %>%
summarize(prob=mean(InCollege))
```

```
## prob
## 1 0.3854167
```



# **DIFF-IN-DIFF EXAMPLE SUMMARY**

$$\widehat{Enrolled}_{it} = 0.406 - 0.105 Georgia_{it} - 0.004 After_{it} + 0.089 Georgia_{it} \times After_{it}$$

	Neighbors	Georgia	Group Diff. $(\Delta Y_i)$
Before	0.406	0.301	-0.105
After	0.402	0.386	0.016
Time Diff. $(\Delta Y_t)$	-0.004	0.085	0.089
			Diff is diff (A A V)



# **DIFF-IN-DIFF EXAMPLE SUMMARY**

$$\widehat{Enrolled}_{it} = 0.406 - 0.105 Georgia_{it} - 0.004 After_{it} + 0.089 Georgia_{it} \times After_{it}$$

	Neighbors	Georgia	Group Diff. $(\Delta Y_i)$
Before	0.406	0.301	-0.105
After	0.402	0.386	0.016
Time Diff. $(\Delta Y_t)$	-0.004	0.085	0.089

Diff-in-diff ( $\Delta\Delta Y$ )

$$\begin{split} \Delta\Delta \textit{Enrolled} &= \left( \mathsf{GA}_{\textit{after}} - \mathsf{GA}_{\textit{before}} \right) - \left( \mathsf{neighbors}_{\textit{after}} - \mathsf{neighbors}_{\textit{before}} \right) \\ &= \left( 0.386 - 0.301 \right) - \left( 0.402 - 0.406 \right) \\ &= \left( 0.085 \right) - \left( -0.004 \right) \\ &= 0.089 \end{split}$$

