

Structured Prediction and PyStruct

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Motivation

Multi-Label Classification

	Politics	Sports	Finance	Domestic	Religion
News Story1	1	0	0	1	1
News Story2	0	1	0	1	0
News Story3	0	0	1	0	0

Multi-Label Classification

	Politics	Sports	Finance	Domestic	Religion
News Story1	1	0	0	1	1
News Story2	0	1	0	1	0
News Story3	0	0	1	0	0

	Owns Car	Smokes	Married	Self-Employed	Has Kids
Customer1	1	0	1	0	1
Customer2	1	1	0	1	0
Customer3	0	1	1	0	0

Sequence Tagging



Sequence Tagging



Stroke cat.



Stroke cat.



Stroke cat.



Open trash can.



Put cat in trash can.

Sequence Tagging



Stroke cat.



Stroke cat.



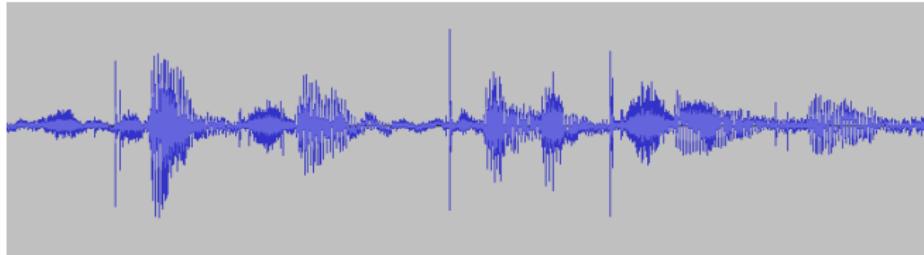
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Sequence Tagging



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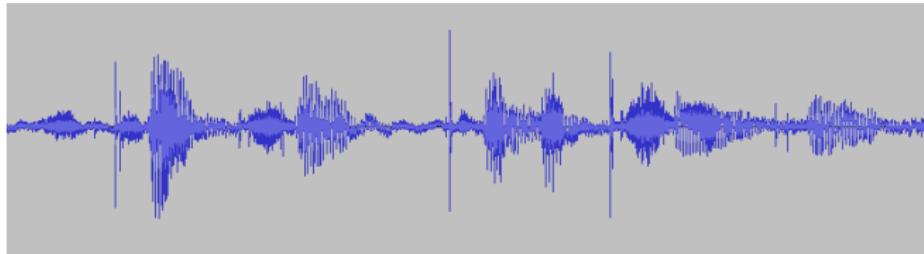
Stroke cat.



Open trash can.

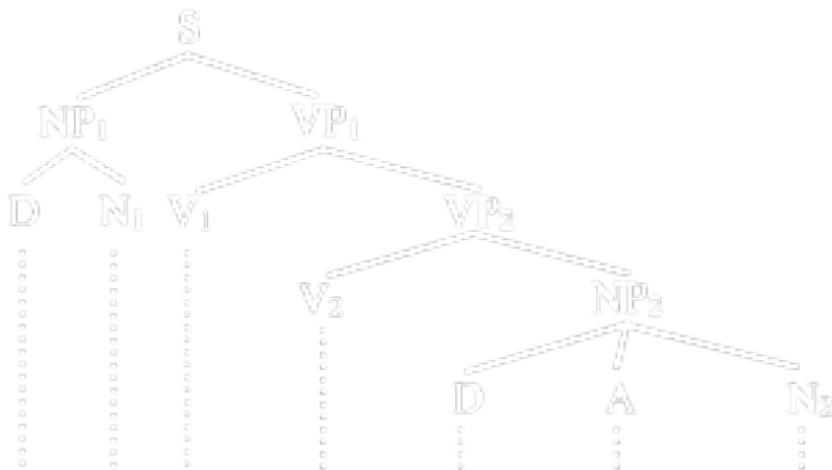


Put cat in trash can.



Struc-tured pre-dic-tion in Py-thon

Predicting Parse Trees



This tree is illustrating the constituency relation.

Constituency relation (PSG)

Semantic Images Segmentation



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Predicting Structured Objects

$$f(x, w) := \arg \max_{y \in \mathcal{Y}} g(x, y, w)$$

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$$\arg \max_{y \in \mathcal{Y}} p(y|x, w)$$

$$f(x, w) := \arg \max_{y \in \mathcal{Y}} w^T \psi(x, y)$$

Inference and Factor Graphs

Predicting discrete vectors

$$\mathbf{y} = (y_1, y_2, \dots, y_{n_i})$$

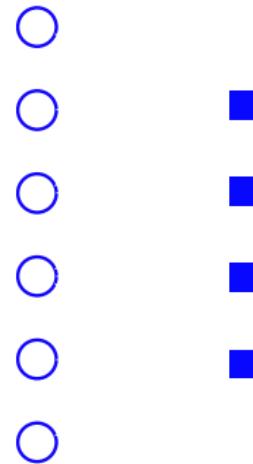
Predicting discrete vectors

$$y = (y_1, y_2, \dots, y_{n_i})$$

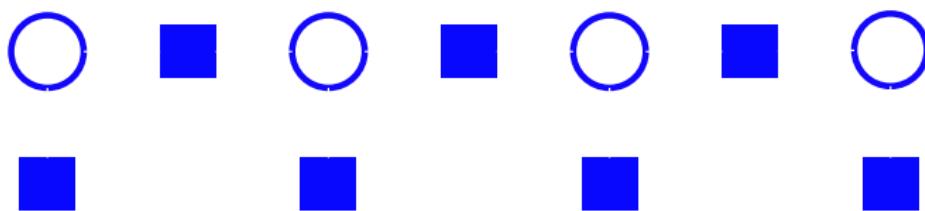
$$\begin{aligned} f(x, w) &= \arg \max_{y \in \mathcal{Y}} w^T \psi(x, y) \\ &= \arg \max_{y_1, y_2, \dots, y_{n_i}} w^T \psi(x, y) \end{aligned}$$

Factor Graphs

$$g(x, y) = g_1(x, y_1, y_2, y_3) + g_2(x, y_3, y_4) \\ + g_3(x, y_4) + g_4(x, y_4, y_5, y_6)$$

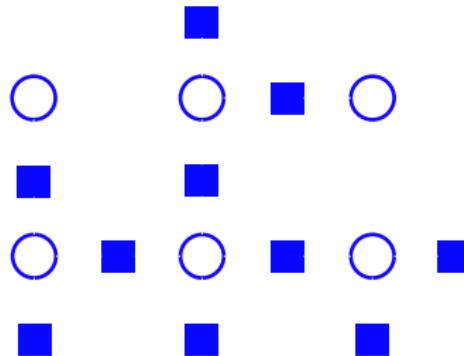


Factor Graph for HMM

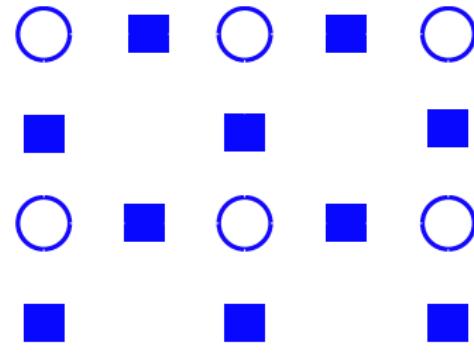


Inference

Easy



Tricky



Learning

Probabilistic Learning

$$p(y|x, w) = \frac{1}{Z} \exp(w^T \psi(x, y))$$

$$Z = \sum_{y' \in \mathcal{Y}} \exp(w^T \psi(x, y'))$$

Probabilistic Learning

$$p(y|x, w) = \frac{1}{Z} \exp(w^T \psi(x, y))$$

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Objective

$$\begin{aligned} & \max_w \sum_i \log(p(y^i|x^i, w)) \\ &= \max_w \sum_i w^T \psi(x^i, y^i) - \log(Z) \end{aligned}$$

Max-Margin Learning

$$\min_w \frac{1}{2} \|w\|^2 + C \sum_i \ell(x^i, y^i, w)$$

$$\ell(x^i, y^i, w) = [\max_{y \in \mathcal{Y}} \Delta(y^i, y) + w^T \psi(x^i, y) - w^T \psi(x^i, y^i)]_+.$$

PyStruct

Simple structured prediction

Estimator = Learner + Model + Inference

Simple structured prediction

Estimator = Learner + Model + Inference

- Learner: SubgradientSSVM, StructuredPerceptron, OneSlackSSVM, LatentSSVM
- Model: BinaryClf, MultiLabelClf, ChainCRF, GraphCRF, EdgeFeatureGraphCRF
- Inference: Linear Programming, QPBO (PyQPBO), Dual Decomposition (AD3), Message Passing (OpenGM), Everything (OpenGM)

Example OCR

```
from pystruct.datasets import load_letters
from pystruct.models import ChainCRF
from pystruct.learners import OneSlackSSVM

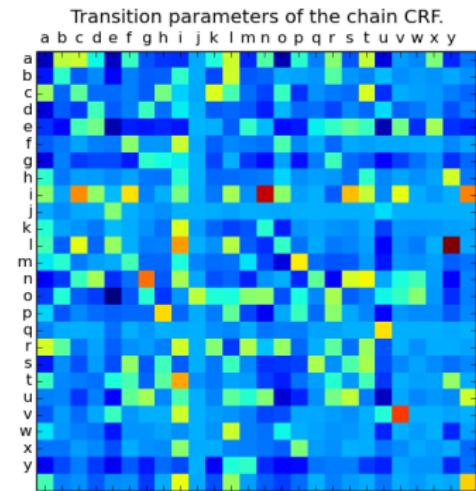
abc = "abcdefghijklmnopqrstuvwxyz"

letters = load_letters()
X, y, folds = letters['data'], letters['labels'], letters['folds']
# we convert the lists to object arrays, as that makes slicing much more
# convenient
X, y = np.array(X), np.array(y)
X_train, X_test = X[folds == 1], X[folds != 1]
y_train, y_test = y[folds == 1], y[folds != 1]

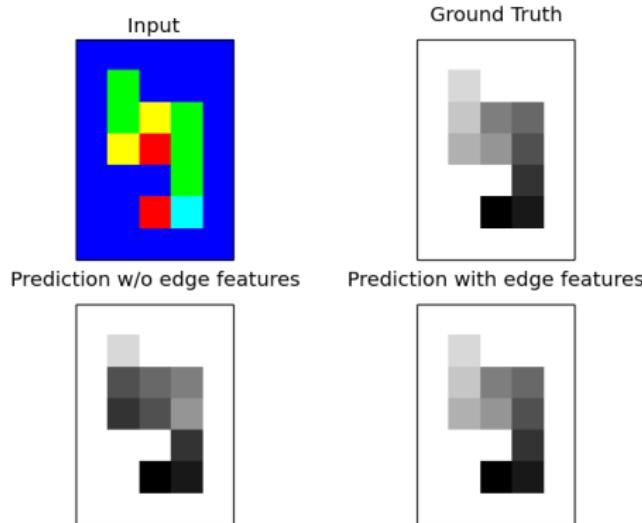
# Train linear SVM
svm = LinearSVC(dual=False, C=.1)
# flatten input
svm.fit(np.vstack(X_train), np.hstack(y_train))

# Train linear chain CRF
model = ChainCRF()
ssvm = OneSlackSSVM(model=model, C=.1, inference_cache=50, tol=0.1, verbose=3)
ssvm.fit(X_train, y_train)
```

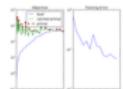
Example OCR



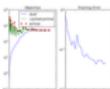
Example Snake



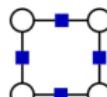
Examples



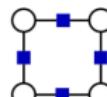
Plotting the objective and constraint caching in 1-slab SSVM



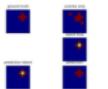
Efficient exact learning of 1-slab SSVMs



SVM as CRF



Semantic Image Segmentation on Pascal VOC



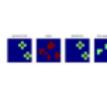
Latent Dynamics CRF



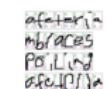
SVM objective values



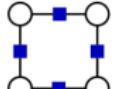
Learning directed interactions on a 2d grid



Learning interactions on a 2d grid



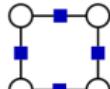
OCR Letter sequence recognition



Crammer-Singer Multi-Class SVM



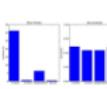
Latent SVM for odd vs. even digit classification



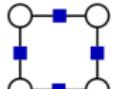
Mult-label classification



Latent Variable Hierarchical CRF



Binary SVM as SSVM



Comparing PyStruct and SVM-Struct