

1 Recursion

1.1 DFS

```
1 Function dfs(G,u)
   color(u) = gray
3   for each (u,v) ∈ G and color(v) = white do
       dfs(G,v)
5   color(u) = black
```

```
1 void dfs(int node){
   strcpy(graph[node-1].color , "gray");
3   aux++;
   graph[node-1].dfs = aux;
5   int i;
   for(i = 0; i < graph[node-1].n_edges; i++){
7       if(strcmp(graph[graph[node-1].edges[i]-1].color , "white") == 0){
           dfs(graph[node-1].edges[i]);
9       }
       aux--;
   }
11 }
   strcpy(graph[node-1].color , "black");
13 }
```

2 Backtracking

2.1 Template

```
1 Function BT(s)
   if reject(s) = true then
3       return false
   if accept(s) = true then
5       output(s)
       return true
7   while condition(s) = true do
       s' = update(s)
9       if BT(s') = true then
           return true
11  return false
```

2.2 8 Queens

```
1 Function nQueens(col)
   if col = N + 1 then
3       return true
   for i = 1 to N do
```

```

5   Q[col] = i
   if attack(col) = false then
7       if nQueens(col + 1) = true then
           return true
9   return false

```

2.3 Hamiltonian path

```

1 Function HamPath(v)
   if v = t then
3       if sum(visit) = N then
           return true
5       else
           return false
7   for (v, i) ∈ G do
       if visit[i] = 0 then
9           visit[i] = 1
           if HamPath(i) = true then
11              return true
           visit[i] = 0
13   return false

```

2.4 Hamiltonian cycle

```

1 Function HamCycle(v)
   if sum(visit) = N then
3       if (v, 1) ∈ G then
           return true
5   for (v, i) ∈ G do
       if visit[i] = 0 then
7           visit[i] = 1
           if HamCycle(i) = true then
9               return true
           visit[i] = 0
11   return false

```

2.5 Graph coloring

```

1 Function gcp(v)
   if v = N + 1 then
3       return true
   for i = 1 to K do
5       feasible = true
       for (v, j) ∈ G do
7           if color[j] = i then
               feasible = false

```

```

9      break
    if feasible = true then
11      color[v] = i
      if gcp(v + 1) = true then
13          return true
      color[v] = 0
15 return false

```

2.6 Shortest Hamiltonian path

```

1 Function ShortPath(v, len)
  if len >= best then
3      return
  if sum(visit) = N and len < best then
5      best = len
      return
7  for (v, i) ∈ G do
    if visit[i] = 0 then
9        visit[i] = 1
        ShortPath(i, len + M[v][i])
11       visit[i] = 0

```

3 Dynamic Programming

3.1 Longest Increasing Subsequence - Top-down

```

1 Function lis(S, i)
  if LIS[i] is cached then
3      return LIS[i]
  if i = 1 then
5      LIS[i] = 1
  else
7      LIS[i] = 0
  for j = 1 to i - 1 do
9      LIS[j] = lis(S, j)
      if S[j] < S[i] and LIS[j] > LIS[i] then
11         LIS[i] = LIS[j]
  LIS[i] = LIS[i] + 1
13 return LIS[i]

```

3.2 Longest Increasing Subsequence - Bottom-up

```

1 Function lis(S)
  LIS[1] = 1
3  for i = 2 to n do

```

```

    LIS[i] = 0
5   for j = 1 to i - 1 do
        if S[j] < S[i] and LIS[j] > LIS[i] then
7       LIS[i] = LIS[j]
    LIS[i] = LIS[i] + 1
9   return max(LIS[1], ..., LIS[n])

```

3.3 Longest Common Subsequence - Top-down

```

1 Function lcs(A[1..i], B[1..j])
    if LCS[i, j] is cached then
3     return LCS[i, j]
    if i = 0 or j = 0 then
5     LCS[i, j] = 0
    return LCS[i, j]
7   if A[i] = B[j] then
        LCS[i, j] = lcs(A[1..i - 1], B[1..j - 1]) + 1
9   else
        LCS1 = lcs(A[1..i - 1], B[1..j])
11        LCS2 = lcs(A[1..i], B[1..j - 1])
        LCS[i, j] = max(LCS1, LCS2)
13   return LCS[i, j]

```

3.4 Longest Common Subsequence - Bottom-up

```

1 Function lcs(A, B)
    for i = 0 to n do
3     LCS[i, 0] = 0
    for j = 0 to m do
5     LCS[0, j] = 0
    for i = 1 to n do
7     for j = 1 to m do
        if A[i] = B[j] then
9         LCS[i, j] = LCS[i - 1, j - 1] + 1
        else
11        LCS[i, j] = max(LCS[i - 1, j], LCS[i, j - 1])
    return LCS[n, m]

```

3.5 Number of monotonic paths - Top-down

```

Function count(x, y)
2   if T[x, y] is cached then
        return T[x, y]
4   if x = 1 or y = 1 then
        return 1
6   C1 = count(x - 1, y)

```

```

C2 = count (x, y - 1)
8  T[x, y] = C1 + C2
   return T[x, y]

```

3.6 Number of monotonic paths - Bottom-up

```

1  Function count(n, m)
   for i = 1 to n do
3   T[i, 1] = 1
   for j = 1 to m do
5   T[1, j] = 1
   for i = 2 to n do
7   for j = 2 to m do
       T[i, j] = T[i - 1, j] + T[i, j - 1])
9   return T[n, m]

```

3.7 Coin Changing - Top-down

```

1  Function change(i, C)
   if C < 0 or i = 0 then
3   return ∞
   if C = 0 then
5   return 0
   if T[i, C] > 0 then
7   return T[i, C]
   if di > C then
9   T[i, C] = change (i - 1, C )
   else
11  T[i, C] = min(change(i - 1, C), 1 + change(i, C - di))
   return T[i, C]

```

3.8 Coin Changing - Bottom-up

```

Function change(n, C)
2  for i = 0 to n do
   T[i, 0] = 0
4  for j = 0 to C do
   T[0, j] = ∞
6  for i = 1 to n do
   for j = 1 to C do
8   if di > j then
       T[i, j] = T[i - 1, j]
10  else
       T[i, j] = min(T[i - 1, j], 1 + T[i, j - di])
12  return T[n, C]

```

3.9 Subset Sum - Top-down

```
Function subset(i, C)
2  if C = 0 then
    return true
4  if i = 0 and C ≠ 0 then
    return false
6  if T[i, C] is not empty then
    return T[i, C]
8  if  $d_i > C$  then
    T[i, C] = subset(i - 1, C)
10 else
    T[i, C] = subset(i - 1, C) ∨ subset(i - 1, C -  $d_i$ )
12 return T[i, C]
```

3.10 Subset Sum - Bottom-up

```
Function subset(n, C)
2  for i = 0 to n do
    T[i, 0] = true
4  for j = 1 to C do
    T[0, j] = false
6  for i = 1 to n do
    for j = 1 to C do
8      if  $d_i > j$  then
        T[i, j] = T[i - 1, j]
10     else
        T[i, j] = T[i - 1, j] ∨ T[i - 1, j -  $d_i$ ]
12 return T[n, C]
```

3.11 Knapsack - Top-down

```
Function knapsack(i, W)
2  if i = 0 then
    return 0
4  if T[i, W] >= 0 then
    return T[i, W]
6  if  $w_i > W$  then
    T[i, W] = knapsack(i - 1, W)
8  else
    T[i, W] = max(knapsack(i - 1, W),  $v_i$  + knapsack(i - 1, W -  $w_i$ ))
10 return T[i, W]
```

3.12 Knapsack - Bottom-up

```

Function knapsack(n, W)
2   for j = 1 to W do
    T[0, j] = 0
4   for i = 0 to n do
    T[i, 0] = 0
6   for i = 1 to n do
    for j = 1 to W do
8      if  $w_i > j$  then
        T[i, j] = T[i - 1, j]
10     else
        T[i, j] = max(T[i - 1, j],  $v_i + T[i - 1, j - w_i]$ )
12   return T[n, W]

```

3.13 Matrix-chain multiplication - Top-down

```

Function mult(i, j)
2   if j <= i then
    return 0
4   if M[i, j] >= 0 then
    return M[i, j]
6   cost =  $\infty$ 
   for k = i to j - 1 do
8     cost = min(cost, mult(i, k) + mult(k + 1, j) +  $p_{i-1} p_k p_j$ )
    M[i, j] = cost
10  return cost

```

3.14 Matrix-chain multiplication - Bottom-up

```

Function mc(n)
2   for d = 2 to n do
    for i = 1 to n - d + 1 do
4      j = i + d - 1
      M[i, j] =  $\infty$ 
6      for k = i to j - 1 do
        M[i, j] = min(M[i, j], M[i, k] + M[k + 1, j] +  $p_{i-1} p_k p_j$ )
8   return m[1][n]

```

4 Mooshak Problems

4.1 Radical Winter Games

```

def read_input():
2   tests = []
   n_tests = input()

```

```

4     for i in range(n_tests):
5         n_lines = input()
6         test = []
7         for j in range(n_lines):
8             line = raw_input()
9             l = map(int, line.split(" "))
10            test.append(l)
11            tests.append(test)
12    return tests

14 def calc_scores(tests):
15     j=1
16     for i in range(len(tests)):
17         tests[i][1][0] += tests[i][0][0]
18         tests[i][1][1] += tests[i][0][0]
19         for j in range(2, len(tests[i])):
20             for k in range(len(tests[i][j])):
21                 if k==0:
22                     tests[i][j][k] += tests[i][j-1][k]
23                 elif k==(len(tests[i][j])-1):
24                     tests[i][j][k] += tests[i][j-1][k-1]
25                 else:
26                     tests[i][j][k] = max(tests[i][j][k] + tests[i][j-1][k-1],
27 tests[i][j][k] + tests[i][j-1][k])
28             print max(tests[i][j])

29 if __name__ == '__main__':
30     tests = read_input()
31     calc_scores(tests)

```

4.2 Train Sorting

```

1 #include <stdio.h>
2 #include <stdlib.h>
3
4 int main() {
5     int n, i, j, k, l, size_train, max;
6     unsigned int cars[5001];
7     int aux[5001];
8     scanf("%d", &n);
9     for (i=0; i<n; i++){
10         scanf("%d", &cars[i]);
11     }
12     aux[0] = 1;
13     for (j=1; j<n; j++){
14         size_train = 0;
15         for (k=j-1; k>=0; k--){
16             if (cars[j] > cars[k] && size_train < aux[k]){
17                 size_train = aux[k];
18             }
19         }
20     }
21 }

```



```

19     }
    aux[j] = ++size_train;
21 }
max = 0;
23 for (l=0;l<n;l++){
    if (aux[l] > max){
25         max = aux[l];
    }
27 }
printf("%d\n",max);
29 return 0;
}

```

4.3 Dividing Coins

```

#include <stdio.h>
2 #include <stdlib.h>
#include <vector>
4 #include <string.h>

6 using namespace std;

8 int sum = 0;
vector<int> coins;
10
int knapsack(int n, int w){
12     int table[n+1][w+1];
    for(int j = 1; j <= w; j++){
14         table[0][j] = 0;
    }
16     for(int i = 0; i <= n; i++){
        table[i][0] = 0;
18     }
    for(int i = 1; i <= n; i++){
20         for(int j = 1; j <= w; j++){
            if(coins[i] > j){
22                 table[i][j] = table[i-1][j];
            } else {
24                 table[i][j] = max(table[i-1][j], coins[i] + table[i-1][j-coins[i]]);
            }
26         }
    }
28     return table[n][w];
}

30
int main(){
32     int n_problems, n_coins, aux = 0;
    scanf("%d", &n_problems);
34     for(int i = 0; i < n_problems; i++){
        sum = 0;

```

```

36     coins.clear();
    scanf("%d", &n_coins);
38     for(int j = 0; j < n_coins; j++){
        scanf("%d", &aux);
40         coins.push_back(aux);
        sum += aux;
42     }
    printf("%d\n", sum - 2*knapsack(n_coins, (int)sum/2));
44 }
}

```

4.4 Two Towers

```

1  #include <stdio.h>
   #include <stdlib.h>
3  #include <vector>
   #include <string.h>
5
   using namespace std;
7
   vector<int> tiles_tower_1;
9   vector<int> tiles_tower_2;

11  int lcs(int n1, int n2){
    int table[n1+1][n2+1];
13     for(int i = 0; i <= n1; i++){
        table[i][0] = 0;
15     }
    for(int j = 0; j <= n2; j++){
17         table[0][j] = 0;
19     }
    for(int i = 1; i <= n1; i++){
21         for(int j = 1; j <= n2; j++){
23             if(tiles_tower_1[i-1] == tiles_tower_2[j-1]){
                table[i][j] = table[i-1][j-1] + 1;
25             }else {
                table[i][j] = max(table[i-1][j], table[i][j-1]);
27             }
            }
29     }
    return table[n1][n2];
31 }

33 int main(){
    int n1, n2, aux, k = 0;
35     while(scanf("%d %d", &n1, &n2) == 2){
        if(n1 == 0 && n2 == 0){
37             return 0;

```

```

    }
39    k++;
    tiles_tower_2.clear();
41    tiles_tower_1.clear();
    for(int i = 0; i < n1; i++){
43        scanf("%d", &aux);
        tiles_tower_1.push_back(aux);
45    }
    for(int i = 0; i < n2; i++){
47        scanf("%d", &aux);
        tiles_tower_2.push_back(aux);
49    }
    int result = lcs(n1, n2);
51    printf("Twin Towers #%d\n", k);
    printf("Number of Tiles : %d\n\n", result);
53 }
    return 0;
55 }

```

4.5 Little Red Riding Hood

```

1  #include <stdio.h>
   #include <stdlib.h>
3  #include <vector>
   #include <string.h>
5
   using namespace std;
7
   unsigned long wolves[101][101];
9   unsigned long grid[101][101];
11
   unsigned long count(unsigned long w, unsigned long h){
       unsigned long table[w+1][h+1];
13
       for(unsigned long i = 0; i < w; i++){
15           table[i][0] = 1;
       }
17
       for(unsigned long j = 0; j < h; j++){
19           table[0][j] = 1;
       }
21
       for(unsigned long i=0; i < w; i++){
23           for(unsigned long j=0; j < h; j++){
               if(wolves[i][j] == 1){
25                 table[i][j] = 0;
               } else {
27                 if(j==0 && i==0){
                     table[i][j] = 1;
29                 } else if(i==0){

```

```

31         table[i][j] = table[i][j-1];
32     }else if(j==0){
33         table[i][j] = table[i-1][j];
34     } else{
35         table[i][j] = table[i-1][j] + table[i][j-1];
36     }
37 }
38 }
39 return table[w-1][h-1];
40 }
41
42 int main(){
43     unsigned long w, h, n_wolves, wolf_w, wolf_h, result = 0;
44
45     while(scanf("%ld %ld", &w, &h) == 2 && (w || h)){
46         for(unsigned long i = 0; i < w; i++){
47             for(unsigned long j = 0; j < h; j++){
48                 wolves[i][j] = 0;
49                 grid[i][j] = 0;
50             }
51         }
52         scanf("%ld", &n_wolves);
53         for(unsigned long i = 0; i < n_wolves; i++){
54             scanf("%ld %ld", &wolf_w, &wolf_h);
55             wolves[wolf_w][wolf_h] = 1; // posicoes onde estao lobos
56         }
57         w++;
58         h++;
59         result = count(w,h);
60         if(result == 0){
61             printf("There is no path.\n");
62         }else if(result == 1){
63             printf("There is one path from Little Red Riding Hood's house to her
64 grandmother's house.\n");
65         } else {
66             printf("There are %lu paths from Little Red Riding Hood's house to her
67 grandmother's house.\n", result);
68         }
69     }
70     return 0;
71 }

```

4.6 The Trip of Mr. Rowan

```

1 #include <stdio.h>
2 #include <stdlib.h>
3 #include <vector>
4 #include <string.h>
5 #include <math.h>

```

```

7 using namespace std;

9 int visited_nodes[12];
  int nodes[12][2];
11 int number_of_nodes;

13 double best;

15 void solve(int i, double distance){

17     int number_visited_nodes = 0;

19     double calc = 0;
    if(distance == 0)
21         visited_nodes[i] = 1;

23     for(int j = 0; j < number_of_nodes; j++){
        if(visited_nodes[j] == 0){
25             visited_nodes[j] = 1;
            calc = sqrt(pow((nodes[j][0] - nodes[i][0]),2) + pow((nodes[j][1] -
nodes[i][1]),2));
27             distance += calc;
            if(distance <= best){
29                 solve(j, distance);
            }
31             distance -= calc;
            visited_nodes[j] = 0;
33         } else {
            number_visited_nodes++;
35         }
    }
37     if(number_visited_nodes == number_of_nodes){
        if(best == 0){
39             best = distance;
        }
41         else if(distance < best){
            best= distance;
43         }
    }
45     return;
}

47 int main(){
49     int a, b = 0;
    best = 100000;
51     memset(visited_nodes,0,sizeof(visited_nodes));

53     scanf("%d", &number_of_nodes);
    for(int i = 0; i < number_of_nodes; i++){
55         scanf("%d %d", &a, &b);

```

```

57     nodes[i][0] = a;
    nodes[i][1] = b;
59 }
61 for(int i = 1; i < number_of_nodes; i++){
    visited_nodes[i-1] = 0;
    solve(i, 0);
63 }
    printf("%.3f\n", best);
65 return 0;
}

```

4.7 Delicious Pasta

```

#include <stdio.h>
2 #include <stdlib.h>
#include <vector>
4 #include <string.h>
#include <math.h>
6
using namespace std;
8
int id, number_of_pastas, budget, cooking_time, taste_value = 0;
10 int pastas[5000][2];
12 double get_max_taste(){
    double cache[number_of_pastas+1][budget+1];
14     int i,j,b;
16     for(j = 0; j <= budget; j++){
        cache[0][j] = 0;
18     }
20     for(j = 0; j <= number_of_pastas; j++){
        cache[j][0] = 0;
22     }
24     for(i = 1; i <= number_of_pastas; i++){
        for(j = 1; j <= budget; j++){
26             int inspetormax= 0;
            for(b = 1; b <= j; b++){
28                 inspetormax = max(cache[i-1][j], pastas[budget*(i-1) + b - 1][1] +
                cache[i-1][j-b]);
                if(inspetormax > cache[i][j]){
30                     cache[i][j] = inspetormax;
                }
            }
32         }
    }
34 }
return cache[number_of_pastas][budget];

```

```

36 }
38 int main() {
39     int result = 0;
40
41     scanf("%d %d", &number_of_pastas, &budget);
42     for(int i = 0; i < number_of_pastas; i++){
43         for(int j = 0; j < budget; j++){
44             scanf("%d %d %d", &id, &cooking_time, &taste_value);
45             pastas[budget*i + j*budget][0] = cooking_time;
46             pastas[budget*i + j*budget][1] = taste_value;
47         }
48     }
49     result = get_max_taste();
50     printf("%d\n", result);
51     return 0;
52 }

```

5 C++ Reference

5.1 vector

```
#include <vector>
```

- begin() - Return iterator to beginning
- end() - Return iterator to end
- size() - Return size
- empty() - Test whether vector is empty
- push_back(element) - Add element at the end
- pop_back() - Delete last element
- insert(position, val); - Insert elements
- erase(position) | erase(first, last) - Erase elements

5.2 qsort

```

1 void qsort(void* base, size_t num, size_t size, int (*compar)(const void*,
    const void*));

```

- base - Pointer to the first object of the array to be sorted, converted to a void*
- num - Number of elements in the array pointed to by base.
- size - Size in bytes of each element in the array.
- compar - Pointer to a function that compares two elements:
(return value - meaning)
- <0 - The element pointed to by p1 goes before the element pointed to by p2

0 - The element pointed to by p1 is equivalent to the element pointed to by p2

>0 - The element pointed to by p1 goes after the element pointed to by p2

Exemplo compare:

```
1 int compareMyType(const void * a, const void * b){
    if ( *(MyType*)a < *(MyType*)b ) return -1;
3   if ( *(MyType*)a == *(MyType*)b ) return 0;
    if ( *(MyType*)a > *(MyType*)b ) return 1;
5 }
```

Exemplo de uso:

```
1 #include <stdio.h>          /* printf */
   #include <stdlib.h>        /* qsort */
3 int values[] = { 40, 10, 100, 90, 20, 25 };
   int compare(const void * a, const void * b){
5     return( *(int*)a - *(int*)b );
   }
7 int main(){
    int n;
9     qsort(values, 6, sizeof(int), compare);
    for (n=0; n<6; n++)
11         printf("%d ", values[n]);
    return 0;
13 }
```