Orthogonal Sets

If for set $\{ec{u}_1,\ldots,ec{v}_n\}$ for j
eq k, $ec{u}_j \perp ec{u}_k$. i.e. $ec{u}_j \cdot ec{u}_k = 0$

If Set S is orthogonal, the vectors of S are linearly independent.

If we have an Orthogonal Basis $\{ ec{u}_1, \dots, ec{v}_n \}$ in \mathbb{R}^n then for any $ec{w} \in \mathbb{R}^n$,

$$\vec{w} = c_1 \vec{u}_1 + \dots + c_n \vec{v}_n$$

 C_q can be found using $c_q = rac{ec{w} \cdot ec{u}_q}{ec{u}_q \cdot ec{u}_q}$

Length of a Vector in the basis of an orthogonal set

If
$$ec{w}=c_1ec{u}_1+\cdots+c_nec{v}_n=(ec{w}\cdotec{u}_1)ec{u}_1+\cdots+(ec{w}\cdotec{u}_n)ec{v}_n$$

$$||ec{w}|| = \sqrt{(ec{w} \cdot ec{u}_1)^2 + \cdots + (ec{w} \cdot ec{u}_n)^2}$$