

Log Linear Models – degrees of freedom

Example – all possible outcomes for $A*B*C$ (4x2x2)

Model	Effects	df (equation)	df (calculated)
1	$A + B + C$	$df1 = a*b*c-(a-1)-(b-1)-(c-1)-1$	10
2	$A*B + C$	$df2 = df1-(a-1)*(b-1)$	7
3	$A*C + B$	$df3 = df1-(a-1)*(c-1)$	7
4	$A + B*C$	$df4 = df1-(b-1)*(c-1)$	9
5	$A*B + A*C$	$df5 = df2-(a-1)*(c-1)$	4
6	$A*B + B*C$	$df6 = df2-(b-1)*(c-1)$	6
7	$A*C + B*C$	$df7 = df3-(b-1)*(c-1)$	6
8	$A*B + A*C + B*C$	$df8 = df7-(a-1)*(b-1)$	3
9	$A*B*C$	$df9 = df8-(a-1)*(b-1)*(c-1)$	0

- Model 1
 - Full independence ($A + B + C$)
 - Degrees of freedom is product of all categorical outcomes (N) minus the degrees of freedom for each individual variable minus 1.
- When you add an interaction term, the portion you subtract from the degrees of freedom set the product of degrees of freedom (e.g. $(a-1)*(b-1)$)
- Whenever you add an interaction term (e.g. $A * B$) to an independent term (e.g. $A*B + C$), you need to subtract the value from a model with one less interaction term (for this model, there are a maximum of 3 interaction terms)
- Model 9
 - Full dependence ($A * B * C$)
 - Degrees of freedom is zero;