

# Lists, Stacks, and Queues

Computer Science E-22  
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## Representing a Sequence: Arrays vs. Linked Lists

- Sequence – an ordered collection of items (position matters)
  - we will look at several types: lists, stacks, and queues
- Can represent any sequence using an array *or* a linked list

	<i><b>array</b></i>	<i><b>linked list</b></i>
representation in memory	elements occupy consecutive memory locations	nodes can be at arbitrary locations in memory; the links connect the nodes together
advantages		
disadvantages		

## A List as an Abstract Data Type

- list = a sequence of items that supports at least the following functionality:
  - accessing an item at an arbitrary position in the sequence
  - adding an item at an arbitrary position
  - removing an item at an arbitrary position
  - determining the number of items in the list (the list's *length*)
- ADT: specifies *what* a list will do, without specifying the implementation

## Review: Specifying an ADT Using an Interface

- Recall that in Java, we can use an interface to specify an ADT:

```
public interface List {  
    Object getItem(int i);  
    boolean addItem(Object item, int i);  
    int length();  
    ...  
}
```

- We make any implementation of the ADT a class that implements the interface:

```
public class MyList implements List {  
    ...  
}
```

- This approach allows us to write code that will work with different implementations of the ADT:

```
public static void processList(List l) {  
    for (int i = 0; i < l.length(); i++) {  
        Object item = l.getItem(i);  
        ...  
    }  
}
```

## Our List Interface

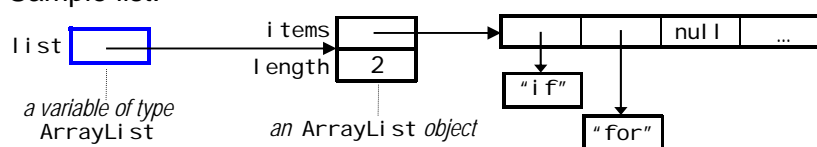
```
public interface List {  
    Object getItem(int i);  
    boolean addItem(Object item, int i);  
    Object removeItem(int i);  
    int length();  
    boolean isFull();  
}
```

- We include an `isFull()` method to test if the list already has the maximum number of items
- Recall that all methods in an interface are assumed to be public.
- The actual interface definition includes comments that describe what each method should do.

## Implementing a List Using an Array

```
public class ArrayList implements List {  
    private Object[] items;  
    private int length;  
  
    public ArrayList(int maxSize) {  
        items = new Object[maxSize];  
        length = 0;  
    }  
  
    public int length() {  
        return length;  
    }  
  
    public boolean isFull() {  
        return (length == items.length);  
    }  
    ...  
}
```

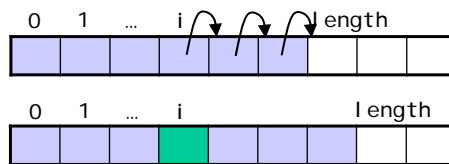
- Sample list:



## Adding an Item to an ArrayList

- Adding at position  $i$  (shifting items  $i, i+1, \dots$  to the right by one):

```
public boolean addItem(Object item, int i) {  
    if (i < 0 || i > length)  
        throw new IndexOutOfBoundsException();  
    if (isFull())  
        return false;  
  
    // make room for the new item  
    for (int j = length - 1; j >= i; j--)  
        items[j + 1] = items[j];  
  
    items[i] = item;  
    length++;  
    return true;  
}
```

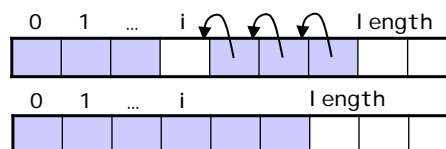


## Other ArrayList Methods

- Getting item  $i$ :  

```
public Object getItem(int i) {  
    if (i < 0 || i >= length)  
        throw new IndexOutOfBoundsException();  
    return items[i];  
}
```
- Removing item  $i$  (shifting items  $i+1, i+2, \dots$  to the left by one):

```
public Object removeItem(int i) {  
    if (i < 0 || i >= length)  
        throw new IndexOutOfBoundsException();  
}
```



## Converting an ArrayList to a String

- The `toString()` method is designed to allow objects to be displayed in a human-readable format.
- This method is called implicitly when you attempt to print an object or when you perform string concatenation:

```
ArrayList l = new ArrayList();  
System.out.println(l);  
String str = "My list: " + l;  
System.out.println(str);
```

- A default version of this method is inherited from the `Object` class.
  - returns a `String` consisting of the type of the object and a hash code for the object.
- It usually makes sense to override the default version.

## toString() Method for the ArrayList Class

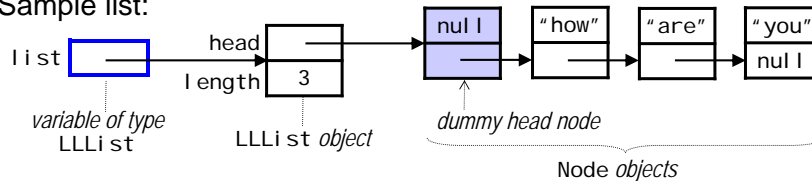
```
public String toString() {  
    String str = "{";  
    if (length > 0) {  
        for (int i = 0; i < length - 1; i++)  
            str = str + items[i] + ", ";  
        str = str + items[length - 1];  
    }  
    str = str + "}"  
    return str;  
}
```

- Produces a string of the following form:  
`{items[0], items[1], ... }`
- Why is the last item added outside the loop?
- Why do we need the `if` statement?

## Implementing a List Using a Linked List

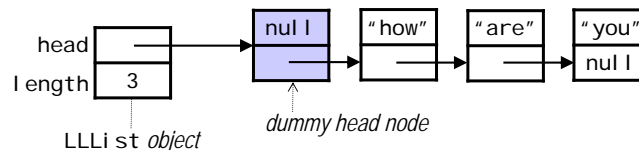
```
public class LLLi st implements Li st {
    private Node head; // dummy head node
    private int length;
    ...
}
```

- Sample list:

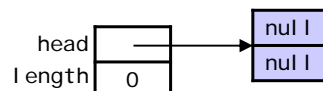


- Differences from the linked list we used for strings:
  - we “embed” the linked list inside another class
    - users of our LLLi st class will never actually touch the nodes
    - users of our Stri ngNode class hold a reference to the first node
  - we use a dummy head node
  - we use instance methods instead of static methods
    - myLi st. l ength() instead of l ength(myLi st)

## Using a Dummy Head Node



- The dummy head node is always at the front of the linked list.
  - like the other nodes in the linked list, it's of type Node
  - it does *not* store an item
  - it does *not* count towards the length of the list
- An empty LLLi st still has a dummy head node:

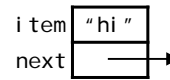


- Using a dummy head node allows us to avoid special cases when adding and removing nodes from the linked list.

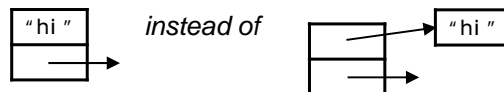
## An Inner Node Class

```
public class LLLi st implements List {
    private class Node {
        private Object i tem;
        private Node next;

        private Node(Object i , Node n) {
            i tem = i;
            next = n;
        }
    }
    ...
}
```



- We make Node an *inner class*, defining it within LLLi st.
  - allows the LLLi st methods to directly access Node's private members, while restricting all other access
  - the compiler creates this class file: LLLi st\$Node. cl ass
- For simplicity, our diagrams show the items inside the nodes.



## Other Details of Our LLLi st Class

```
public class LLLi st implements List {
    private class Node {
        ...
    }

    private Node head;
    private int length;

    public LLLi st() {
        head = new Node(null , null);
        length = 0;
    }

    public boolean isFull () {
        return false;
    }
}
```

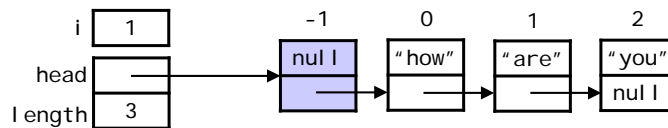
- Unlike ArrayLi st, there's no need to preallocate space for the items. The constructor simply creates the dummy head node.
- The linked list can grow indefinitely, so the list is never full!

## Getting a Node

- Private helper method for getting node  $i$ 
  - to get the dummy head node, use  $i = -1$

```
private Node getNode(int i) {
    // private method, so we assume i is valid!

    Node trav = _____;
    int travIndex = -1;
    while ( _____ ) {
        travIndex++;
        _____;
    }
    return trav;
}
```



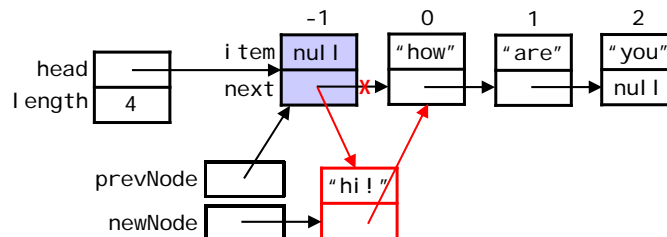
## Adding an Item to an LLList

```
public boolean addItem(Object item, int i) {
    if (i < 0 || i > length)
        throw new IndexOutOfBoundsException();

    Node newNode = new Node(item, null);
    Node prevNode = getNode(i - 1);
    newNode.next = prevNode.next;
    prevNode.next = newNode;

    length++;
    return true;
}
```

- This works even when adding at the front of the list ( $i == 0$ ):





## addItem() Without a Dummy Head Node

```
public boolean addItem(Object item, int i) {
    if (i < 0 || i > length)
        throw new IndexOutOfBoundsException();

    Node newNode = new Node(item, null);

    if (i == 0) {                // case 1: add to front
        newNode.next = first;
        first = newNode;
    } else {                    // case 2: i > 0
        Node prevNode = getNode(i - 1);
        newNode.next = prevNode.next;
        prevNode.next = newNode;
    }

    length++;
    return true;
}
```

(instead of a reference named head to the dummy head node, this implementation maintains a reference named first to the first node, which does hold an item).

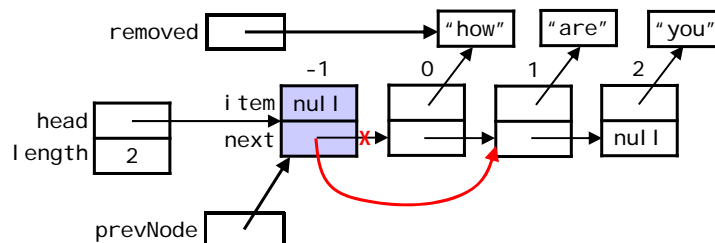
## Removing an Item from an LinkedList

```
public Object removeItem(int i) {
    if (i < 0 || i >= length)
        throw new IndexOutOfBoundsException();

    Node prevNode = getNode(i - 1);
    Object removed = prevNode.next.item;
    _____ // what line goes here?

    length--;
    return removed;
}
```

- This works even when removing the first item (i == 0):



### toString() Method for the LinkedList Class

```
public String toString() {  
    String str = "{";  
  
    // what should go here?  
  
    str = str + " }"  
    return str;  
}
```

### Counting the Number of Occurrences of an Item

- One possible approach:

```
public class MyClass {  
    public static int numOccur(List l, Object item) {  
        int numOccur = 0;  
        for (int i = 0; i < l.length(); i++) {  
            Object itemAt = l.getItem(i);  
            if (itemAt.equals(item))  
                numOccur++;  
        }  
        return numOccur;  
    }  
}
```

- Problem: for LinkedList objects, each call to getItem() starts at the head of the list and traverses to item i.
  - to access item 0, access 1 node
  - to access item 1, access 2 nodes
  - to access item i, access i+1 nodes
  - if length = n, total nodes accessed =  $1 + 2 + \dots + n = O(n^2)$

### Solution 1: Make numOccur() an LLList Method

```
public class LLList {
    public int numOccur(Object item) {
        int numOccur = 0;
        Node trav = head.next; // skip the dummy head node
        while (trav != null) {
            if (trav.item.equals(item))
                numOccur++;
            trav = trav.next;
        }
        return numOccur;
    } ...
}
```

- Each node is only visited once, so the # of accesses =  $n = O(n)$
- Problem: we can't anticipate all of the types of operations that users may wish to perform.
- We would like to give users the general ability to iterate over the list.

### Solution 2: Give Access to the Internals of the List

- Make our private helper method getNode() a public method.
- Make Node a non-inner class and provide getter methods.
- This would allow us to do the following:

```
public class MyClass {
    public static int numOccur(LLList l, Object item) {
        int numOccur = 0;
        Node trav = l.getNode(0);
        while (trav != null) {
            Object itemAt = trav.getItem();
            if (itemAt.equals(item))
                numOccur++;
            trav = trav.getNext();
        }
        return numOccur;
    } ...
}
```

- What's wrong with this approach?

### Solution 3: Provide an Iterator

- An iterator is an object that provides the ability to iterate over a list *without* violating encapsulation.

- Our iterator class will implement the following interface:

```
public interface ListIterator {  
    // Are there more items to visit?  
    boolean hasNext();  
    // Return next item and advance the iterator.  
    Object next();  
}
```

- The iterator starts out prepared to visit the first item in the list, and we use `next()` to access the items sequentially.

- Ex: position of the iterator is shown by the cursor symbol (|)

after the iterator <code>i</code> is created:		"do"	"we"	"go"	...
after calling <code>i.next()</code> , which returns "do":	"do"		"we"	"go"	...
after calling <code>i.next()</code> , which returns "we":	"do"	"we"		"go"	...

### numOccur() Using an Iterator

```
public class MyClass {  
    public static int numOccur(List l, Object item) {  
        int numOccur = 0;  
        ListIterator iter = l.iterator();  
        while (iter.hasNext()) {  
            Object itemAt = iter.next();  
            if (itemAt.equals(item))  
                numOccur++;  
        }  
        return numOccur;  
    } ...  
}
```

- The `iterator()` method returns an iterator object that is ready to visit the first item in the list. (Note: we also need to add the header of this method to the `List` interface.)
- Note that `next()` does two things at once:
  - gets an item
  - advances the iterator.

## Using an Inner Class for the Iterator

```
public class LLList {  
    public ListIterator iterator() {  
        return new LLListIterator();  
    }  
  
    private class LLListIterator implements ListIterator {  
        private Node nextNode;  
        private Node lastVisitedNode;  
        public LLListIterator() {  
            ...  
        }  
    }  
}
```

- Using an inner class gives the iterator access to the list's internals.
- Because LLListIterator is a private inner class, methods outside LLList can't create LLListIterator objects or have variables that are declared to be of type LLListIterator.
- Other classes use the *interface name* as the declared type, e.g.:  
ListIterator iter = l.iterator();

## LLListIterator Implementation

```
private class LLListIterator implements ListIterator {  
    private Node nextNode;  
    private Node lastVisitedNode;  
  
    public LLListIterator() {  
        nextNode = head.next;    // skip over head node  
        lastVisitedNode = null;  
    }  
    ...  
}
```

- Two instance variables:
  - nextNode keeps track of the next node to visit
  - lastVisitedNode keeps track of the most recently visited node
    - not needed by hasNext() and next()
    - what iterator operations might we want to add that *would* need this reference?

### LLListIterator Implementation (cont.)

```
private class LListIterator implements ListIterator {
    private Node nextNode;
    private Node lastVisitedNode;

    public LListIterator() {
        nextNode = head.next;    // skip over dummy node
        lastVisitedNode = null;
    }

    public boolean hasNext() {
        return (nextNode != null);
    }

    public Object next() {
        if (nextNode == null)
            throw new NoSuchElementException();

        Object item = nextNode.item;
        lastVisited = nextNode;
        nextNode = nextNode.next;
        return item;
    }
}
```

### More About Iterators

- In theory, we could write list-iterator methods that were methods of the list class itself.
- Instead, our list-iterator methods are encapsulated within an iterator object.
  - allows us to have multiple iterations active at the same time:

```
ListIterator i = l.iterator();
while (i.hasNext()) {
    ListIterator j = l.iterator();
    while (j.hasNext()) {
        ...
    }
}
```
- Java's built-in *collection classes* all provide iterators.
  - `LinkedList`, `ArrayList`, etc.
  - the built-in `Iterator` interface specifies the iterator methods
    - they include `hasNext()` and `next()` methods like ours

## Efficiency of the List Implementations

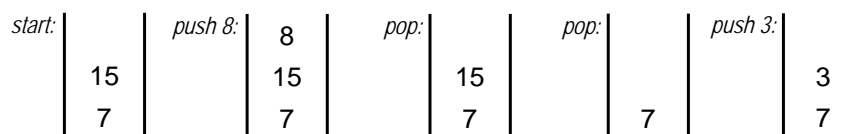
$n$  = number of items in the list

	ArrayList	LinkedList
getItem()		
addItem()		
removeItem()		
space efficiency		

## Stack ADT



- A stack is a sequence in which:
  - items can be added and removed only at one end (the *top*)
  - you can only access the item that is currently at the top
- Operations:
  - push: add an item to the top of the stack
  - pop: remove the item at the top of the stack
  - peek: get the item at the top of the stack, but don't remove it
  - isEmpty: test if the stack is empty
  - isFull: test if the stack is full
- Example: a stack of integers



## A Stack Interface: First Version

```
public interface Stack {
    boolean push(Object item);
    Object pop();
    Object peek();
    boolean isEmpty();
    boolean isFull();
}
```

- push() returns false if the stack is full, and true otherwise.
- pop() and peek() take no arguments, because we know that we always access the item at the top of the stack.
  - return null if the stack is empty.
- The interface provides no way to access/insert/delete an item at an arbitrary position.
  - encapsulation allows us to ensure that our stacks are manipulated only in ways that are consistent with what it means to be stack

## Implementing a Stack Using an Array: First Version

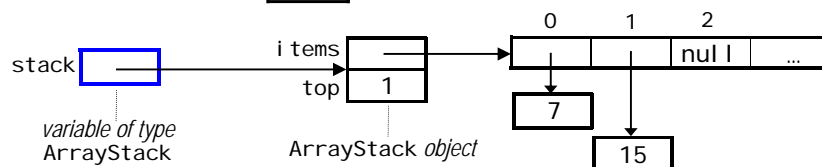
```
public class ArrayStack implements Stack {
    private Object[] items;
    private int top;    // index of the top item

    public ArrayStack(int maxSize) {
        items = new Object[maxSize];
        top = -1;
    }
    ...
}
```

- Example: the stack 

15
7

 would be represented as follows:



- Items are added from left to right. The instance variable `top` stores the index of the item at the top of the stack.



## Limiting a Stack to Objects of a Given Type

- We can do this by using a *generic* interface and class.

- Here is a generic version of our Stack interface:

```
public interface Stack<T> {  
    boolean push(T item);  
    T pop();  
    T peek();  
    boolean isEmpty();  
    boolean isFull();  
}
```

- It includes a *type variable* T in its header and body.
- This type variable is used as a placeholder for the actual type of the items on the stack.

## A Generic ArrayStack Class

```
public class ArrayStack<T> implements Stack<T> {  
    private T[] items;  
    private int top;    // index of the top item  
    ...  
    public boolean push(T object) {  
        ...  
    }  
    ...  
}
```

- Once again, a type variable T is used as a placeholder for the actual type of the items.
- When we create an ArrayStack, we specify the type of items that we intend to store in the stack:

```
ArrayStack<Integer> s1 = new ArrayStack<Integer>(10);  
ArrayStack<String> s2 = new ArrayStack<String>(5);  
ArrayStack<Object> s3 = new ArrayStack<Object>(20);
```

## ArrayStack Constructor

- Java doesn't allow you to create an object or array using a type variable. Thus, we *cannot* do this:

```
public ArrayStack(int maxSize) {  
    items = new T[maxSize];    // not allowed  
    top = -1;  
}
```

- To get around this limitation, we create an array of type Object and cast it to be an array of type T:

```
public ArrayStack(int maxSize) {  
    items = (T[])new Object[maxSize];  
    top = -1;  
}
```

(This doesn't produce a `ClassCastException` at runtime, because in the compiled version of the class, `T` is replaced with `Object`.)

- The cast generates a compile-time warning, but we'll ignore it.
- Java's built-in `ArrayList` class takes this same approach.

## More on Generics

- When a collection class uses the type `Object` for its items, we often need to use casting:

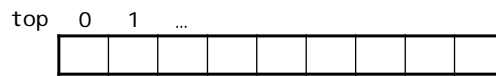
```
LinkedList list = new LinkedList();  
list.addItem("hello");  
list.addItem("world");  
String item = (String)list.getItem(0);
```

- Using generics allows us to avoid this:

```
ArrayStack<String> s = new ArrayStack<String>;  
s.push("hello");  
s.push("world");  
String item = s.pop();    // no casting needed
```

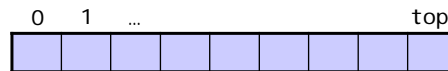
## Testing if an ArrayStack is Empty or Full

- Empty stack:



```
public boolean isEmpty() {  
    return (top == -1);  
}
```

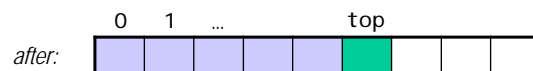
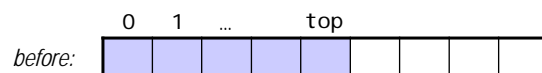
- Full stack:



```
public boolean isFull() {  
    return (top == items.length - 1);  
}
```

## Pushing an Item onto an ArrayStack

- We increment top before adding the item:



```
public boolean push(T item) {  
    if (isFull())  
        return false;  
    top++;  
    items[top] = item;  
    return true;  
}
```

## ArrayStack pop() and peek()

- pop: need to get `items[top]` *before* we decrement `top`.



```
public T pop() {  
    if (isEmpty())  
        return null;  
    T removed = items[top];  
    items[top] = null;  
    top--;  
    return removed;  
}
```

- peek just returns `items[top]` without decrementing `top`.

## toString() Method for the ArrayStack Class

- Assume that we want the method to show us everything in the stack – returning a string of the form

`"{top, one-below-top, two-below-top, ... bottom}"`

```
public String toString() {  
    String str = "{";  
  
    // what should go here?
```

```
    str = str + "}"  
    return str;  
}
```

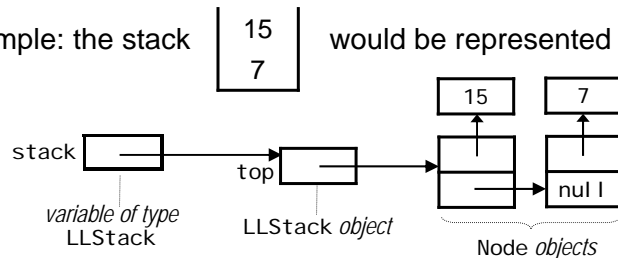
## Implementing a Generic Stack Using a Linked List

```
public class LLStack<T> implements Stack<T> {
    private Node top;    // top of the stack
    ...
}
```

- Example: the stack 

15
7

 would be represented as follows:



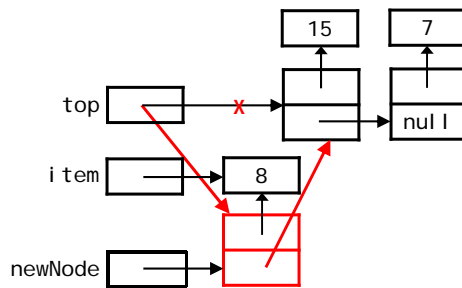
- Things worth noting:
  - our `LLStack` class needs only a single instance variable—a reference to the first node, which holds the top item
  - top item = leftmost item (vs. rightmost item in `ArrayStack`)
  - we don't need a dummy node, because we always insert at the front, and thus the insertion code is already simple

## Other Details of Our LLStack Class

```
public class LLStack<T> implements Stack<T> {
    private class Node {
        private T item;
        private Node next;
        ...
    }
    private Node top;
    public LLStack() {
        top = null;
    }
    public boolean isEmpty() {
        return (top == null);
    }
    public boolean isFull() {
        return false;
    }
}
```

- The inner `Node` class uses the type parameter `T` for the item.
- We don't need to preallocate any memory for the items.
- The stack is never full!

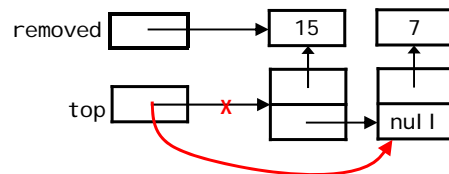
### LLStack.push



```
public boolean push(T item) {

}
```

### LLStack pop() and peek()



```
public T pop() {
    if (isEmpty())
        return null;
    T removed = _____;

}

public T peek() {
    if (isEmpty())
        return null;
    return top.item;
}
```

### toString() Method for the LLStack Class

- Again, assume that we want a string of the form  
"{top, one-below-top, two-below-top, ... bottom}"

```
public String toString() {  
    String str = "{";  
  
    // what should go here?
```

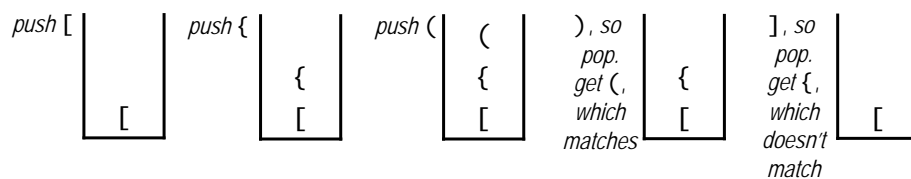
```
        str = str + "}"  
    return str;  
}
```

### Efficiency of the Stack Implementations

	ArrayStack	LLStack
push()	$O(1)$	$O(1)$
pop()	$O(1)$	$O(1)$
peek()	$O(1)$	$O(1)$
space efficiency	$O(m)$ where $m$ is the anticipated maximum number of items	$O(n)$ where $n$ is the number of items currently on the stack

## Applications of Stacks

- The runtime stack in memory
- Converting a recursive algorithm to an iterative one by using a stack to emulate the runtime stack
- Making sure that delimiters (parens, brackets, etc.) are balanced:
  - push open (i.e., left) delimiters onto a stack
  - when you encounter a close (i.e., right) delimiter, pop an item off the stack and see if it matches
  - example:  $5 * [3 + \{ (5 + 16 - 2) ]$



- Evaluating arithmetic expressions (see textbooks)

## An Example of Switching Between Implementations

- In the example code for this unit, there is a test program for each type of sequence:
 

```
Li stTester. j ava, StackTester. j ava, QueueTester. j ava
```
- Each test program uses a variable that has the appropriate *interface* as its type. For example:
 

```
Stack<Stri ng> myStack;
```
- The program asks you which implementation you want to test, and it calls the corresponding constructor:
 

```
if (type == 1)
    myStack = new ArrayStack<Stri ng>(10);
else if (type == 2)
    myStack = new LLStack<Stri ng>();
```
- This is an example of what principle of object-oriented programming?



## Declared Type vs. Actual Type

- An object has two types that may or may not be the same.
  - declared type: type specified when declaring the variable
  - actual type: type specified when creating the object
- Consider again our StackTester program:

```
int type;
Stack<String> myStack;
Scanner in = new Scanner(System.in);
...
type = in.nextInt();
if (type == 1)
    myStack = new ArrayStack<String>(10);
else if (type == 2)
    myStack = new LLStack<String>();
```
- What is the declared type of myStack?
- What is its actual type?

## Dynamic Binding

- Example of how StackTester tests the methods:

```
String item = myStack.pop();
```
- There are two different versions of the pop method, but we don't need two different sets of code to test them.
  - the line shown above will test whichever version of the method the user has specified!
- At runtime, the Java interpreter selects the version of the method that is appropriate to the *actual* type of myStack.
  - This is known as *dynamic binding*.
  - Why can't this selection be done by the compiler?

## Determining if a Method Call is Valid

- The compiler uses the *declared* type of an object to determine if a method call is valid.
- Example:
  - assume that we add our `iterator()` method to `LLList` but do not add a header for it to the `List` interface
  - under that scenario, the following will *not* work:  

```
List myList = new LList();  
ListIterator iter = myList.iterator();
```
- Because the declared type of `myList` is `List`, the compiler looks for that method in `List`.
  - if it's not there, the compiler will not compile the code.
- We can use a type cast to reassure the compiler:  

```
ListIterator iter = ((LLList)myList).iterator();
```

## Queue ADT



- A queue is a sequence in which:
  - items are added at the rear and removed from the front
    - first in, first out (FIFO) (vs. a stack, which is last in, first out)
  - you can only access the item that is currently at the front
- Operations:
  - insert: add an item at the rear of the queue
  - remove: remove the item at the front of the queue
  - peek: get the item at the front of the queue, but don't remove it
  - isEmpty: test if the queue is empty
  - isFull: test if the queue is full
- Example: a queue of integers  
*start:* 12 8  
*insert 5:* 12 8 5  
*remove:* 8 5

## Our Generic Queue Interface

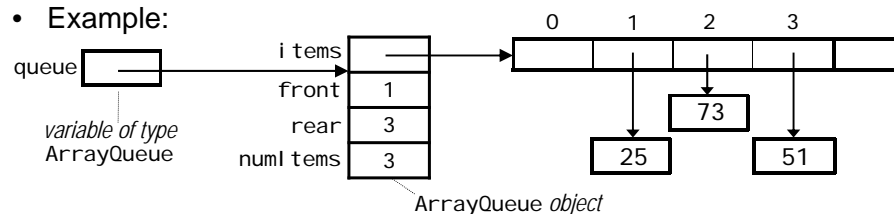
```
public interface Queue<T> {  
    boolean insert(T item);  
    T remove();  
    T peek();  
    boolean isEmpty();  
    boolean isFull();  
}
```

- `insert()` returns `false` if the queue is full, and `true` otherwise.
- `remove()` and `peek()` take no arguments, because we know that we always access the item at the front of the queue.
  - return `null` if the queue is empty.
- Here again, we will use encapsulation to ensure that the data structure is manipulated only in valid ways.

## Implementing a Queue Using an Array

```
public class ArrayQueue<T> implements Queue<T> {  
    private T[] items;  
    private int front;  
    private int rear;  
    private int numItems;  
    ...  
}
```

- Example:



- We maintain two indices:
  - `front`: the index of the item at the front of the queue
  - `rear`: the index of the item at the rear of the queue

## Avoiding the Need to Shift Items

- Problem: what do we do when we reach the end of the array?

*example: a queue of integers:*

front								rear	
54	4	21	17	89	65				

*the same queue after removing two items and inserting one:*

front								rear	
		21	17	89	65	43			

*to insert two or more additional items, would need to shift items left*

- Solution: maintain a *circular queue*. When we reach the end of the array, we wrap around to the beginning.

*the same queue after inserting two additional items:*

rear								front	
5			21	17	89	65	43		81

## A Circular Queue

- To get the front and rear indices to wrap around, we use the modulus operator (%).
- $x \% y$  = the remainder produced when you divide  $x$  by  $y$ 
  - examples:
    - $10 \% 7 = 3$
    - $36 \% 5 = 1$
- Whenever we increment front or rear, we do so modulo the length of the array.

$\text{front} = (\text{front} + 1) \% \text{items.length};$

$\text{rear} = (\text{rear} + 1) \% \text{items.length};$

- Example:

front								rear	
		21	17	89	65	43	81		

$\text{items.length} = 8, \text{rear} = 7$

before inserting the next item:  $\text{rear} = (7 + 1) \% 8 = 0$

which wraps rear around to the start of the array

## Testing if an ArrayQueue is Empty

- Initial configuration: rear front  
 rear = -1  
 front = 0  

--	--	--	--	--	--	--	--
- We increment rear on every insertion, and we increment front on every removal.  
 after one insertion: rear front  

15							
----	--	--	--	--	--	--	--
- after two insertions: front rear  

15	32						
----	----	--	--	--	--	--	--
- after one removal: front rear  

	32						
--	----	--	--	--	--	--	--
- after two removals: rear front  

--	--	--	--	--	--	--	--
- The queue is empty when rear is one position “behind” front:  
 $((\text{rear} + 1) \% \text{items.length}) == \text{front}$

## Testing if an ArrayQueue is Full

- Problem: if we use all of the positions in the array, our test for an empty queue will also hold when the queue is full!  
*example: what if we added one more item to this queue?*

rear		front					
5		21	17	89	65	43	81

- This is why we maintain numItems!

```

public boolean isEmpty() {
    return (numItems == 0);
}

public boolean isFull() {
    return (numItems == items.length);
}

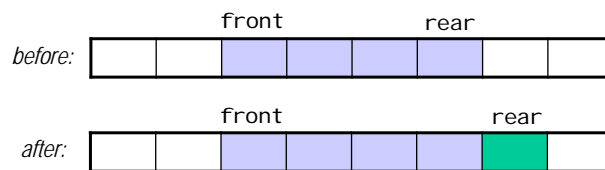
```

## Constructor

```
public ArrayQueue(int maxSize) {  
    items = (T[])new Object[maxSize];  
    front = 0;  
    rear = -1;  
    numItems = 0;  
}
```

## Inserting an Item in an ArrayQueue

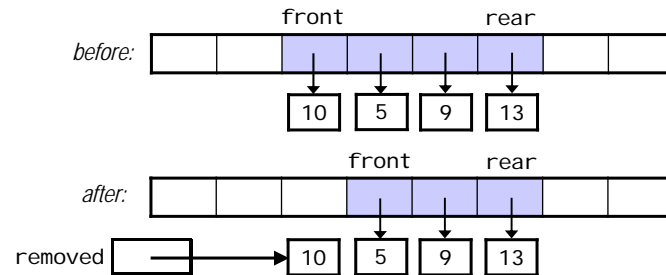
- We increment rear before adding the item:



```
public boolean insert(T item) {  
    if (isFull())  
        return false;  
    rear = (rear + 1) % items.length;  
    items[rear] = item;  
    numItems++;  
    return true;  
}
```

## ArrayQueue remove()

- remove: need to get `items[front]` *before* we increment front.

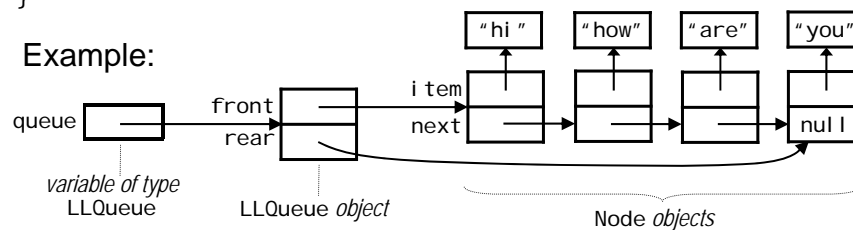


```
public T remove() {
    if (isEmpty())
        return null;
    T removed = items[front];
    items[front] = null;
    front = (front + 1) % items.length;
    numItems--;
    return removed;
}
```

## Implementing a Queue Using a Linked List

```
public class LLQueue<T> implements Queue<T> {
    private Node front;    // front of the queue
    private Node rear;     // rear of the queue
    ...
}
```

- Example:



- Because a linked list can be easily modified on both ends, we don't need to take special measures to avoid shifting items, as we did in our array-based implementation.

## Other Details of Our LLQueue Class

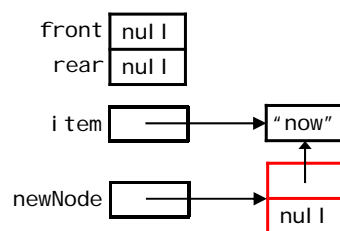
```
public class LLQueue<T> implements Queue<T> {
    private class Node {
        private T item;
        private Node next;
        ...
    }

    private Node front;
    private Node rear;

    public LLQueue() {
        front = rear = null;
    }
    public boolean isEmpty() {
        return (front == null);
    }
    public boolean isFull() {
        return false;
    }
    ...
}
```

- Much simpler than the array-based queue!

## Inserting an Item in an Empty LLQueue



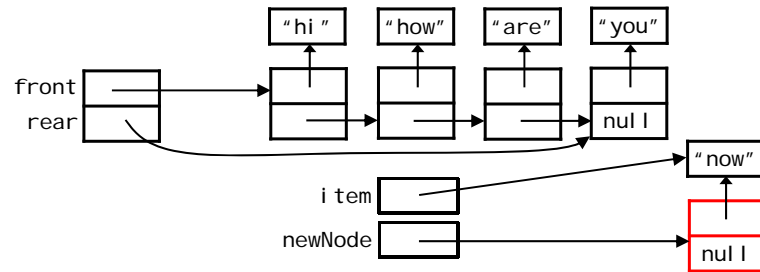
*The next field in the newNode will be null in either case. Why?*

```
public boolean insert(T item) {
    Node newNode = new Node(item, null);
    if (isEmpty())
    else {

    }
    return true;
}
```



## Inserting an Item in a Non-Empty LLQueue

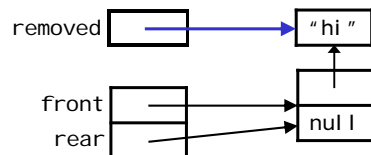


```
public boolean insert(T item) {
    Node newNode = new Node(item, null);
    if (isEmpty())

    else {

    }
    return true;
}
```

## Removing from an LLQueue with One Item



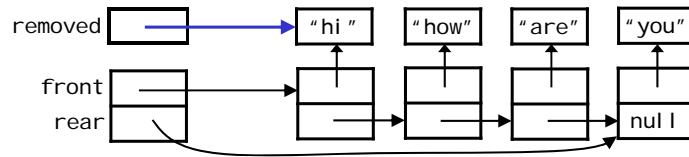
```
public T remove() {
    if (isEmpty())
        return null;

    T removed = _____;
    if (front == rear) // removing the only item

    else

    return removed;
}
```

## Removing from an LLQueue with Two or More Items



```
public T remove() {
    if (isEmpty())
        return null;

    T removed = _____;
    if (front == rear)    // removing the only item

    else

    return removed;
}
```

## Efficiency of the Queue Implementations

	ArrayQueue	LLQueue
insert()	$O(1)$	$O(1)$
remove()	$O(1)$	$O(1)$
peek()	$O(1)$	$O(1)$
space efficiency	$O(m)$ where $m$ is the anticipated maximum number of items	$O(n)$ where $n$ is the number of items currently in the queue

## Applications of Queues

- first-in first-out (FIFO) inventory control
- OS scheduling: processes, print jobs, packets, etc.
- simulations of banks, supermarkets, airports, etc.
- breadth-first traversal of a graph or level-order traversal of a binary tree (more on these later)

## Lists, Stacks, and Queues in Java's Class Library

- Lists:
  - interface: `java.util.List<T>`
    - slightly different methods, some extra ones
  - array-based implementations: `java.util.ArrayList<T>`  
`java.util.Vector<T>`
    - the array is expanded as needed
    - `Vector` has extra non-`List` methods
  - linked-list implementation: `java.util.LinkedList<T>`
    - `addLast()` provides  $O(1)$  insertion at the end of the list
- Stacks: `java.util.Stack<T>`
  - extends `Vector` with methods that treat a vector like a stack
  - problem: other `Vector` methods can access items below the top
- Queues:
  - interface: `java.util.Queue<T>`
  - implementation: `java.util.LinkedList<T>`.