

Quadratic Surfaces

Say we have a constant C

Curves in \mathbb{R}^2

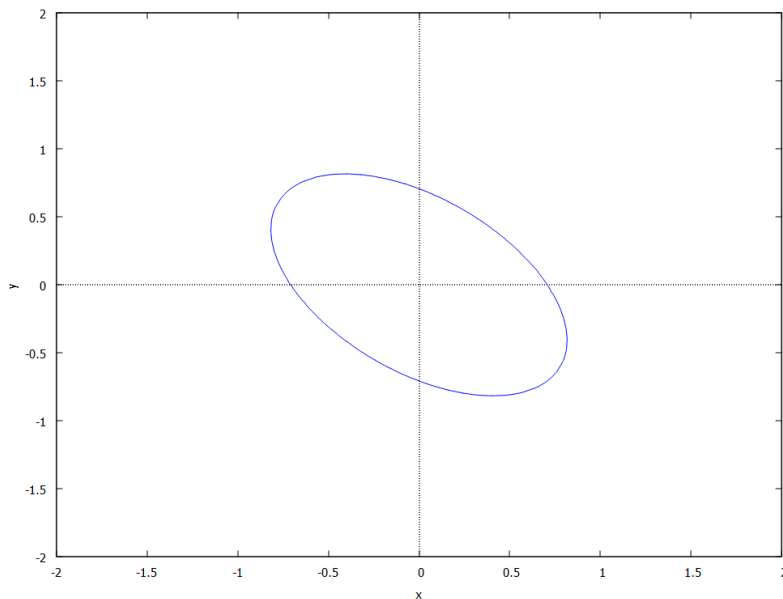
$Q(x) = x^T A x$ where $A \in \mathbb{R}^{2 \times 2}$. Then,

$$C = x^T A x$$

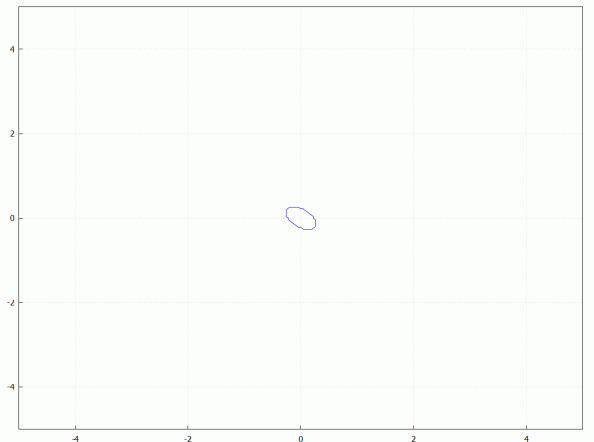
Is a curve in \mathbb{R}^2 .

Say $A = \begin{bmatrix} 2 & 1 \\ 1 & 2 \end{bmatrix}$. Then $Q(x) = 2x^2 + 2y^2 + 2xy = C$.

If $C = 1$ we can plot,



Here is it plotted when we changed C from 1 to 10.



Curves in \mathbb{R}^3

Say we have $z = Q(x)$, $z = x^2 + y^2 = x^T \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} x$

We can graph this,

