## Span

Given vectors  $\mathbf{v_1}, \mathbf{v_2}, \dots, \mathbf{v_p} \in \mathbb{R}^n$ . The set of all linear combinations of  $\mathbf{v_1}, \mathbf{v_2}, \dots, \mathbf{v_p}$  is called the **span** of  $\mathbf{v_1}, \mathbf{v_2}, \dots, \mathbf{v_p}$ .

Thus,  $\operatorname{span}\{\mathbf{v_1},\mathbf{v_2},\ldots,\mathbf{v_p}\}$  can be represented like this:

$$c_1\mathbf{v_1} + c_2\mathbf{v_2} + \cdots + c_p\mathbf{v_p}$$

Where  $c_1, c_2, \ldots, c_p$  are scalars.

Is  $\vec{y}$  in the span of vectors  $\vec{v}_1$  and  $\vec{v}_2$ ?

$$ec{v}_1=egin{pmatrix}1\-2\-3\end{pmatrix}$$
 ,  $ec{v}_2=egin{pmatrix}2\5\6\end{pmatrix}$  , and  $ec{y}=egin{pmatrix}7\4\15\end{pmatrix}$  .

$$c_1egin{bmatrix}1\-2\-3\end{bmatrix}+c_2egin{bmatrix}2\5\6\end{bmatrix}=egin{bmatrix}7\4\15\end{bmatrix}$$

$$egin{bmatrix} c_1 \ -2c_1 \ -3c_1 \end{bmatrix} + egin{bmatrix} 2c_2 \ 5c_2 \ 6c_2 \end{bmatrix} = egin{bmatrix} 7 \ 4 \ 15 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 2 & 7 \\ -2 & 5 & 4 \\ -3 & 6 & 15 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 2 & 7 \\ -2 & 5 & 4 \\ -1 & 2 & 5 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 2 & 7 \\ 0 & 1 & -6 \\ -1 & 2 & 5 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 2 & 7 \\ 0 & 1 & -6 \\ 0 & 1 & 3 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 19 \\ 0 & 1 & -6 \\ 0 & 1 & 3 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 19 \\ 0 & 1 & -6 \\ 0 & 0 & 9 \end{bmatrix}$$

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$$\begin{bmatrix} 1 & 0 & 19 \\ 0 & 1 & -6 \\ 0 & 0 & 1 \end{bmatrix}$$

So y is not in span  $\{\mathbf{v_1}, \mathbf{v_2}\}$ Look at Row Operations