

# **Intelligent Scissors Project**

## **Team [173]**

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# Priority Queue (Minimum Heap) :

```
public class PeriorityQueue // O(log (V))
{
    private List<Arc> H = new List<Arc>(); //  $\theta(1)$ 
    private int LeftChild(int Node) //  $\theta(1)$ 
    {
        return Node * 2 + 1; //  $\theta(1)$ 
    }
    private int RightChild(int Node) //  $\theta(1)$ 
    {
        return Node * 2 + 2; //  $\theta(1)$ 
    }
    private int Parent(int Node) //  $\theta(1)$ 
    {
        return (Node - 1) / 2; //  $\theta(1)$ 
    }
    private void ShiftUp(int Node) //  $\theta(1)$ 
    {
        if (Node == 0 || H[Node].Cost >= H[Parent(Node)].Cost) //  $\theta(1)$ 
            return; //  $\theta(1)$ 
        Arc temp = H[Parent(Node)]; //  $\theta(1)$ 
        H[Parent(Node)] = H[Node]; //  $\theta(1)$ 
        H[Node] = temp; //  $\theta(1)$ 
        ShiftUp(Parent(Node)); //  $\theta(1)$ 
    }
    private void ShiftDown(int Node) //  $\theta(1)$ 
    {
        if (LeftChild(Node) >= H.Count
            || (LeftChild(Node) < H.Count && RightChild(Node) >= H.Count
            && H[LeftChild(Node)].Cost >= H[Node].Cost)
            || (LeftChild(Node) < H.Count && RightChild(Node) < H.Count
            && H[LeftChild(Node)].Cost >= H[Node].Cost &&
            H[RightChild(Node)].Cost >= H[Node].Cost)) //  $\theta(1)$ 
            return; //  $\theta(1)$ 
        if (RightChild(Node) < H.Count && H[RightChild(Node)].Cost <=
            H[LeftChild(Node)].Cost) //  $\theta(1)$ 
        {
            Arc temp = H[RightChild(Node)]; //  $\theta(1)$ 
            H[RightChild(Node)] = H[Node]; //  $\theta(1)$ 
            H[Node] = temp; //  $\theta(1)$ 
            ShiftDown(RightChild(Node)); //  $\theta(1)$ 
        }
        else
        {
            Arc temp = H[LeftChild(Node)]; //  $\theta(1)$ 
            H[LeftChild(Node)] = H[Node]; //  $\theta(1)$ 
            H[Node] = temp; //  $\theta(1)$ 
            ShiftDown(LeftChild(Node)); //  $\theta(1)$ 
        }
    }
}
```

```

    }
    public void Push(Arc Node) //  $O(\log V)$ 
    {
        H.Add(Node); //  $\theta(1)$ 
        ShiftUp(H.Count - 1); //  $\theta(1)$ 
    }
    public Arc Pop() //  $O(\log V)$ 
    {
        Arc temp = H[0]; //  $\theta(1)$ 
        H[0] = H[H.Count - 1]; //  $\theta(1)$ 
        H.RemoveAt(H.Count - 1); //  $O(\log V)$ 
        ShiftDown(0); //  $\theta(1)$ 
        return temp; //  $\theta(1)$ 
    }
    public bool IsEmpty() //  $\theta(1)$ 
    {
        if (H.Count == 0) //  $\theta(1)$ 
            return true; //  $\theta(1)$ 
        return false; //  $\theta(1)$ 
    }
    public Arc Top() //  $\theta(1)$ 
    {
        return H[0]; //  $\theta(1)$ 
    }
}

```

Which means that a parent node can't have a greater value than its children. Thus, the minimum element is located at the root, and the maximum elements are located in the leaves. Depending on the type of heap used, the heap property may have additional requirements. So its easier to apply dijsktra algorithm.

# Dijkstra Algorithm :

```
public static List<Point> Inverting_Path(List<int> ParentList, int Dest, int
matrix_width) //  $O(E)$ 
{
    List<Point> ShortestPath = new List<Point>(); //  $\theta(1)$ 
    Stack<int> ReversedPath = new Stack<int>(); //  $\theta(1)$ 
    ReversedPath.Push(Dest); //  $\theta(1)$ 
    int Parent = ParentList[Dest]; //  $\theta(1)$ 
    while (Parent != -1) //  $\theta(E)$ 
    {
        ReversedPath.Push(Parent); //  $\theta(1)$ 
        Parent = ParentList[Parent]; //  $\theta(1)$ 
    }

    while (ReversedPath.Count != 0) //  $O(E)$ 
    {
        var TwoD = Functions.oneDtoTwoD(ReversedPath.Pop(),
matrix_width); //  $\theta(1)$ 
        Point point = new Point((int)TwoD.X, (int)TwoD.Y); //  $\theta(1)$ 
        ShortestPath.Add(point); //  $\theta(1)$ 
    }
    return ShortestPath; //  $\theta(1)$ 
}
```

Fill a stack with the selected nodes from the anchor point until reach the begging anchor point. Then Pop all the stack one by one and fill the shortest path list. So it has all the anchor points from the begging to the last anchor point (Destination)

Note: Using stack to easily reverse the anchor nodes to get the right path with low complexity.

# Generate Dijkstra Algorithm :

```
public static List<int> Dijkstra(int src, int dest, RGBPixel[,] ImageMatrix)
// O(EV)
{
    double infinity = 999999999999999999; //  $\theta(1)$ 
    int MinValue = -1; //  $\theta(1)$ 

    int W = ImageOperations.GetWidth(ImageMatrix); //  $\theta(1)$ 
    int H = ImageOperations.GetHeight(ImageMatrix); //  $\theta(1)$ 
    int Pixel_number = W * H; //  $\theta(1)$ 

    List<double> Distance = new List<double>(); //  $\theta(1)$ 
    Distance = Enumerable.Repeat(infinity, Pixel_number).ToList();
//O(E)

    List<int> ParentsPath = new List<int>(); //  $\theta(1)$ 
    ParentsPath = Enumerable.Repeat(MinValue, Pixel_number).ToList();
//O(E)

    PeriorityQueue Shortest_Distances = new PeriorityQueue(); //  $\theta(1)$ 
    Shortest_Distances.Push(new Arc(-1, src, 0)); //  $\theta(1)$ 

    if (dest == 0) // O(EV)
    {
        while (!Shortest_Distances.IsEmpty()) // O(EV)
        {
            Arc CurrentEdge = Shortest_Distances.Top(); //  $\theta(1)$ 
            Shortest_Distances.Pop(); //  $O(\log(V))$ 

            if (CurrentEdge.Cost < Distance[CurrentEdge.dest]) //
O(V)
            {
                Distance[CurrentEdge.dest] = CurrentEdge.Cost; //
 $\theta(1)$ 

                ParentsPath[CurrentEdge.dest] = CurrentEdge.src; //
 $\theta(1)$ 

                List<Arc> neighbours =
Functions.GetSibling(CurrentEdge.dest, ImageMatrix);
                int i = 0; //  $\theta(1)$ 
                var neighboursNUM = neighbours.Count; //  $\theta(1)$ 
                while (i < neighboursNUM) // O(V)
                {
                    if (Distance[neighbours[i].dest] >
Distance[neighbours[i].src] + neighbours[i].Cost) //  $\theta(1)$ 
                    {
                        neighbours[i].Cost +=
Distance[neighbours[i].src]; //  $\theta(1)$ 
                        Shortest_Distances.Push(neighbours[i]); //  $\theta(1)$ 
                    }
                }
            }
        }
    }
}
```

```

        i++; //  $\theta(1)$ 
    }
}
}
return ParentsPath; //  $\theta(1)$ 
}
else
{
    while (!Shortest_Distances.IsEmpty()) //  $O(N^3)$ 
    {
        Arc CurrentEdge = Shortest_Distances.Top(); //  $\theta(1)$ 
        Shortest_Distances.Pop(); //  $O(N)$ 

        if (CurrentEdge.Cost < Distance[CurrentEdge.dest]) //
 $O(N^2)$ 
        {
            ParentsPath[CurrentEdge.dest] = CurrentEdge.src; //
 $\theta(1)$ 
            Distance[CurrentEdge.dest] = CurrentEdge.Cost; //
 $\theta(1)$ 
            if (CurrentEdge.dest == dest) break; //  $\theta(1)$ 

            List<Arc> neighbours =
Functions.GetSibling(CurrentEdge.dest, ImageMatrix);
            int i = 0; //  $\theta(1)$ 
            while (i < neighbours.Count) //  $O(N^2)$ 
            {
                if (Distance[neighbours[i].dest] >
Distance[neighbours[i].src] + neighbours[i].Cost) //  $\Omega(1)$   $O(N)$ 
                {
                    neighbours[i].Cost +=
Distance[neighbours[i].src]; //  $\theta(1)$ 
                    Shortest_Distances.Push(neighbours[i]); //  $\Omega(1)$ 
 $O(N)$ 
                }
                i++; //  $\theta(1)$ 
            }
        }
    }
}
return ParentsPath; //  $\theta(1)$ 
}
}

public static List<Point> Create_ShortestPath(int src, int dest, RGBPixel[, ]
ImageMatrix) //  $O(EV)$ 
{
    List<int> ParentList = Dijkstra(src, dest, ImageMatrix); //  $O(EV)$ 
    return Inverting_Path(ParentList, dest,
ImageOperations.GetWidth(ImageMatrix)); //  $O(V)$ 
}

```

Using Dijkstra algorithm to find the shortest path by connecting the anchor nodes throw the least cost path to be easily back tracked. By calculating the energy difference between the pixels and their nearby pixels in four directions. And return a list holding all the pixels of the least cost shortest path.

## Crop Image Boundaries :

```
public static RGBPixel[,] CroppedImageFrame(RGBPixel[,] ImageMatrix, Boundary
border) //  $O(V^2)$ 
{
    int W = border.X_max - border.X_min; //  $\theta(1)$ 
    int H = border.Y_max - border.Y_min; //  $\theta(1)$ 

    RGBPixel[,] CroppedImage = new RGBPixel[H + 1, W + 1]; //  $\theta(1)$ 

    int i = 0; //  $\theta(1)$ 
    while (i <= H) //  $O(V^2)$ 
    {
        int j = 0; //  $\theta(1)$ 
        while (j <= W) //  $O(V)$ 
        {
            CroppedImage[i, j] = ImageMatrix[border.Y_min + i,
border.X_min + j]; //  $\theta(1)$ 
            j++; //  $\theta(1)$ 
        }
        i++; //  $\theta(1)$ 
    }
    return CroppedImage; //  $\theta(1)$ 
}
```

This function finds the width and height of the selected shortest path nodes and crop the original image into a Square or Rectangle.

# Nearby Pixels :

```
public static List<Arc> GetSibling(int Pixel, RGBPixel[,] ImageMatrix) //
    0(1)
{
    List<Arc> Sibling = new List<Arc>(); // 0(1)
    int H = ImageOperations.GetHeight(ImageMatrix); // 0(1)
    int W = ImageOperations.GetWidth(ImageMatrix); // 0(1)

    Vector2D TwoD = oneDtoTwoD(Pixel, W); // 0(1)
    int X = (int)TwoD.X; // 0(1)
    int Y = (int)TwoD.Y; // 0(1)
    var G = ImageOperations.CalculatePixelEnergies(X, Y,
ImageMatrix);
    if (X < W - 1) // 0(1)
    {
        if (G.X != 0) // 0(1)
            Sibling.Add(new Arc(Pixel, twoDtoOneD(X + 1, Y, W), 1 /
(G.X))); // 0(1)
        else // 0(1)
            Sibling.Add(new Arc(Pixel, twoDtoOneD(X + 1, Y, W),
10000000000000000)); // 0(1)
    }
    if (Y < H - 1) // 0(1)
    {
        if (G.Y != 0) // 0(1)
            Sibling.Add(new Arc(Pixel, twoDtoOneD(X, Y + 1, W), 1 /
(G.Y))); // 0(1)
        else // 0(1)
            Sibling.Add(new Arc(Pixel, twoDtoOneD(X, Y + 1, W),
10000000000000000)); // 0(1)
    }
    if (Y > 0) // 0(1)
    {
        if (G.Y != 0) // 0(1)
            Sibling.Add(new Arc(Pixel, twoDtoOneD(X, Y - 1, W), 1 /
(G.Y))); // 0(1)
        else // 0(1)
            Sibling.Add(new Arc(Pixel, twoDtoOneD(X, Y - 1, W),
10000000000000000)); // 0(1)
    }
    if (X > 0) // 0(1)
    {
        if (G.X != 0) // 0(1)
            Sibling.Add(new Arc(Pixel, twoDtoOneD(X - 1, Y, W), 1 /
(G.X))); // 0(1)
        else // 0(1)
            Sibling.Add(new Arc(Pixel, twoDtoOneD(X - 1, Y, W),
10000000000000000)); // 0(1)
    }
    return Sibling; // 0(1)
}
```



```
}
```

This function calculate difference between all the nearby energies of the current selected node in its four directions ( up, down, left, right ).

## DFS And Cropping Image :

```
private static RGBPixel[,] CroppedImage; //  $\theta(1)$ 
    public static RGBPixel[,] Cropped_Image(List<Point> MainSelection,
    RGBPixel[,] ImageMatrix) //  $O(E^2 + V)$ 
    {
        Boundary border = Border_Limits(MainSelection); // Boundary of the main selection
        CroppedImage = Functions.CroppedImageFrame(ImageMatrix, border); // get cropped image
        int counter = MainSelection.Count; //  $\theta(1)$ 
        int i = 0; //  $\theta(1)$ 
        while (i < counter) //  $O(V)$ 
        {
            int X = MainSelection[i].X - border.X_min; //  $\theta(1)$ 
            int Y = MainSelection[i].Y - border.Y_min; //  $\theta(1)$ 
            CroppedImage[Y, X].visited = true; //  $\theta(1)$ 
            i++; //  $\theta(1)$ 
        }
        filtering_Image(ImageOperations.GetWidth(CroppedImage) - 1,
        ImageOperations.GetHeight(CroppedImage) - 1); //  $O(E^2)$ 
        return CroppedImage; //  $\theta(1)$ 
    }
private static void filtering_Image(int Width , int Height) //  $O(E^2)$ 
{
    int i = 0; //  $\theta(1)$ 
    while (i <= Width) //  $O(E^2)$ 
    {
        if (!CroppedImage[0, i].visited) //  $O(E)$ 
            DFS(new Vector2D(i, 0)); //  $O(E)$ 
        i++; //  $\theta(1)$ 
    }
    i = 0; //  $\theta(1)$ 
    while (i <= Width) //  $O(E^2)$ 
    {
        if (!CroppedImage[Height, i].visited) //  $O(E)$ 
            DFS(new Vector2D(i, Height)); //  $O(E)$ 
        i++; //  $\theta(1)$ 
    }
    i = 0; //  $\theta(1)$ 
```

```

while (i <= Height) //  $O(E^2)$ 
{
    if (!CroppedImage[i, 0].visited) //  $O(E)$ 
        DFS(new Vector2D(0, i)); //  $O(E)$ 
    i++; //  $\theta(1)$ 
}
i = 0; //  $\theta(1)$ 
while (i <= Height) //  $O(E^2)$ 
{
    if (!CroppedImage[i, Width].visited) //  $O(E)$ 
        DFS(new Vector2D(Width, i)); //  $O(E)$ 
    i++; //  $\theta(1)$ 
}
}
private static void DFS(Vector2D SelectedPixel) //  $O(E)$ 
{
    Queue<Vector2D> queue = new Queue<Vector2D>(); //  $\theta(1)$ 
    queue.Enqueue(SelectedPixel); //  $\theta(1)$ 
    while (queue.Count > 0) //  $O(E)$ 
    {
        Vector2D Cpixel = queue.Dequeue(); //  $\theta(1)$ 
        bool FoundX = (Cpixel.X >= 0 && Cpixel.X <
ImageOperations.GetWidth(CroppedImage)); //  $\theta(1)$ 
        bool FoundY = (Cpixel.Y >= 0 && Cpixel.Y <
ImageOperations.GetHeight(CroppedImage)); //  $\theta(1)$ 

        if (FoundX && FoundY && !CroppedImage[(int)Cpixel.Y,
(int)Cpixel.X].visited) //  $\theta(1)$ 
        {
            //make these pixels white
            CroppedImage[(int)Cpixel.Y, (int)Cpixel.X].visited = true;
//  $\theta(1)$ 

            CroppedImage[(int)Cpixel.Y, (int)Cpixel.X].red = 255; //
 $\theta(1)$ 

            CroppedImage[(int)Cpixel.Y, (int)Cpixel.X].green = 255; //
 $\theta(1)$ 

            CroppedImage[(int)Cpixel.Y, (int)Cpixel.X].blue = 255; //
 $\theta(1)$ 

            //push arounded pixels
            queue.Enqueue(new Vector2D(Cpixel.X, Cpixel.Y + 1)); //
 $\theta(1)$ 

            queue.Enqueue(new Vector2D(Cpixel.X, Cpixel.Y - 1)); //
 $\theta(1)$ 

            queue.Enqueue(new Vector2D(Cpixel.X + 1, Cpixel.Y)); //
 $\theta(1)$ 

            queue.Enqueue(new Vector2D(Cpixel.X - 1, Cpixel.Y)); //
 $\theta(1)$ 
        }
    }
}
private static Boundary Border_Limits(List<Point> selected_points)
//  $O(V)$ 

```

```

{
    Boundary border; //  $\theta(1)$ 
    border.X_max = border.Y_max = -999999999; //  $\theta(1)$ 
    border.X_min = border.Y_min = 999999999; //  $\theta(1)$ 
    int counter = selected_points.Count; //  $\theta(1)$ 
    int i = 0; //  $\theta(1)$ 
    while ( i < counter) //  $O(V)$ 
    {
        if (selected_points[i].X > border.X_max) //  $\theta(1)$ 
            border.X_max = selected_points[i].X; //  $\theta(1)$ 

        if (selected_points[i].X < border.X_min) //  $\theta(1)$ 
            border.X_min = selected_points[i].X; //  $\theta(1)$ 

        if (selected_points[i].Y > border.Y_max) //  $\theta(1)$ 
            border.Y_max = selected_points[i].Y; //  $\theta(1)$ 

        if (selected_points[i].Y < border.Y_min) //  $\theta(1)$ 
            border.Y_min = selected_points[i].Y; //  $\theta(1)$ 
        i++; //  $\theta(1)$ 
    }
    return border; //  $\theta(1)$ 
}

```

After cropping the boundaries of the selected anchor points as a default value of False (Non-Visited) turning the part bounded by the anchor nodes into True (Visited) and keeping the rest as False (Non-Visited) then color each non-visited pixel with white background color and turning it from false (Non-Visited) into true (Visited).