

# Gram-Schmidt Process

Given  $n$  [linearly independent](#) vectors that form the subspace  $W$ , you can use the Gram-Schmidt Process to find the orthogonal basis for  $W$ .

## 2 Vectors

We take one of the 2 vectors and find its 'z' using the other vector. Now this new vector and 'other' vector are the new orthogonal basis. As math:

Given the linearly independent vectors:  $\vec{v}, \vec{u}$  the orthogonal basis is  $\{\vec{v}, \vec{u} - \text{Proj}_{\vec{v}}\vec{u}\}$ .

More formally, given the linearly independent vectors:  $\vec{x}_1, \vec{x}_2$ ,

$$\begin{aligned}\vec{v}_1 &= \vec{x}_1 \\ \vec{v}_2 &= \vec{x}_2 - \frac{\vec{x}_2 \cdot \vec{x}_1}{\vec{x}_1 \cdot \vec{x}_1} \vec{x}_1\end{aligned}$$

Then the set  $\{\vec{v}_1, \vec{v}_2\}$  is the orthogonal basis.