

How To find Outliers.

data = [45, 67, 56, 78, 90, 45, 67, 89, 92, 55, 77, 88, 99, 74, 63, 150, 200].

Step-1 → Sort the data in ascending order.

data = [45, 45, 55, 56, 63, 67, 67, 74, 78, 77, 88, 89, 90, 92, 99, 150, 200].

Step-2 → Find Quartiles & Median
(Q_1 , Q_2 & Q_3).

Median (Q_2) → $\left(\frac{n+1}{2}\right)^{\text{th}}$ term (as n is odd).

$$\rightarrow \left(\frac{17+1}{2}\right)^{\text{th}} = \left(\frac{18}{2}\right)^{\text{th}} \text{ term} = 9^{\text{th}} \text{ term} = \boxed{78}$$

Now median (Q_2) is 78 which is the 9th term of our sorted data.
Now we will find Q_1 & Q_3 .

from first 8 elements
of data

from last 8
elements of
data.

Q₁ (Median of lower half).

[45, 45, 55, 56, 63, 67, 67, 74].
even number of elements.

$$\Rightarrow \left(\frac{n}{2} \right)^{\text{th}} \text{ term} + \left(\frac{n+1}{2} \right)^{\text{th}} \text{ term}$$

$$\Rightarrow \left(\left(\frac{8}{2} \right)^{\text{th}} + \left(\frac{8+1}{2} \right)^{\text{th}} \right) / 2$$

$$\Rightarrow \frac{4^{\text{th}} + 5^{\text{th}}}{2}$$

$$\Rightarrow \frac{56 + 63}{2} = \boxed{59.5}$$

Q₃ (Median of upper half):

[77, 88, 89, 90, 92, 99, 150, 200]

$$\Rightarrow \frac{12^{\text{th}} \text{ term} + 13^{\text{th}} \text{ term}}{2}$$

$$\Rightarrow \frac{90 + 92}{2} = \boxed{91}$$

Ques-3 → Calculate Interquartile Range (IQR).

$$IQR = Q_3 - Q_1 = 91 - 59.5$$

$$= \boxed{31.5}$$

Step 4 \Rightarrow Determine Outliers

Lower bound $\rightarrow Q_1 - 1.5 \times IQR$
 $\rightarrow 59.5 - 1.5 \times 31.5$
 $= 12.25$

Upper bound $\rightarrow Q_3 + 1.5 \times IQR$
 $\rightarrow 91 + 1.5 \times 31.5$
 $\rightarrow 138.25$

Identify Outliers

\Rightarrow Data Points below 12.25 &
~~or~~ above 138.25 are outliers.

Conclusion \rightarrow The outliers are 150 & 200.