Formulas

Formulas and Theorem

Expansion in Orthogonal Basis

If we have an Orthogonal Basis $\{ ec{u}_1, \dots, ec{v}_n \}$ in \mathbb{R}^n then for any $ec{w} \in \mathbb{R}^n$,

$$ec{w} = c_1 ec{u}_1 + \dots + c_n ec{v}_n$$

 C_q can be found using,

$$c_q = rac{ec{w} \cdot ec{u}_q}{ec{u}_q \cdot ec{u}_q}$$

Orthogonal Projection

Let non-zero $\vec{u} \in \mathbb{R}^n$, and $\vec{y} \in \mathbb{R}^n$. The orthogonal projection of \vec{y} onto \vec{u} is the vector in the span of \vec{u} that is closest to \vec{y} .

$$\mathrm{proj}_{ec{u}}ec{y} = rac{ec{y}\cdotec{u}}{ec{u}\cdotec{u}}ec{u}$$

Also, $ec{y} = \hat{y} + ec{z}$ and, $ec{z} \in W^{\perp}$