

Formulas-2

$\lim_{(x,y) \rightarrow (x_0,y_0)} f(x,y) = L$ if for every $\epsilon > 0$, there exists a corresponding $\delta > 0$, such that for all (x,y) in the domain of f , $|f(x,y) - L| < \epsilon$ whenever $0 < \sqrt{(x - x_0)^2 + (y - y_0)^2} < \delta$

$$\frac{\partial f}{\partial x} \Big|_{(x_0,y_0)} = \lim_{h \rightarrow 0} \frac{f(x_0 + h, y_0) - f(x_0, y_0)}{h} = f_x(x_0, y_0)$$

$$f_{xx} = \frac{\partial^2 f}{\partial x^2} = \frac{\partial}{\partial x} \left(\frac{\partial f}{\partial x} \right)$$

$$f_{yy} = \frac{\partial^2 f}{\partial y^2} = \frac{\partial}{\partial y} \left(\frac{\partial f}{\partial y} \right)$$

$$f_{xy} = \frac{\partial^2 f}{\partial y \partial x} = \frac{\partial}{\partial y} \left(\frac{\partial f}{\partial x} \right)$$

$$f_{yx} = \frac{\partial^2 f}{\partial x \partial y} = \frac{\partial}{\partial x} \left(\frac{\partial f}{\partial y} \right)$$

$$f'_u(x,y) = D_u f(x,y) = \lim_{s \rightarrow 0} \frac{f(x + su_1, y + su_2) - f(x,y)}{s} = \nabla f(x,y) \cdot u$$

$$\frac{dw}{dt} = \frac{\partial w}{\partial x} \cdot \frac{dx}{dt} + \frac{\partial w}{\partial y} \cdot \frac{dy}{dt} + \frac{\partial w}{\partial z} \cdot \frac{dz}{dt}$$

$$\frac{dy}{dx} = -\frac{F_x}{F_y}$$