

PSY 308B – ANOVA Midterm Formulas

t tests

Independent samples *t* test

- $$t = \frac{(\text{Observed} - \text{Expected})}{SE}$$

Observed = difference between two samples means

Expected = difference between two population means (always defaults to 0)

SE = standard error of the difference

So...

- $$t = \frac{(\bar{x}_1 - \bar{x}_2)}{SE}$$

Where $SE = \sqrt{\frac{s_{pooled}^2}{N_1} + \frac{s_{pooled}^2}{N_2}}$

And $s_{pooled}^2 = [(N_1 - 1) * s_1^2 + (N_2 - 1) * s_2^2] / [(N_1 - 1) + (N_2 - 1)]$

- $$df = (N_1 - 1) + (N_2 - 1)$$

- $$\text{Cohen's } d = \frac{(M_1 - M_2)}{SD_{pooled}}$$

Where $SD_{pooled} = \sqrt{s_{pooled}^2}$

Paired (dependent) samples *t* test

- $$t = \frac{(\text{Observed} - \text{Expected})}{SE}$$

Observed = sample mean of difference scores

Expected = population mean of difference scores (always defaults to 0)

SE = standard error of the difference scores

Where $SE = \frac{s_d}{\sqrt{n}} = \frac{\sqrt{\frac{\sum (d - \bar{d})^2}{n-1}}}{\sqrt{n}}$ and $\bar{d} = \frac{\sum d}{n}$

- $$df = (N - 1)$$

- $$\text{Cohen's } d = \frac{\bar{d}}{s_d}$$

One-way ANOVA

- $F = \frac{\text{between-groups variance}}{\text{within-groups variance}}$
- In other words... $F = \frac{MS_{\text{between}}}{MS_{\text{within}}}$ or $F = \frac{MS_{\text{treat}}}{MS_{\text{error}}}$

Source	SS	df	MS	F
treat	$n \sum (x_j - x_T)^2$	$k - 1$	$\frac{SS_{\text{treat}}}{df_{\text{treat}}}$	$\frac{MS_{\text{treat}}}{MS_{\text{error}}}$
error	$\sum (x_{ij} - x_j)^2$	$k(n - 1)$	$\frac{SS_{\text{error}}}{df_{\text{error}}}$	
Total	$\sum (x_{ij} - x_T)^2$	$N - 1$		

- Eta-squared = $\eta^2 = \frac{SS_{\text{treat}}}{SS_{\text{total}}}$

Factorial ANOVA

- In a factorial ANOVA, you get F ratios for main effects of each of your independent variables (F_A and F_B) and for your interaction ($F_{A \times B}$)
- $F_A = \frac{MS_A}{MS_{\text{error}}}$ $F_B = \frac{MS_B}{MS_{\text{error}}}$ $F_{A \times B} = \frac{MS_{A \times B}}{MS_{\text{error}}}$

Source	SS	df	MS	F
Factor A	$bn \sum (x_{A_j} - x_T)^2$	$a - 1$	$\frac{SS_A}{df_A}$	$\frac{MS_A}{MS_{\text{error}}}$
Factor B	$an \sum (x_{B_k} - x_T)^2$	$b - 1$	$\frac{SS_B}{df_B}$	$\frac{MS_B}{MS_{\text{error}}}$
Interaction	$SS_{\text{total}} - SS_{\text{error}} - SS_A - SS_B$	$(a - 1)(b - 1)$	$\frac{SS_{A \times B}}{df_{A \times B}}$	$\frac{MS_{A \times B}}{MS_{\text{error}}}$
Error (S/AB)	$\sum (x_{ijk} - x_{AB_{jk}})^2$	$ab(n - 1)$	$\frac{SS_{\text{error}}}{df_{\text{error}}}$	
Total	$\sum (x_{ijk} - x_T)^2$	$N - 1$		

- Complete eta-squared = $\eta^2 = \frac{SS_{\text{effect}}}{SS_{\text{total}}}$
- Partial eta-squared = partial $\eta^2 = \frac{SS_{\text{effect}}}{(SS_{\text{effect}} + SS_{\text{error}})}$

Repeated-measures ANOVA

- $F = \frac{\text{between-groups variance}}{\text{Error variance}}$
- In other words... $F = \frac{MS_{\text{between}}}{MS_{\text{error}}}$ or $F = \frac{MS_{\text{treat}}}{MS_{\text{error}}}$

Source	SS	df	MS	F
treat	$n \sum (x_j - x_T)^2$	$k - 1$	$\frac{SS_{\text{treat}}}{df_{\text{treat}}}$	$\frac{MS_{\text{treat}}}{MS_{\text{error}}}$
within	$\sum (x_{ij} - x_j)^2$	$k(n - 1)$		
subject	$k \sum (M_i - x_T)^2$	$n - 1$		
error	$SS_{\text{within}} - SS_{\text{subject}}$	$(k - 1)(n - 1)$	$\frac{SS_{\text{error}}}{df_{\text{error}}}$	
Total	$\sum (x_{ij} - x_T)^2$	$N - 1$		

- Eta-squared = $\eta^2 = \frac{SS_{\text{treat}}}{SS_{\text{treat}} + SS_{\text{error}}}$

Mixed Factorial ANOVA

- $F = \frac{\text{between-groups variance}}{\text{Error variance}}$

- In other words... $F = \frac{MS_{\text{between}}}{MS_{\text{error}}}$ or $F = \frac{MS_{\text{treat}}}{MS_{\text{error}}}$

Source	SS	df	MS	F
Between-group				
A	$n \sum (x_{ij} - x_T)^2$	a - 1	$\frac{SS_A}{df_A}$	$\frac{MS_A}{MS_{S/A}}$
S/A	$\sum (x_{ij} - x_j)^2$	a (n - 1)	$\frac{SS_{S/A}}{df_{S/A}}$	
Within-group				
B	$k \sum (M_i - x_T)^2$	b - 1	$\frac{SS_B}{df_B}$	$\frac{MS_B}{MS_{B \times S/A}}$
AxB	$\sum n(Y_{jk} - Y_{...})^2$	(a - 1)(b - 1)	$\frac{SS_{A \times B}}{df_{A \times B}}$	$\frac{MS_{A \times B}}{MS_{B \times S/A}}$
BxS/A	$\sum (Y_{ijk} - Y_{.jk})^2$	a(b - 1)(n - 1)	$\frac{SS_{B \times S/A}}{df_{B \times S/A}}$	
Total	$\sum (x_{ij} - x_T)^2$	N - 1 or (a)(b)(n) - 1	$\frac{SS_{Total}}{df_{Total}}$	

- Eta-squared = $\eta^2 = \frac{SS_{\text{treat}}}{SS_{\text{treat}} + SS_{\text{error}}}$