Assignment 1

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Contents

1	•	Generate 100 random from a Bivariate Generalized exponential, Bivariate Weibull ribution.	1
	1.1	Bivariate Generalized Exponential Distribution	1
	1.2	Bivariate Weibull Distribution	3
2	•	Generate 100 random from an absolutely continuous bivariate Generalized expotial, absolutely continuous Bivariate Weibull distribution.	6
	2.1	Absolutely Continuous Bivariate Generalized Exponential Distribution	6
	2.2	Absolutely Continuous Bivariate Weibull Distribution	8
1	•	1. Generate 100 random from a Bivariate Generalized experience.	0-

1.1 Bivariate Generalized Exponential Distribution

To calculate BVGE we will first generate a GE using genExp.

```
genExp<-function(alpha, lambda){
   (-(1/lambda) * log(1 - (runif(1)^(1/alpha))))
}</pre>
```

Lets generate 100 BVGE with parameters $(\lambda, \alpha_1, \alpha_2, \alpha_3) = (0.04, 1, 2, 0.5)$.

```
N = 100
X = matrix(NA, N, 2)

i = 1
while(i <= N) {
    u_0 = genExp(alpha[1], lambda)
    u_1 = genExp(alpha[2], lambda)
    u_2 = genExp(alpha[3], lambda)
    X[i,] = c(max(u_0, u_1), max(u_0, u_2))
    i = i + 1
}</pre>
X
```

```
## [,1] [,2]
## [1,] 75.261737 75.261737
```

```
##
     [2,]
           34.759710
                        6.098882
##
     [3,]
           34.447019
                       32.528619
##
     [4,]
           64.898659
                       64.898659
           27.775730
##
     [5,]
                       27.775730
##
     [6,]
           50.683957
                       21.630647
##
     [7,]
           54.628470
                       38.591701
##
     [8,]
           14.979264
                        9.833217
     [9,]
           90.118060
                       77.757317
##
##
    [10,]
           19.079674
                       30.983857
##
    [11,]
           63.397236
                       63.397236
    [12,]
           15.950122
                       49.931611
    [13,]
           24.008456
                       25.991248
##
           28.110829
##
    [14,]
                       28.110829
##
    [15,]
           25.804315
                       25.804315
##
    [16,]
           39.543601
                       10.942091
##
    [17,]
           73.469483
                       31.721465
##
    [18,]
           62.327929
                        4.644148
    [19,] 162.564042 162.564042
    [20,]
           35.761495
                     13.709846
##
##
    [21,]
           56.688396
                       32.608536
##
    [22,]
           51.186353
                       51.186353
##
    [23,]
           55.760596
                       16.083679
##
    [24,]
           33.504431
                       12.006770
    [25,]
           78.650709
                       10.554889
##
##
    [26,]
           17.150956
                        1.096294
    [27,]
           17.742161
                      11.468341
##
    [28,]
           55.740694
                       8.265121
    [29,]
           57.529683
##
                       57.529683
##
    [30,]
           14.570845
                       7.349198
##
    [31,]
           31.566062
                       31.566062
##
    [32,]
           41.792008
                       38.853224
##
    [33,]
           86.835936
                       86.835936
##
    [34,]
           28.537797
                       12.505912
    [35,]
           35.037567
##
                       35.037567
##
    [36,]
           22.311876
                       16.492583
##
    [37,]
           46.937160
                       3.202666
##
    [38,]
          59.159236 59.159236
##
    [39,] 118.745760 118.745760
##
    [40,] 111.030808
                       20.949105
                       31.260178
##
    [41,] 21.825781
    [42,]
            4.048259
                       6.246982
##
    [43,]
           39.492960
                       33.199246
    [44,]
           74.095366
##
                       65.084759
##
    [45,]
           57.210030
                       10.659956
    [46,]
           38.778431
##
                       85.151922
    [47,]
##
           37.299565
                       34.055943
##
    [48,]
           15.915295
                      15.915295
##
    [49,]
           84.209227 110.110286
##
    [50,]
           63.829005
                     78.975819
##
    [51,]
           35.617427
                       26.045818
##
    [52,] 118.456288 118.456288
##
    [53,] 19.232761 14.075188
##
    [54,] 113.841665 22.785290
##
    [55,] 52.906304 52.906304
```

```
##
    [56,]
           35.618309
                        35.618309
##
                         6.554898
    [57,]
           66.234375
##
    [58,]
           98.226465
                        24.742346
    [59,]
           33.740954
                        24.458537
##
    [60,]
##
           53.873053
                        35.063658
##
    [61,]
           68.703923
                        65.762914
##
    [62,]
           59.931626
                        59.931626
    [63,]
##
           73.134967
                        73.134967
##
    [64,] 140.332882 100.529219
##
    [65,]
           22.313461
                        22.313461
##
    [66,]
           22.676364
                         6.050316
    [67,]
           24.297769
##
                        15.765221
##
    [68,]
           59.360843
                         3.167281
##
    [69,]
            48.951912
                        15.958934
##
    [70,]
            46.253468
                        46.253468
##
    [71,] 102.306235 102.306235
                        78.557227
##
    [72,]
           78.557227
##
    [73,]
           80.488762
                         7.191763
    [74,]
           50.528666
##
                        40.838360
##
    [75,]
           19.208921
                         4.793367
##
    [76,]
           45.512643
                        24.118033
##
    [77,]
            40.160985
                        44.105826
##
    [78,]
             6.747788
                        34.156489
    [79,]
           21.394085
##
                         9.519606
##
    [80,]
           28.194290
                        12.194475
##
    [81,]
           51.457120
                        30.236116
##
            18.153108
    [82,]
                         8.887474
##
    [83,]
           63.561831
                        20.690250
            16.553138
##
    [84,]
                        25.129956
##
    [85,]
            32.605282
                        21.478017
##
    [86,]
            28.294441
                        51.207744
##
    [87,]
           56.711544
                        56.711544
##
    [88,]
            43.449519
                        43.449519
           88.799347
##
    [89,]
                        88.799347
##
    [90,]
           59.650016
                        59.650016
##
    [91,] 123.287831
                         7.741560
##
    [92,]
            46.592821
                        26.131382
##
    [93,]
           33.298807
                         3.546861
##
    [94,]
           14.154009
                        13.534068
##
    [95,]
           63.373995
                         3.029261
           26.809435
##
    [96,]
                        10.360186
##
    [97,]
           25.843980
                        25.843980
##
    [98,]
           37.770178
                        37.770178
##
    [99,]
           98.622653
                        98.622653
## [100,]
           43.721012
                         9.312461
```

1.2 Bivariate Weibull Distribution

To calculate BW we will first generate a Weibull using genWeibull.

```
genWeibull<-function(lambda, alpha){
  (((-log(1 - (runif(1)^(1/lambda))))^(1/alpha)))
}</pre>
```

Lets generate 100 BW with parameters $(\alpha, \lambda_1, \lambda_2, \lambda_3) = (2, 0.5, 1, 2)$.

```
N = 100
X = matrix(NA, N, 2)

i = 1
while(i <= N) {
    u_0 = genWeibull(lambda[1], alpha)
    u_1 = genWeibull(lambda[2], alpha)
    u_2 = genWeibull(lambda[3], alpha)
    X[i,] = c(max(u_0, u_1), max(u_0, u_2))
    i = i + 1
}</pre>
X
```

```
##
               [,1]
                         [,2]
     [1,] 0.2750139 1.0757377
##
     [2,] 1.2404192 0.9692566
##
##
     [3,] 0.3302639 0.8245903
     [4,] 1.8409034 1.8409034
##
##
     [5,] 1.2205111 0.7156043
##
     [6,] 0.7283177 0.8833713
     [7,] 2.8365415 2.8365415
##
##
     [8,] 1.8767641 1.0506367
##
     [9,] 2.3479123 1.2585923
##
    [10,] 0.9241678 0.9931425
##
    [11,] 1.2550641 1.3939921
   [12,] 2.1455687 2.1455687
##
   [13,] 1.4353385 0.9175502
   [14,] 0.8766751 0.8766751
##
    [15,] 0.5132323 1.5996778
##
##
   [16,] 1.2987772 0.4906242
   [17,] 0.6135403 1.4417312
   [18,] 2.1917424 2.1917424
##
##
   [19,] 1.4974836 1.4974836
   [20,] 0.6297661 1.1164879
##
   [21,] 0.5751490 1.1134314
   [22,] 0.8858369 0.7415648
##
##
   [23,] 0.7292640 0.9160692
##
   [24,] 1.6022287 1.2068723
   [25,] 1.4624313 1.3290872
   [26,] 1.1950642 1.1454899
##
##
   [27,] 0.7423398 1.1684946
   [28,] 1.3899244 1.5927890
   [29,] 0.8746791 1.3839697
   [30,] 0.5071619 1.0712178
##
   [31,] 0.5690653 0.9335970
   [32,] 1.2682233 1.2682233
  [33,] 0.5681257 1.2983655
##
##
   [34,] 1.3445021 1.4923192
## [35,] 1.1350971 1.7026982
## [36,] 1.5171384 1.1341920
  [37,] 0.9893825 1.8695618
```

```
[38,] 1.2505853 1.2505853
    [39,] 0.6629872 1.6698280
    [40,] 1.5384679 0.7153568
   [41,] 0.7501651 2.1393896
    [42,] 0.6209266 1.7991533
##
   [43,] 1.1951675 1.1951675
    [44,] 1.0661876 1.2046914
   [45,] 1.5506575 1.0981689
##
    [46,] 0.6979713 0.7787587
##
    [47,] 0.8374978 1.1182699
   [48,] 1.3201983 1.3201983
##
   [49,] 0.6538431 0.8106302
    [50,] 1.0438946 1.0438946
##
   [51,] 1.6382724 1.8335772
    [52,] 0.8967069 1.5415856
##
    [53,] 0.2845800 1.0966414
##
    [54,] 0.2937943 0.5959693
##
    [55,] 0.8157267 1.1865089
   [56,] 1.7304244 0.7709779
    [57,] 0.9641327 0.9641327
##
    [58,] 1.1095410 1.1095410
    [59,] 0.4905547 1.7864279
##
    [60,] 1.4770337 1.4580289
    [61.] 1.4716320 0.7764980
##
    [62,] 0.4231334 1.5052572
    [63,] 0.9207055 1.6692847
##
    [64,] 0.8541225 1.3825239
    [65,] 0.3255503 0.7068747
    [66,] 1.6609593 1.6083194
    [67,] 0.7199052 0.8760474
##
    [68,] 1.4132883 1.0542712
    [69,] 1.0548427 1.0548427
##
    [70,] 1.4212127 1.4212127
   [71,] 1.1571475 1.1571475
##
    [72,] 1.9039548 1.2029723
##
    [73,] 1.8747115 1.4495716
##
   [74,] 1.2430015 0.8337790
##
   [75,] 0.5578454 0.4163779
##
    [76,] 0.5522280 0.7744843
##
    [77,] 0.9639062 0.7983927
    [78,] 1.1880340 1.1880340
##
   [79,] 0.8959318 1.3004355
    [80,] 1.2700041 1.4562438
##
    [81,] 1.5622249 0.6504415
    [82,] 0.4966494 1.5473649
##
    [83,] 1.3070725 1.4034855
    [84,] 2.3283857 2.3283857
##
    [85,] 1.4338381 1.3599487
   [86,] 0.9134427 1.4959542
##
    [87,] 1.9524758 1.2131475
##
    [88,] 1.3039432 2.1246588
##
   [89,] 1.1517282 1.1517282
##
  [90,] 1.0758669 0.6974877
  [91,] 1.3240072 1.0131918
```

```
## [92,] 1.3929176 1.3929176

## [93,] 0.8618756 1.1628052

## [94,] 1.0279477 2.2674708

## [95,] 2.1891051 2.1891051

## [96,] 1.1235170 1.3370961

## [97,] 0.9807383 0.7336026

## [98,] 1.2952894 1.7084950

## [99,] 0.8106716 1.5534555

## [100,] 1.2689368 0.5307114
```

- 2 Q2. Generate 100 random from an absolutely continuous bivariate Generalized exponential, absolutely continuous Bivariate Weibull distribution.
- 2.1 Absolutely Continuous Bivariate Generalized Exponential Distribution

To calculate BVGE-AC we will first generate a GE using genExp.

```
genExp<-function(alpha, lambda){
  (-(1/lambda) * log(1 - (runif(1)^(1/alpha))))
}</pre>
```

Lets generate 100 BVGE-AC with parameters $(\lambda, \alpha_1, \alpha_2, \alpha_3) = (0.04, 1, 2, 0.5)$.

```
N = 100
X = matrix(NA, N, 2)

i = 1
while(i <= N) {
    u_0 = genExp(alpha[1], lambda)
    u_1 = genExp(alpha[2], lambda)
    u_2 = genExp(alpha[3], lambda)
    x1 = max(u_0, u_1)
    x2 = max(u_0, u_2)
    if(x1 == x2) {
        next
    }
    X[i,] = c(x1, x2)
    i = i + 1
}</pre>
```

```
##
               [,1]
                          [,2]
    [1,] 166.623143
##
                     2.995476
    [2,] 14.101508 13.571480
    [3,] 24.945407
##
                     3.644292
##
    [4,] 170.602406 16.596414
##
    [5,] 245.916688 8.218372
    [6,] 31.142179 50.816810
    [7,] 16.865562 10.176493
##
```

```
##
     [8,]
           84.824042
                       26.180734
##
     [9,]
           33.494667
                       12.689829
    [10,]
           37.645444 142.941610
##
    [11,]
           18.630140
                        7.399741
##
##
    [12,]
           46.919233
                        1.039311
##
    [13,]
           62.485132
                       32.926388
                        6.015652
    [14,]
           22.326685
##
    [15,]
           17.201596
##
                       12.093777
##
    [16,]
           11.205144
                       10.113635
##
    [17,]
           63.592825
                       11.270820
    [18,]
           51.118164
                       35.121781
    [19,]
           37.212087
##
                       15.064262
                       95.054468
##
    [20,]
           31.957090
##
    [21,] 131.059514
                       19.527750
##
    [22,]
           13.587197
                        8.971881
##
    [23,]
           30.336378
                        1.411553
##
    [24,]
           81.660957
                        3.111607
##
    [25,]
           55.980265
                       58.209563
    [26,]
           81.160713
##
                       40.460184
##
    [27,]
           40.233614
                       35.379565
##
    [28,]
           44.817404
                       25.980321
##
    [29,]
           70.533717
                        7.078962
##
    [30,]
           40.975607
                       22.554061
    [31,]
            7.597524
                       28.940312
##
           38.362948
##
    [32,]
                        9.923999
    [33,] 148.804993
                       37.192352
##
    [34,]
            9.871421
                       19.525137
    [35,]
           33.342454
##
                        6.555366
##
    [36,]
           38.897150
                        9.586244
    [37,]
##
           33.194915
                       43.792320
##
    [38,]
           37.173969
                       40.544551
##
    [39,]
           36.963627
                        1.661150
##
    [40,]
           26.220216
                       19.604363
    [41,]
           19.154948
                        1.976823
##
##
    [42,]
           17.566260
                       10.843680
##
    [43,] 107.863604
                       22.938380
##
    [44,]
           41.331912
                       30.431111
##
    [45,]
           46.512952
                       34.863485
##
    [46,]
           36.967473
                       50.536334
##
    [47,]
           23.794342
                       20.750151
    [48,]
           61.678293
                       54.466703
##
    [49,]
           48.593993
                       12.931412
    [50,]
           19.758776
##
                       11.796338
##
    [51,]
           52.437308
                       41.911303
    [52,]
           30.522659
##
                       14.247339
    [53,]
                        9.738188
##
           85.216816
##
    [54,]
           19.818774
                        5.225307
##
           41.723795
    [55,]
                       38.825726
##
    [56,] 154.746125
                       29.691365
##
    [57,]
           83.155347
                       44.062084
##
    [58,]
           57.964031
                       26.568405
##
    [59,]
           25.488444
                       18.565966
##
    [60,]
           20.425199
                       18.555669
##
    [61,]
           98.096339
                       21.652586
```

```
##
    [62,]
           42.990392
                       25.215489
##
    [63,]
           10.928949
                        6.720731
    [64,]
##
           17.349339
                        2.782620
    [65,]
           29.897748
                        4.236304
##
           27.575869
##
    [66,]
                       21.737578
##
    [67,] 110.980113
                       85.212744
    [68,]
           40.006935
##
                        8.593092
##
    [69,]
           14.446809
                        5.790400
    [70,]
##
           42.532057
                        4.594376
##
    [71,]
           78.095878
                       53.568953
##
    [72,]
           14.316188
                       24.893120
    [73,]
           46.077679
##
                       25.365492
##
    [74,]
           70.119716
                       22.372842
    [75,]
##
           33.979716
                       17.339368
##
    [76,]
           41.731295
                       17.403252
##
    [77,]
           39.176505
                       31.431025
##
    [78,]
           46.641843
                       25.985916
##
    [79,]
            6.851052
                        3.086978
    [80,]
           77.108736
##
                       76.104149
##
    [81,]
           68.048791
                       43.713614
##
    [82,]
           37.005808
                       89.806985
##
    [83,]
           50.636486
                        2.142283
##
    [84,]
           44.182817
                       32.528308
                       31.131488
    [85,]
           23.918423
##
##
    [86,]
           31.869938
                        5.826133
##
    [87,]
           63.978272
                       57.398700
##
    [88,] 107.933940
                        6.313408
##
    [89,]
           32.164199
                       31.849267
##
    [90,]
           75.644883
                       50.680514
##
    [91,]
           58.309820
                        2.729008
##
    [92,]
           49.127921
                        5.821787
##
    [93,]
             5.342036
                        1.036605
##
    [94,]
           55.779966
                       45.826331
           45.825651 168.604121
##
    [95,]
##
    [96,] 150.513288
                       36.597048
##
                       23.642128
    [97,]
           11.342637
##
    [98,]
           27.259334
                       56.071272
##
    [99,]
           13.522676
                        2.034529
## [100,]
           80.724235
                       62.605233
```

2.2 Absolutely Continuous Bivariate Weibull Distribution

To calculate BW we will first generate a Weibull using genWeibull.

```
genWeibull<-function(lambda, alpha){
  (((-log(1 - (runif(1)^(1/lambda))))^(1/alpha)))
}</pre>
```

Lets generate 100 BW-AC with parameters $(\alpha, \lambda_1, \lambda_2, \lambda_3) = (2, 0.5, 1, 2)$.

```
N = 100
X = matrix(NA, N, 2)
```

```
i = 1
while(i <= N) {</pre>
    u_0 = genWeibull(lambda[1], alpha)
    u_1 = genWeibull(lambda[2], alpha)
    u_2 = genWeibull(lambda[3], alpha)
    x1 = \min(u_0, u_1)
    x2 = \min(u_0, u_2)
    if(x1 == x2) {
        next
    X[i,] = c(x1, x2)
    i = i + 1
}
X
##
               [,1]
##
     [1,] 0.4726397 0.4692683
##
     [2,] 0.3010679 0.9768795
##
     [3,] 1.4073465 0.9013180
##
     [4,] 0.6368608 1.1551638
##
     [5,] 0.7637175 0.7761144
##
     [6,] 0.4433259 0.8561968
##
     [7,] 0.6947942 0.7716213
     [8,] 0.3900912 0.4491880
##
     [9,] 0.7531553 0.7181241
## [10,] 1.0904426 1.0688591
   [11,] 0.5444482 0.6817445
##
## [12,] 0.7862929 0.8680676
## [13,] 0.8696646 1.1551976
## [14,] 0.5341866 1.0629082
## [15,] 0.5222446 0.4951530
## [16,] 0.1813412 0.6833863
## [17,] 0.4251942 0.6911030
## [18,] 0.5283130 0.6433881
## [19,] 0.8303231 0.8453176
## [20,] 0.8508425 0.9815838
## [21,] 0.9147454 1.4172201
## [22,] 0.2999970 0.6179247
## [23,] 0.9076358 1.1679432
## [24,] 0.3348133 0.7299876
```

[25,] 0.2707065 0.4030949
[26,] 0.8737152 0.4652092
[27,] 1.0141351 0.9437535
[28,] 0.9071146 0.8379486
[29,] 0.1167770 0.7085718
[30,] 1.0442682 0.7156030
[31,] 0.9061755 1.1380205
[32,] 0.8052872 0.8176728
[33,] 0.4085028 0.5907606
[34,] 0.8901113 1.0264840
[35,] 1.1126195 0.8296021
[36,] 1.1732083 1.3722242
[37,] 0.7441256 0.7204840

```
[38,] 0.2094891 0.4746446
    [39,] 0.3518113 0.9690834
    [40,] 0.1753898 0.9009455
    [41,] 0.1679618 1.2658004
    [42,] 0.5059163 0.5733547
##
    [43,] 0.3471213 0.9010695
    [44,] 0.9186418 0.8644508
##
    [45,] 0.7177780 0.9577449
    [46,] 0.5360858 0.7308727
    [47,] 0.7019440 0.7216478
    [48,] 0.8234410 1.1578482
##
    [49,] 0.8310722 0.8689524
    [50,] 0.3967068 0.4695760
##
    [51,] 1.1106350 0.9829099
    [52,] 0.6114076 0.5767296
##
    [53,] 0.1075524 1.4003699
##
    [54,] 0.7606170 0.6353678
    [55,] 0.1021357 0.6254384
    [56,] 0.2041881 0.3083150
    [57,] 0.4775905 0.8036995
##
    [58,] 0.1789022 0.3634048
    [59,] 0.1782202 0.9992379
##
    [60,] 0.6057025 1.0620131
    [61.] 1.1537883 0.9575717
##
    [62,] 0.1088842 0.1769351
    [63,] 0.8759420 1.2718542
##
    [64,] 0.5586672 0.3965232
    [65,] 0.3405828 1.1809191
    [66,] 0.3722944 1.0396782
    [67,] 0.7795772 1.0086191
##
    [68,] 0.2903497 0.8777798
    [69,] 0.8419007 1.0749510
    [70,] 1.0889172 0.5291603
    [71,] 0.1155084 0.9389237
##
    [72,] 0.5190804 0.6321418
    [73,] 1.0600846 0.5989394
##
    [74,] 0.5089300 0.8813736
##
    [75,] 1.0282478 0.7330704
##
    [76,] 0.6130599 1.2135201
##
    [77,] 0.2175158 0.8548843
    [78,] 0.8390483 0.9078749
##
    [79,] 0.4891769 0.5996401
    [80,] 0.8572551 0.7025048
##
    [81,] 0.1565169 0.5873108
    [82,] 0.1796304 0.9298227
##
    [83,] 0.2500905 1.4960874
    [84,] 0.3208099 0.5342383
    [85,] 0.2899484 0.3849096
    [86,] 0.6276136 0.5920558
##
    [87,] 0.3043504 0.4865439
##
    [88,] 0.9396104 1.1438140
##
   [89,] 0.4355675 0.7917542
   [90,] 0.2965748 0.4929528
    [91,] 0.2725490 0.9967585
```

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## [92,] 1.0670911 1.6868732

## [93,] 1.1122417 0.8885766

## [94,] 0.7220633 0.7358017

## [95,] 0.6761444 0.9091799

## [96,] 0.1783027 0.4936088

## [97,] 0.3995286 0.6111690

## [98,] 0.8480712 1.0899781

## [99,] 0.5598902 0.9211651

## [100,] 0.8856401 1.0322035
```