
HOPKINS

```
//compute floating point RGB
float r = p.r/255.0;
float g = p.g/255.0;
float b = p.b/255.0;

//Convert to YUV
float yp =  .299*r + .587*g + .114*b;
float u = -.147*r - .289*g + .436*b;
float v =  .615*r - .515*g - .100*b;

//Invert Color
yp = .5;
u *= -1;
v *= -1;

//Back to RGB
r = yp + 0*u + 1.140*v;
g = yp - .395*u - .581*v;
b = yp + 2.032*u + 0 *v;

if (r > 1) r = 1; if (g > 1) g = 1; if (b > 1) b = 1;
if (r < 0) r = 0; if (g < 0) g = 0; if (b < 0) b = 0;

p.r = r*255; p.g = g*255; p.b = b*255;
```

# Perspective & Rays

Stephen J. Guy

Oct 2, 2017

# Processing & Sampling Review

- What's a pixel?
  - A discrete sample of a continuous image
- What's a convolution?
  - A weighted average of a signal
- How to resample (e.g., resize/rotate)?
  - Weighted average of source pixels
- Issues without sampling?
  - Aliasing
- What does aliasing look like?
- When is dithering practical?

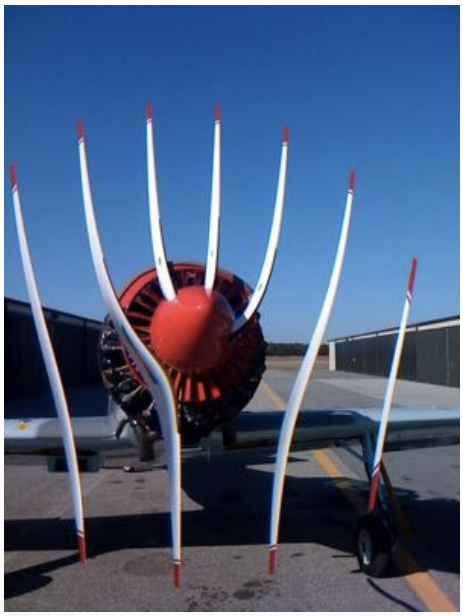
5

# What's happening here?

https://www.youtube.com/watch?v=UOfAmsQvgg4

6

# What's happening here?



7

# Rolling Shutter

8

# Real-life Dithering

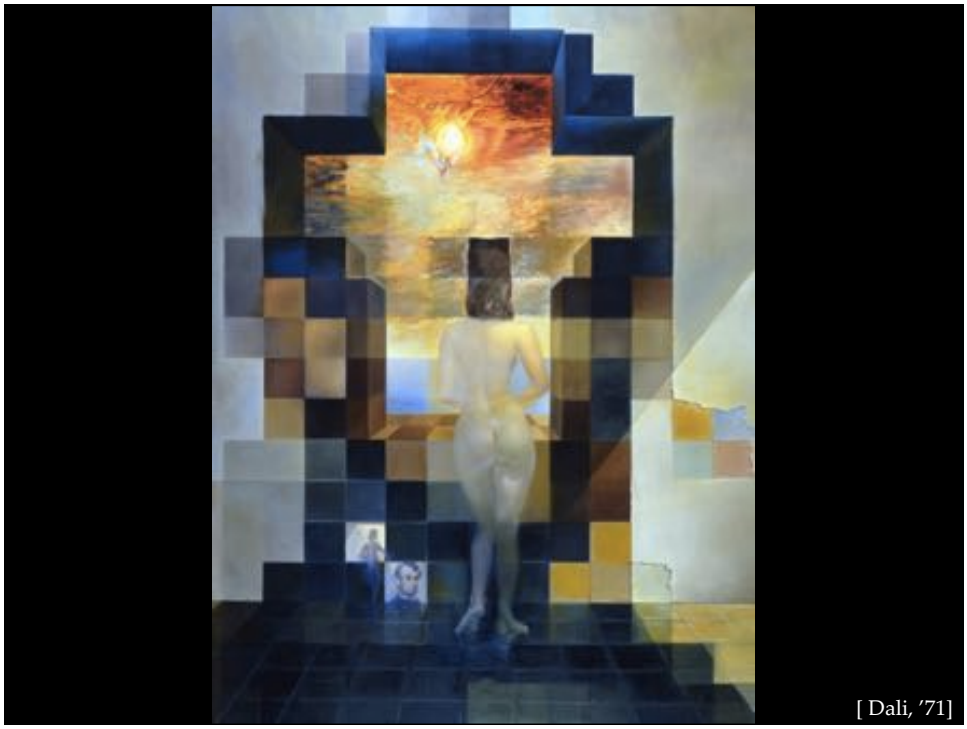
- GIFs have small color pallets

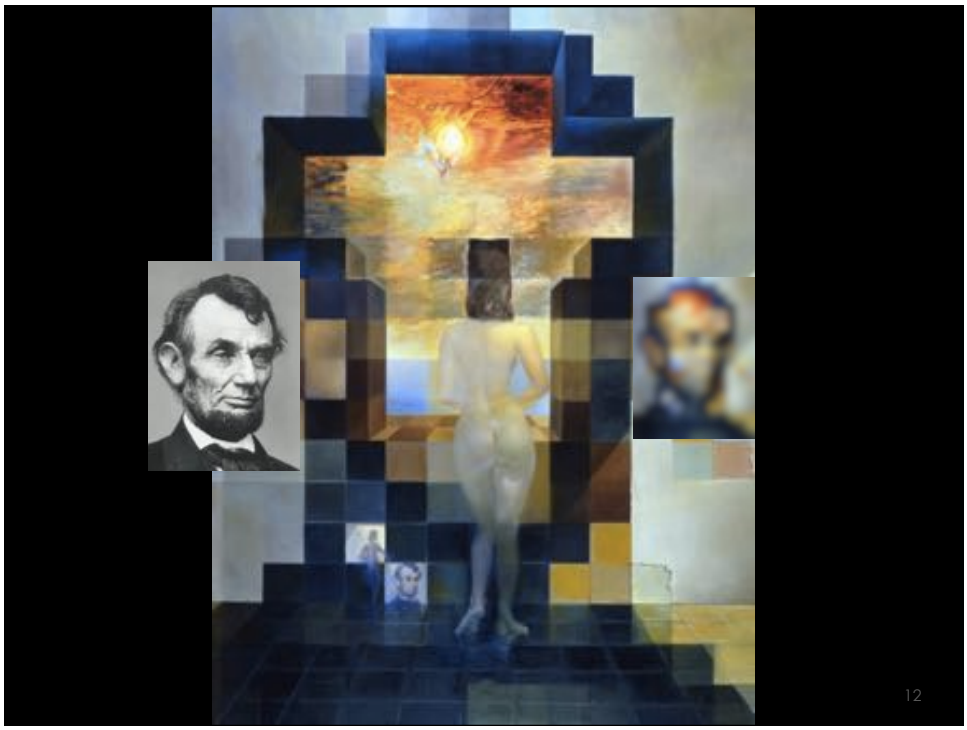


9

# Mark Rothko

10


[ Dali, ’71]



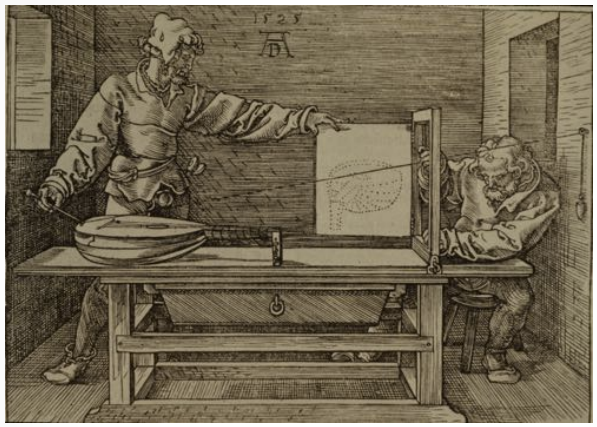
# Perspective

# Perspective

- Brings realistic depth to images

14

# Recall the Durër Woodcuts



- How would you make this an algorithm?
- What is a pixel?
- How to handle multiple objects?

15

# Two Approaches

- Object Centric vs "Pixel" Centric
  - Which is better?
  - What does physics do?

```
For each Object:
   Compute visible Pixels
   For all visible Pixels:
       If closer than previous object in pixel:
           Color pixel accordingly
```

```
For each Pixel:
   For all Objects:
       If Object intersects pixel ray
          If this is closer than previous intersection:
              Color pixel accordingly
```

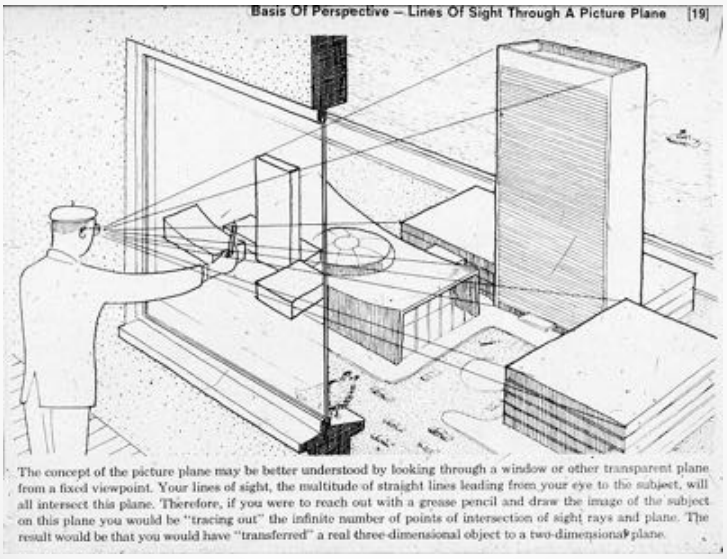
16

# Overview

- We'll start with pixel/sample-centric (~2 weeks)
  - Then move to object-centric (~3 weeks)
- Today
  - High-level concepts of perspective
  - Basic mathematical framework of ray tracing
- Wednesday
  - Algorithmic details

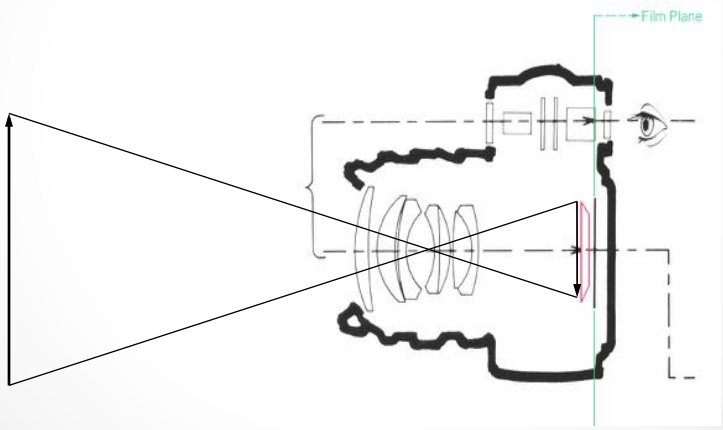
17

# Plane projection in drawing



# Projection in Photography

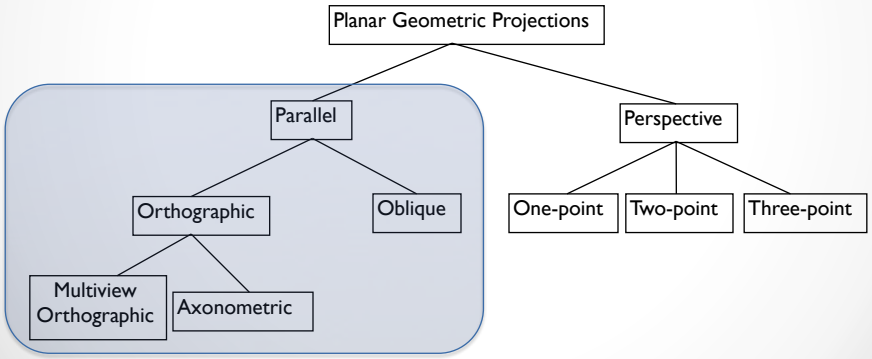
- This is another model for what we are doing
  - applies more directly in realistic rendering




[Source unknown]

# Classical projections

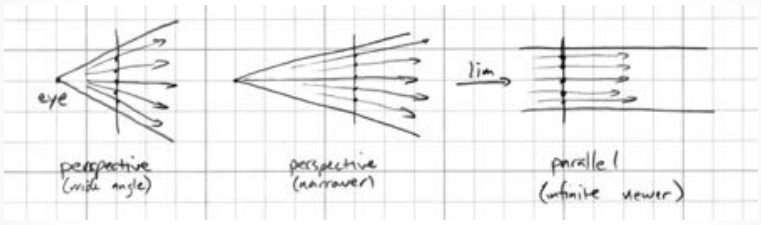
- Emphasis on cube-like objects
  - Traditional in mechanical/architectural drawing




[after Carlbom & Paciorek 78]

# Parallel Projection

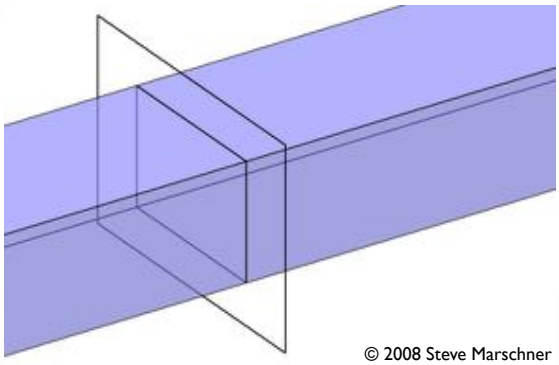
- Viewing rays are parallel rather than diverging
  - like a perspective camera that's far away



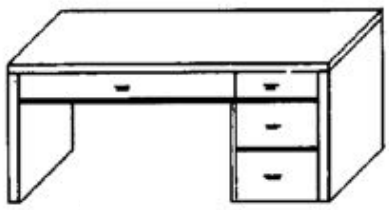

 

# View volume: Orthographic

- Bundle of rays are parallel



# Off-axis Parallel



[Carlbom & Paciorek 78]

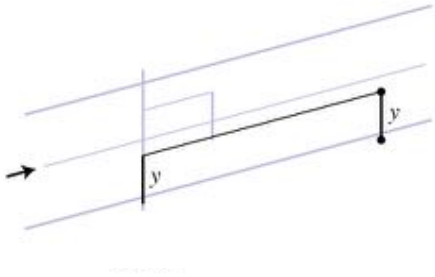
**axonometric**: projection plane perpendicular to projection direction but not parallel to coordinate planes

**oblique**: projection plane parallel to a coordinate plane but not perpendicular to projection direction.

23

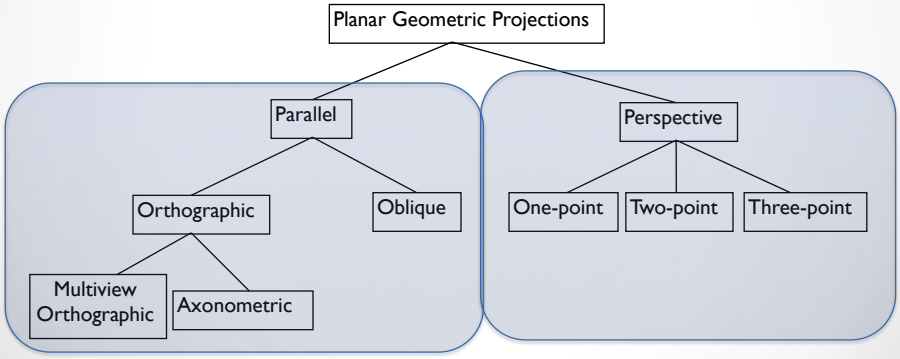
# Oblique projection

- View direction no longer coincides with projection plane normal (one more parameter)
  - objects at different distances still same size
  - objects are shifted in the image depending on their depth



# Classical projections

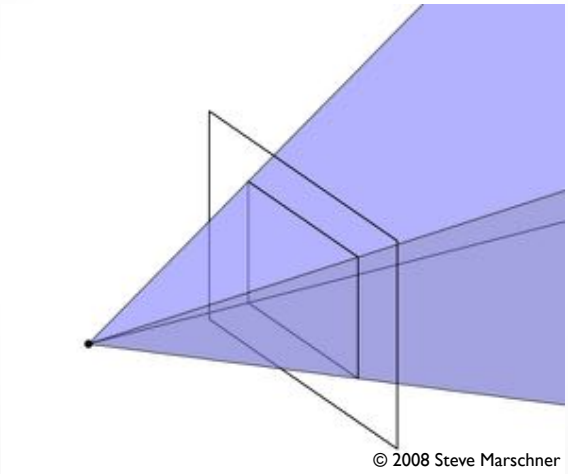
- Emphasis on cube-like objects
  - Traditional in mechanical/architectural drawing




[after Carlbom & Paciorek 78]

# View volume: Perspective

- Bundle of rays converge at the viewer



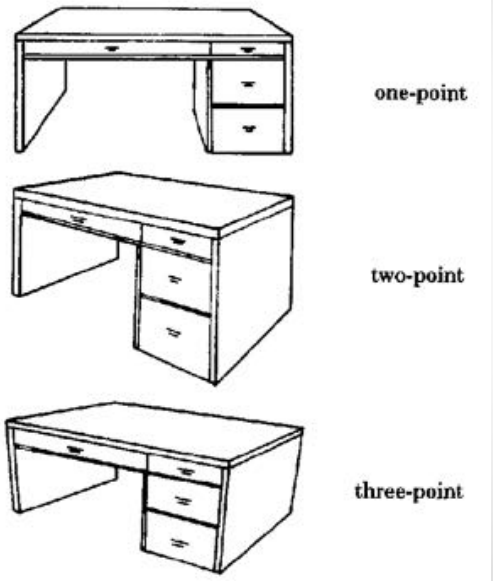

26

# Perspective

**one-point**: projection plane parallel to a coordinate plane (to two coordinate axes)

**two-point**: projection plane parallel to one coordinate axis

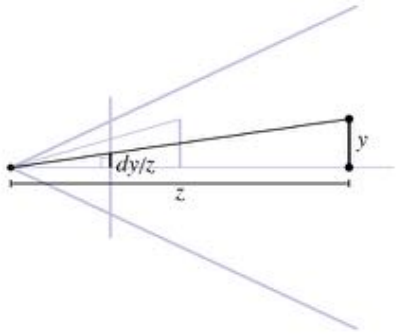
**three-point**: projection plane not parallel to a coordinate axis




[Carlbom & Paciorek 78]

# Perspective Pojection

- Perspective is projection by lines through a point
- Magnification determined by:
  - image height
  - object depth
  - image plane distance
- fov $\alpha = 2\ \text{atan}(h/(2d))$
- $y' = dy/z$
- Assumes project plane is perpendicular to viewing direction
  - "Normal" camera



# Field of view (or f.o.v.)

- Angle between rays corresponding to opposite edges of a perspective image
  - easy to compute only for "normal" perspective
  - different measures: vert., horiz., or diag.
- In cameras, determined by focal length
  - confusing because of many image sizes
  - for 35mm format (36mm by 24mm image)
    - 18mm = 67° v.f.o.v. – super-wide angle
    - 28mm = 46° v.f.o.v. – wide angle
    - 50mm = 27° v.f.o.v. – "normal"
    - 100mm = 14° v.f.o.v. – narrow angle ("telephoto")

# Field of view

- Effects "strength" of perspective effects
  - Real cameras wide lenses are difficult, specialty tools
  - Graphics you can type any number … w/ odd effects!

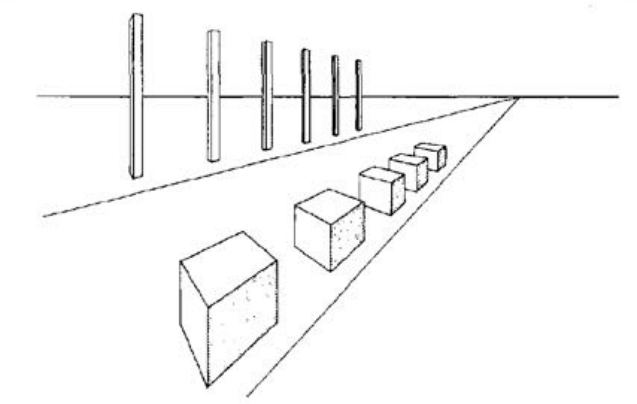
close viewpoint
wide angle
prominent foreshortening

far viewpoint
narrow angle
little foreshortening

[Ansel Adams]

# Perspective Distortions

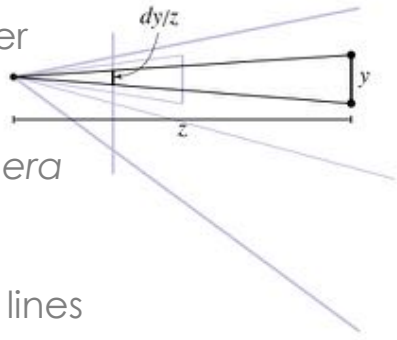
- Lengths, length ratios, angles



[Carlbom & Paciorek 78]

# Shifted Perspective Projection

- Perspective but with projection plane not perpendicular to view direction
  - additional parameter: projection plane normal
  - exactly equivalent to cropping out an off-center rectangle from a larger "normal" perspective
  - corresponds to *view camera* in photography
- Why use this?
  - Controls convergence of lines



[Philip Greenspun]

camera tilted up: converging vertical lines

33

[Philip Greenspun]

lens shifted up: parallel vertical lines

# Specifying Perspective Projections

- Many ways possible – most common:
  - From, At, Up, Hfov (more needed for shifted)
- One way (used in ray tracing):
  - viewpoint, view direction, up
    - establishes location and orientation of viewer
    - view direction is the direction of the center ray
  - image width & height, projection distance
    - establishes size and location of image rectangle
  - image plane normal
    - can be different from view direction to get shifted perspective

# Ray Tracing

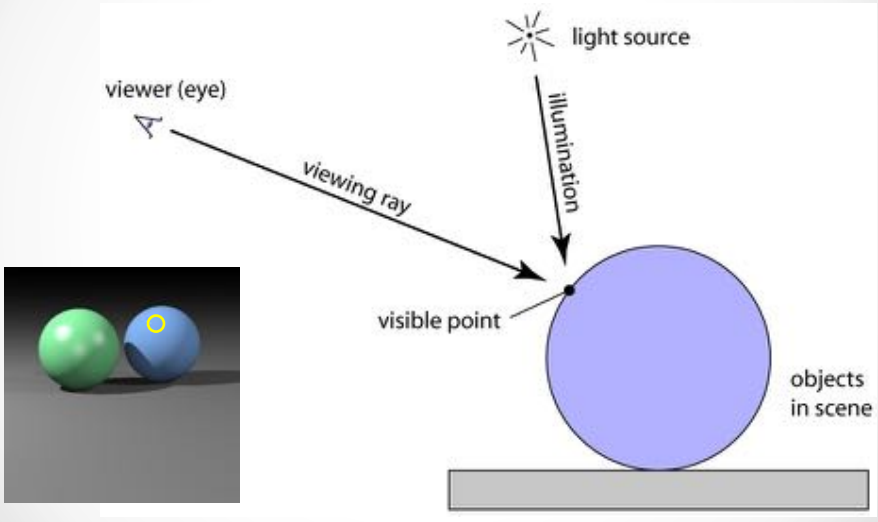
36

# Ray Tracing Lectures

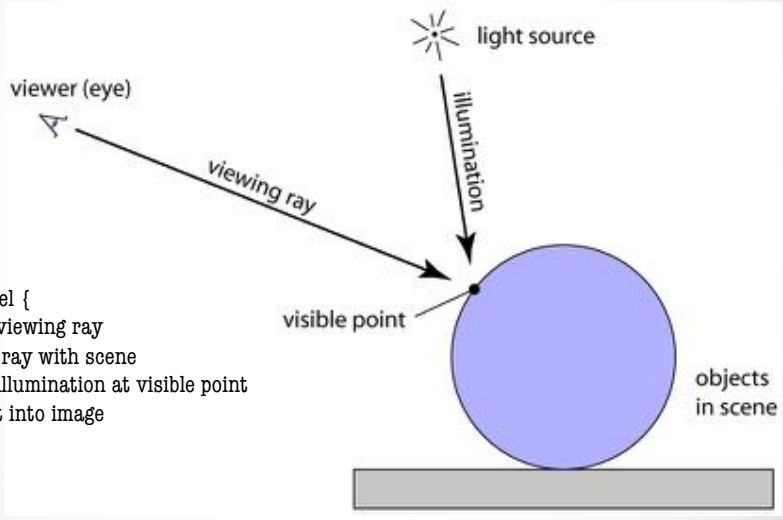
- Today
  - Introduction & Basic Idea
  - Just enough to get you started thinking about how to approach HW2
- Wednesday
  - Equations & Algorithms
  - Everything you need to finish HW2
- Next Week
  - Advanced lighting models
  - Role of recursion
  - Acceleration data structures
  - Everything needed to finish HW3

37

# Ray tracing idea



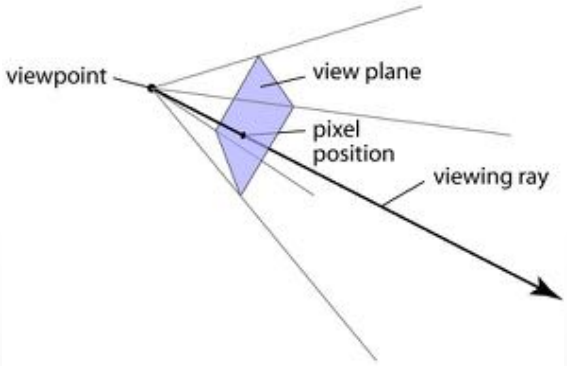
# Ray tracing algorithm



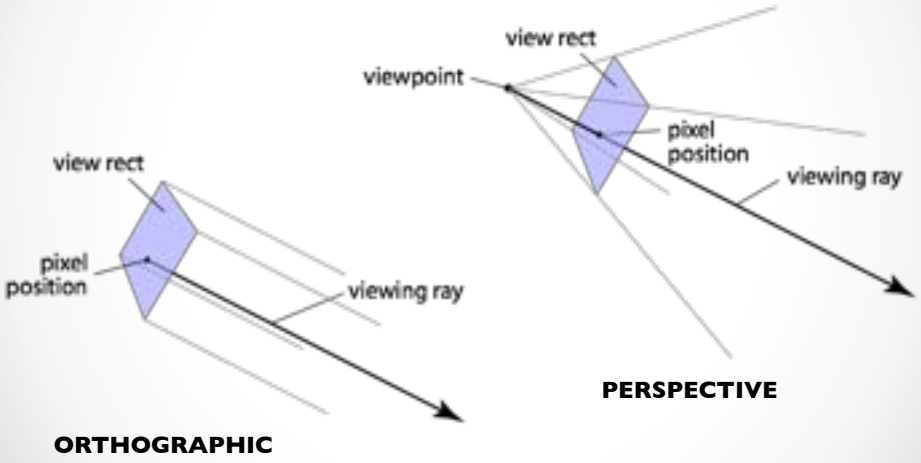

```
for each pixel {
    compute viewing ray
    intersect ray with scene
    compute illumination at visible point
    put result into image
    }
```

# Generating eye rays

- Use window analogy directly

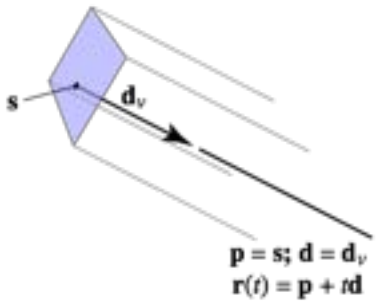


# Generating eye rays




# Eye rays: orthographic

- Just need to compute the view plane point **s**:

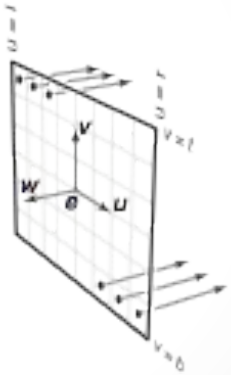



  - **s** moves through each pixel in image plane

42

# Eye rays: orthographic

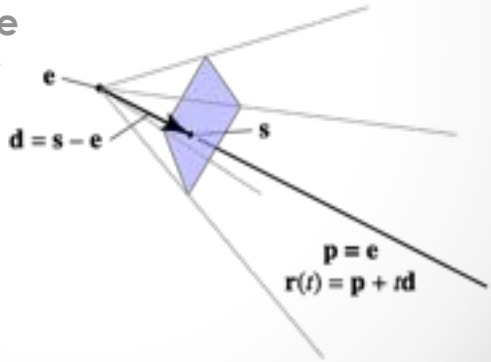
$$\mathbf{s} = \mathbf{e} + u\mathbf{u} + v\mathbf{v}$$
$$\mathbf{p} = \mathbf{s};\ \mathbf{d} = -\mathbf{w}$$
$$\mathbf{r}(t) = \mathbf{p} + t\mathbf{d}$$






# Eye rays: Perspective

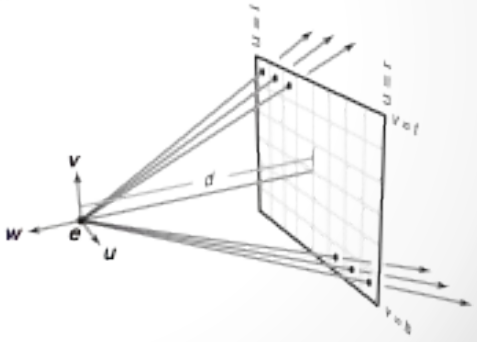
- View rectangle needs to be away from viewpoint
- Distance is important: "focal length" of camera
  - still use camera frame but position view rect away from viewpoint
  - ray origin always **e**
  - ray direction now controlled by **s**



# Eye rays: Perspective

- Compute **s** in the same way; just subtract *d***w**
  - coordinates of **s** are (*u*, *v*, –*d*)

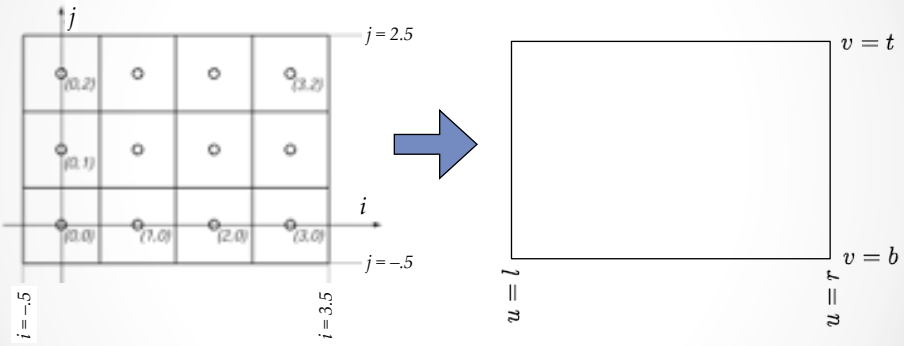
$$\mathbf{s} = \mathbf{e} + u\mathbf{u} + v\mathbf{v} - d\mathbf{w}$$
$$\mathbf{p} = \mathbf{e};\ \mathbf{d} = \mathbf{s} - \mathbf{e}$$
$$\mathbf{r}(t) = \mathbf{p} + t\mathbf{d}$$



# Pixel-to-image mapping

- One last detail: (*u*, *v*) coords of a pixel




$$u = l + (r - l)(i + 0.5)/n_x$$
$$v = b + (t - b)(j + 0.5)/n_y$$

# Ray-Object Intersection

- Test each pixel ray against each object in the scene
- If it hits, color the pixel by the object color
- Question:
  - How to intersect a ray w/ an object?

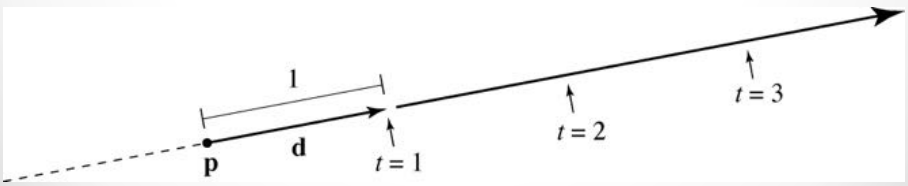
47

# What is Ray: a half line

- Standard representation: point **p** and direction **d**

$$\mathbf{r}(t) = \mathbf{p} + t\mathbf{d}$$

  - this is a *parametric equation* for the line
  - lets us directly generate the points on the line
  - if we restrict to $t > 0$ then we have a ray
  - note replacing **d** with $a$**d** doesn't change ray ($a > 0$)



# Ray-sphere intersection

- Condition 1: point is on ray

$$\mathbf{r}(t) = \mathbf{p} + t\mathbf{d}$$

- Condition 2: point is on sphere
  - assume unit sphere; see book for general

$$\|\mathbf{x}\| = 1 \Leftrightarrow \|\mathbf{x}\|^2 = 1$$

$$f(\mathbf{x}) = \mathbf{x} \cdot \mathbf{x} - 1 = 0$$

- Substitute:

$$(\mathbf{p} + t\mathbf{d}) \cdot (\mathbf{p} + t\mathbf{d}) - 1 = 0$$

  - this is a quadratic equation in *t*



# Ray-sphere intersection

- Solution for *t* by quadratic formula:

$$t = \frac{-\mathbf{d} \cdot \mathbf{p} \pm \sqrt{(\mathbf{d} \cdot \mathbf{p})^2 - (\mathbf{d} \cdot \mathbf{d})(\mathbf{p} \cdot \mathbf{p} - 1)}}{\mathbf{d} \cdot \mathbf{d}}$$

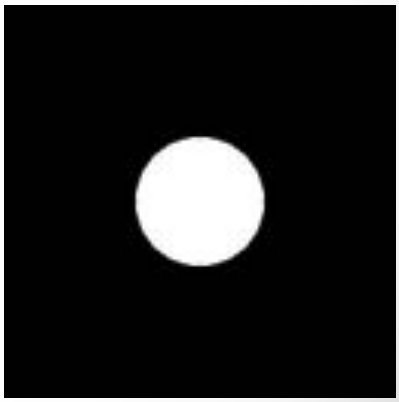
$$t = -\mathbf{d} \cdot \mathbf{p} \pm \sqrt{(\mathbf{d} \cdot \mathbf{p})^2 - \mathbf{p} \cdot \mathbf{p} + 1}$$

  - simpler form holds when **d** is a unit vector but we can't assume this unless we normalize **d**

# Image so far

- With eye ray generation and sphere intersection

```
Surface s = new Sphere((0.0, 0.0, 0.0), 1.0);
for 0 <= iy < ny
   for 0 <= ix < nx {
      ray = camera.getRay(ix, iy);
      hitSurface, t = s.intersect(ray, 0, +inf)
      if hitSurface is not null
         image.set(ix, iy, white);
   }
```



# With Many Shapes

```
Group.intersect (ray, tMin, tMax) {
   tBest = +inf; firstSurface = null;
   for surface in surfaceList {
      hitSurface, t = surface.intersect(ray, tMin, tBest);
      if hitSurface is not null {
         tBest = t;
         firstSurface = hitSurface;
      }
   }
return hitSurface, tBest;
}
```

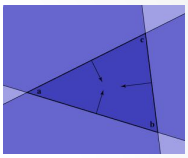
# Image so far

- With eye ray generation and scene intersection

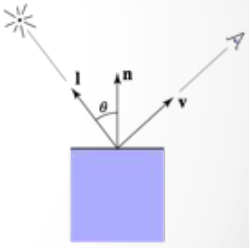
```
for 0 <= iy < ny
   for 0 <= ix < nx {
      ray = camera.getRay(ix, iy);
      c = scene.trace(ray, 0, +inf);
      image.set(ix, iy, c);
   }

...

Scene.trace(ray, tMin, tMax) {
   surface, t = surfs.intersect(ray, tMin, tMax);
   if (surface != null) return surface.color();
   else return black;
}
```

# Advancements

- Support more shapes
  - Ray-plane intersection
  - Ray-triangle intersection



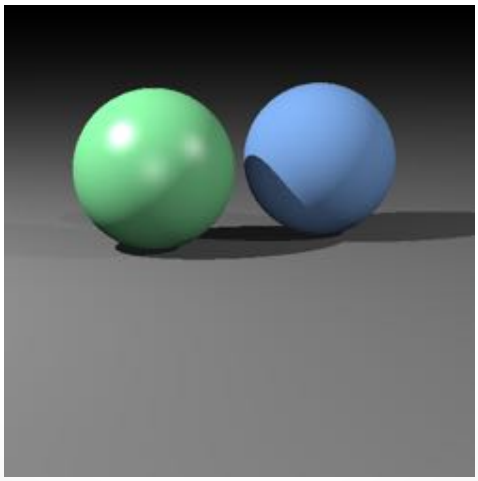
- Lighting models (shading)
  - How much light gets reflected to the camera?
  - Mirrored/glossy materials
  - Shadows




54

# Next Time

- Phong Shading w/ Shadows



55

# Announcements

- Assignment 1 grades are posted
- Assignment 2 should be online – Raytracing!
- One of the most rewarding & frustrating projects in all of CS
  - Split into two parts over ~3 weeks
  - First part due on Wednesday 10/11
  - 2nd part due on Monday 10/23
  - Midterm Week of 10/29

56

# HW 2 & 3 - Raytracing

- Will have 3 weeks to finish
- Counts 1.5x other assignments

- 50 pts from check-in at halfway point (HW2)
- 100 pts from final product (HW3)

- Try to finish Step 1 from the strategy guide today!
  - Come with questions on Wednesday

57

# Math Background

- Should be very familiar with rays & geometry

- Read Chapter 2 of book to refresh

58

# HW 0 is Graded

- Let me know if there is any issue
  - I'll share some of the art entries soon
- H1 submissions are looking cool: