

# Package ‘ioanalysis’

August 5, 2015

**Title** Input-Output Analysis

**Version** 0.1

**Author** Ignacio Sarmiento-Barbieri

**Maintainer** Ignacio Sarmiento-Barbieri <srmtbr2@illinois.edu>

**Description** Input and Output Analysis.

**Depends** R (>= 3.1.1), ggplot2, xlsx

**License** GNU GENERAL PUBLIC LICENSE

**LazyData** true

## R topics documented:

agg.matrix . . . . .	1
key.sector . . . . .	2
leontief.inv . . . . .	4
multipliers . . . . .	5
upstream . . . . .	7
vs.io . . . . .	8
vs.ki . . . . .	9

<b>Index</b>	<b>11</b>
--------------	-----------

---

agg.matrix	<i>Aggregation Matrix</i>
------------	---------------------------

---

## Description

Aggregates Input-Output Matrices. Construct an aggregation matrix of kxn dimension.

## Usage

```
agg.matrix<-function(mat,d.mip)
```

## Arguments

mat	Matrix. How sectors should be aggregated. First column should be the new sector in order, the remaining columns the sectors that are going to be aggregated
dimcol	Numeric. Column dimension

**Author(s)**

Ignacio Sarmiento-Barbieri

**References**

Nazara, Suahasil & Guo, Dong & Hewings, Geoffrey J.D., & Dridi, Chokri, 2003. "PyIO. Input-Output Analysis with Python". REAL Discussion Paper 03-T-23. University of Illinois at Urbana-Champaign. (<http://www.real.illinois.edu/d-paper/03/03-T-23.pdf>)

**Examples**

```
temp<-matrix(sample(1:40), 14)
temp[,1]<-seq(1:14)
S<-agg.matrix(temp,40)
```

---

key.sector

---

*Impact Analysis: Backward and Forward linkages*


---

**Description**

Computation of Backward and Forward linkages. It aims to identify those sectors whose economic activity exerts a greater than average influence on the whole economy. Key sectors are identified by calculating backward and forward linkages. Let

$$B = (I - A)^{-1} = [b_{ij}]$$

be the Leontief inverse matrix and let  $B_j$  and  $B_i$  be the column and row multipliers of this Leontief inverse. The sector  $j$ 's backward linkage ( $BL_j$ ) and forward linkage ( $FL_i$ ) are defined as:

$$BL_j = \frac{\frac{1}{n} \sum_{i=1}^n b_{ij}}{\frac{1}{n^2} \sum_{j=1}^n \sum_{i=1}^n b_{ij}}$$

$$FL_i = \frac{\frac{1}{n} \sum_{j=1}^n b_{ij}}{\frac{1}{n^2} \sum_{j=1}^n \sum_{i=1}^n b_{ij}}$$

The usual interpretation is to propose that, if

$$BL_j > 1$$

, a unit change in final demand in sector  $j$  will generate an above-average increase in activity in the economy. Similarly, for

$$FL_i > 1$$

, it is asserted that a unit change in all sector's final demand would create an above average increase in sector  $i$ . Thus, a key sector is identified as one having both indices greater than one.

**Usage**

```
key.sector(mip, X, epsilon=0.1, key=TRUE, cutoff=1, write.xlsx=TRUE, name="Key_sector.xlsx")
```

**Arguments**

mip	Input-output matrix
X	Total input or output
epsilon	Replaces zeros in X
key	Logical. If TRUE identifies key sectors
cutoff	Cutoff above which are the key sectors
write.xlsx	Logical. If TRUE writes an excel file
name	String. Name of the excel file

**Details**

The function takes the sector names from the column names of the Input-output matrix

**Value**

Returns a vector with the calculated Backward and Forward linkages for each sector

**Author(s)**

Ignacio Sarmiento-Barbieri

**References**

Nazara, Suahasil & Guo, Dong & Hewings, Geoffrey J.D., & Dridi, Chokri, 2003. "PyIO. Input-Output Analysis with Python". REAL Discussion Paper 03-T-23. University of Illinois at Urbana-Champaign. (<http://www.real.illinois.edu/d-paper/03/03-T-23.pdf>)

**See Also**

See Also [leontief.inv](#) [gosh.inv](#)

**Examples**

```
#Uses the 40x40 matrix included in the package

mip<-mat_40x40[1:40,2:41] #Input-output coefficients
X<-mat_40x40$DT.a.PB[1:40] #Total output vector

key<-key.sector(mip,X, key=FALSE, write.xlsx=FALSE)
```

leontief.inv

*Leontief Inverse***Description**

Computes the Leontief Inverse and the Backward Linkage

**Usage**

```
leontief.inv(mip,X.j,write.xlsx=TRUE,name="Leontief_Inv.xlsx")
```

**Arguments**

mip	Matrix. Input output matrix
X.j	Vector. Input in each column
write.xlsx	Logical. if TRUE writes an excel file
name	String. name of the excel file

**Details**

The Leontief inverse is derived from the input-output table  $A=[a_{ij}]$  where  $a_{ij}=z_{ij}/X_j$  where  $z_{ij}$  is the input from  $i$  required in the production of  $j$ .  $X_j$  is the corresponding input in each column. The leontief inverse is then computed as  $(I-A)^{-1}$

Falta describir Backward Linkage

**Author(s)**

Ignacio Sarmiento-Barbieri

**References**

Nazara, Guo, Hewing and Dridi (2003). *PyIO. Input-Output Analysis with Python*. <http://www.real.illinois.edu/pyio/>

**Examples**

```
##---- Should be DIRECTLY executable !! ----
##-- ==> Define data, use random,
##--or do help(data=index) for the standard data sets.

## The function is currently defined as
function (x)
{
}
```

### Description

According to Nazara et al. (2003) and Blair and Miller (2009) four multipliers can be calculated from an input-output matrix: output multiplier, input multiplier, income multiplier and employment multiplier.

Output multiplier: it is computed from the Leontief inverse. Let

$$B = [b_{ij}]$$

be the Leontief inverse matrix the output multiplier for sector j,

$$O_j = \sum_{i=1}^n b_{ij}$$

Input multiplier: it is computed from the Goshian inverse. Let

$$G = [g_{ij}]$$

be the Goshian inverse matrix the input multiplier for sector j,

$$I_j = \sum_{i=1}^n g_{ij}$$

Income multiplier: the calculation of this multiplier requires a wage vector (z) to calculate the household input coefficient (a):

$$a_{n+1,i} = \frac{z_{n+1,i}}{X_i}$$

with the Leontief inverse, the household income multiplier for sector j is

$$H_j = \sum_{i=1}^n a_{n+1,i} b_{ij}$$

Employment multiplier: the calculation of this multiplier requires a sectoral employment vector (e) to calculate the labor input coefficient (w):

$$w_{n+1,i} = \frac{e_i}{X_i}$$

with the Leontief inverse, the employment multiplier for sector j is

$$E_j = \sum_{i=1}^n w_{n+1,i} b_{ij}$$

### Usage

```
multipliers(mip, X, z, e, write.xlsx=TRUE, name="output_multiplier.xlsx")
```

**Arguments**

mip	Input-output matrix
X	Vector. Total input or output
z	Vector. Household input coefficient
e	Vector. If TRUE identifies key sectors
write.xlsx	Logical. If TRUE writes an excel file
name	String. Name of the excel file

**Value**

Returns a data frame with the calculated multipliers for each sector

**Author(s)**

Ignacio Sarmiento-Barbieri

**References**

Nazara, Suahasil & Guo, Dong & Hewings, Geoffrey J.D., & Dridi, Chokri, 2003. "PyIO. Input-Output Analysis with Python". REAL Discussion Paper 03-T-23. University of Illinois at Urbana-Champaign. (<http://www.real.illinois.edu/d-paper/03/03-T-23.pdf>)

Blair, P.D. and Miller, R.E. (2009). "Input-Output Analysis: Foundations and Extensions". Cambridge University Press

**See Also**

See Also [leontief.inv](#) [gosh.inv](#)

**Examples**

```
#Uses the 40x40 matrix included in the package

mip<-mat_40x40[1:40,2:41] #Input-output coefficients
X<-as.matrix(mat_40x40$DT.a.PB[1:40]) #Total output vector

z<-mat_40x40$X[1:40] #

e<-mat_40x40$Chog[1:40]

multipliers<-multipliers(mip,X,z=z,e=e, write.xlsx=FALSE)
```

---

upstream	<i>upstreamness</i>
----------	---------------------

---

## Description

Measures upstreamness as of equation 9 in Antras et al. (2012)

## Usage

```
upstream(linv,y,x,m, write.xlsx=TRUE, name="Upstream.xlsx")
```

## Arguments

linv	Matrix. Input output matrix
y	Output Vector
x	Exports Vector
m	Imports Vector
write.xlsx	Logical. if TRUE writes an excel file
name	String. name of the excel file

## Author(s)

Ignacio Sarmiento-Barbieri

## References

Pol Antràs & Davin Chor & Thibault Fally & Russell Hillberry, 2012. "Measuring the Upstreamness of Production and Trade Flows," NBER Working Papers 17819, National Bureau of Economic Research, Inc.

## Examples

```
##---- Should be DIRECTLY executable !! ----
##-- ==> Define data, use random,
##--or do help(data=index) for the standard data sets.

## The function is currently defined as
function (x)
{
}
```

vs.io

*VS share of total exports***Description**

Vertical Specialization (VS) share of total exports. The formula for VS as a share of total exports for country k is

$$VS \text{ share of total exports} = \frac{VS}{X_k} = \frac{A * L * X}{X_k}$$

where A is the nxn imported coefficient matrix, L is the Leontief inverse, X is an nx1 vector of exports, n is the number of sectors, and X<sub>k</sub> is the sum of exports across the n sectors.

**Usage**

```
vs.io(imp,exp,leon=1, namesector, write.xlsx=TRUE, name="Level_Verticalization.xlsx")
```

**Arguments**

imp	Is the nxn imported coefficient matrix
exp	Numeric Vector. Exports
leon	Leontief Inverse as output of function leontief.inv()
namesector	Character. Name of Sector i
write.xlsx	Logical. if TRUE writes an excel file
name	String. name of the excel file

**Value**

Returns a data frame with the A\*L\*X product, the total exports and the level of verticalization for each sector. Total.exp. returns a scalar, equals to the sum of exports across sectors

**Author(s)**

Ignacio Sarmiento-Barbieri

**References**

Hummels, David & Ishii, Jun & Yi, Kei-Mu, 2001. "The nature and growth of vertical specialization in world trade," Journal of International Economics, Elsevier, vol. 54(1), pages 75-96, June.

**See Also**

See Also [leontief.inv](#)



## Examples

```
#Uses the 40x40 matrix included in the package

exp<-mat_40x40$X[1:40] #Exports Vector
class(exp) #the class is numeric
imp<-mat_imp_40x40[1:40,2:41]/mat_40x40$DT.a.PB[1:40] #Imports Coef Matrix
class(imp) #the class is data.frame
namesector<-colnames(mat_40x40[2:41])
class(namesector) #character

hum<-vs.io(imp,exp,namesector, write.xlsx=FALSE)

#Using the Leontief Inverse
leon<-leontief.inv(mat_40x40[1:40,2:41], as.matrix(mat_40x40$DT.a.PB[1:40]))[,1:40]
hum2<-vs.io(imp,exp,namesector,leon=leon, write.xlsx=FALSE)
```

vs.ki

*Vertical Specialization*

## Description

VS is the imported input content of exports for country k in sector i. The Vertical specialization chain is  $VS\_ki = (\text{imported intermediates} / \text{gross output}) * \text{exports}$ . The first term is the share of imported inputs into gross production. Multiplying this ratio by the amount that is imported provides the monetary value for the imported input content of exports.

## Usage

```
vs.ki(imp,exp,out,namesector, write.xlsx=TRUE, name="Level_Verticalization.xlsx")
```

## Arguments

imp	Vector. Imported intermediates of sector i
exp	Vector. Exports
out	Vector. Gross Output
namesector	String. Name of Sector i
write.xlsx	Logical. if TRUE writes an excel file
name	String. name of the excel file

## Details

The dimension of the four arguments must coincide.

## Value

Returns a data frame

**Author(s)**

Ignacio Sarmiento-Barbieri

**References**

Hummels, David & Ishii, Jun & Yi, Kei-Mu, 2001. "The nature and growth of vertical specialization in world trade," *Journal of International Economics*, Elsevier, vol. 54(1), pages 75-96, June.

**Examples**

```
##---- Should be DIRECTLY executable !! ----
##-- ==> Define data, use random,
##--or do help(data=index) for the standard data sets.

## The function is currently defined as
function (x)
{
}
```

# Index

\*Topic \textasciitildekw1  
upstream, 7  
vs.ki, 9

\*Topic \textasciitildekw2  
leontief.inv, 4  
upstream, 7  
vs.ki, 9

\*Topic \textasciitildeleontief inverse  
leontief.inv, 4

\*Topic **aggregate**  
agg.matrix, 1

\*Topic **key sector**  
key.sector, 2

\*Topic **multipliers**  
multipliers, 5

\*Topic **vs**  
vs.io, 8

agg.matrix, 1

gosh.inv, 3, 6

key.sector, 2

leontief.inv, 3, 4, 6, 8

multipliers, 5

upstream, 7

vs.io, 8  
vs.ki, 9