## **Diagonal Matrices**

Finding powers of a diagonal matrix, is very simple.

$$\begin{bmatrix} a & 0 \\ 0 & b \end{bmatrix}^k = \begin{bmatrix} a^k & 0 \\ 0 & b^k \end{bmatrix}$$

## Diagonalizable

If A is similar to diagonal matrix D ( $A = PDP^{-1}$ ) then A is diagonalizable.

## **Note:** Important

 $v_1 \dots v_n$  are eigenvectors

 $\lambda_1 \dots \lambda_n$  are eigenvalue

## Proof

We construct 
$$P=(\vec{v}_1\ \vec{v}_2\ \dots \vec{v}_n)$$
. Then 
$$AP=A(\vec{v}_1\ \vec{v}_2\ \dots \vec{v}_n)\\ =(A\vec{v}_1\ A\vec{v}_2\ \dots A\vec{v}_n)\\ =(\lambda_1\vec{v}_1\ \lambda_2\vec{v}_2\ \dots \lambda_n\vec{v}_n)\\ AP=(\vec{v}_1\ \vec{v}_2\ \dots \vec{v}_n)\begin{pmatrix} \lambda_1\\ \lambda_2\\ & \lambda_n \end{pmatrix}\\ =PD$$

Or, 
$$A = PDP^{-1}$$
.