

# Mini-batch gradient descent

#### Batch vs. mini-batch gradient descent X { 4 } \ { 54 }.

Vectorization allows you to efficiently compute on m examples.

Andrew Ng

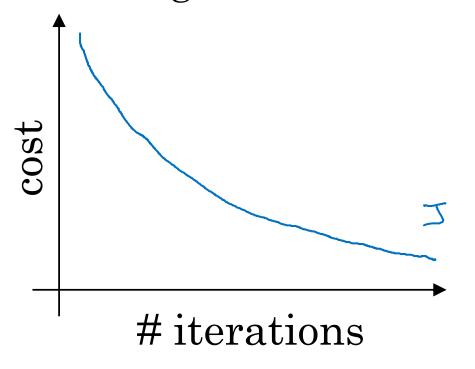
Mini-batch gradient descent stop of grabet deet veg XIII YIti. (as ifmel soo) Formal peop on X Sts. Arg = Prob on (Sers) } lestoisel implementation (1200 examples) A TW = 9 TW (2 TW) Compute cost  $J^{\{\ell\}} = \frac{1}{1000} \stackrel{\text{def}}{=} J(y^{(j)}, y^{(j)}) + \frac{\lambda}{2.1000} \stackrel{\text{E}}{=} ||W^{(1)}||_F^2$ . Bookprop to compart grobates cort JEE2 (usy (XEE2)) W:= W - ddw , btl) = btl) - ddbtes "I epoch" poss through training set.



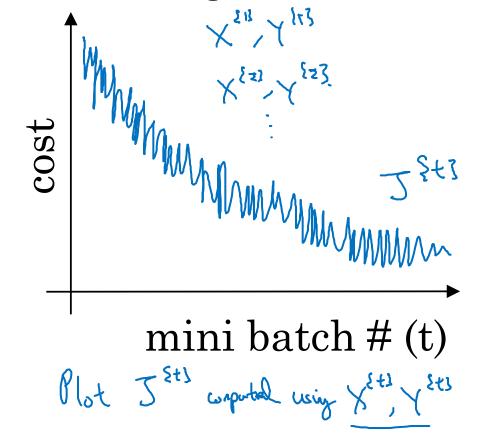
Understanding mini-batch gradient descent

#### Training with mini batch gradient descent

Batch gradient descent

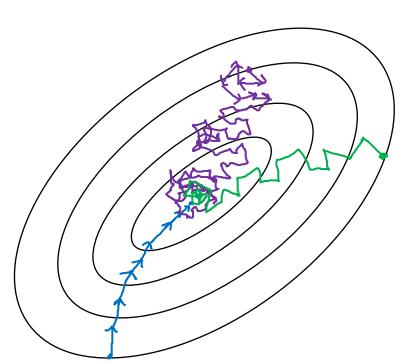


Mini-batch gradient descent



#### Choosing your mini-batch size

 $(X_{\xi i \hat{\gamma}}, X_{\xi i \hat{\gamma}}) = (X, X)$ > If mini-both size = m : Borth godnet desent.  $\rightarrow$  If Min=both Size=1: Stochaster ground descent. Every example is  $(X^{[H]},Y^{[I]})=(K^{(I)},Y^{(I)})\dots(X^{(I)},Y^{(I)})$  Min=both, Evange is it own In practice: Soreule in-between 1 aul m



Stochostic greb-t Descert Lose speakup from vortinition

In-bother (minthotal size not to by (small) Fustest learning. · Vectoraution. (N / 900)

Both gratient desemb (min; both size = m) Too long per iteration · Make propo without processy extra truly set.

Andrew Ng

#### Choosing your mini-batch size

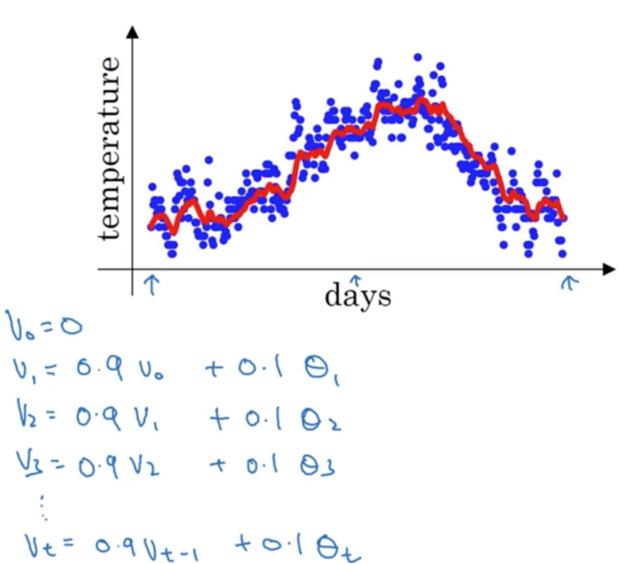
If small tray set: Use both graher descent.
(m < 2000) Typical minz-borth sizes! -> 64 , 128, 256, 512  $2^{2}$   $2^{8}$   $2^{3}$ Make sure ministrate fit in CPU/GPU memory. X Ex Y Ex 3



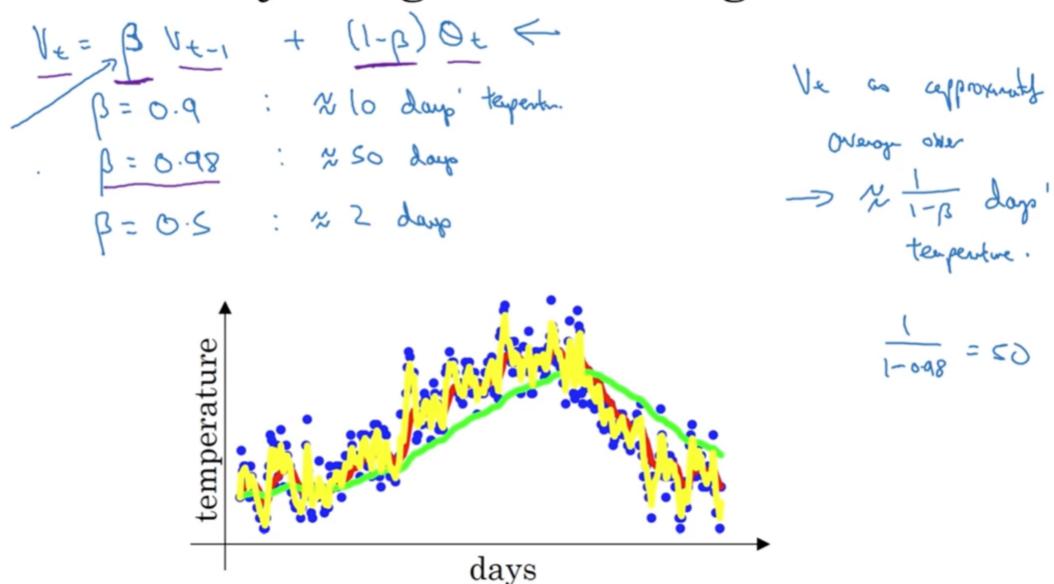
# Exponentially weighted averages

#### Temperature in London

```
\theta_{1} = 40^{\circ}F 9^{\circ}C \theta_{2} = 49^{\circ}F 9^{\circ}C \theta_{3} = 45^{\circ}F \vdots \theta_{180} = 60^{\circ}F 0^{\circ}C \theta_{181} = 56^{\circ}F 0^{\circ}C 0^
```



#### Exponentially weighted averages



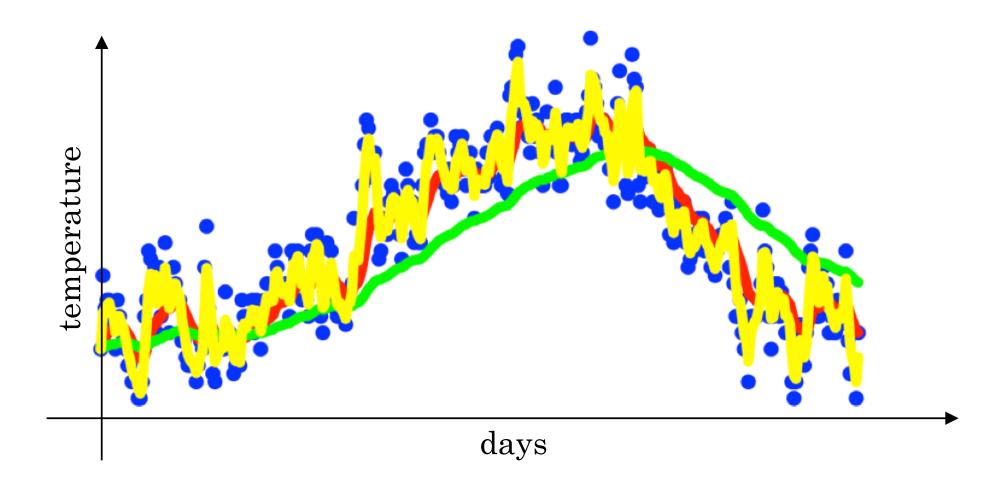


Understanding exponentially weighted averages

#### Exponentially weighted averages

$$v_t = \beta v_{t-1} + (1 - \beta)\theta_t$$





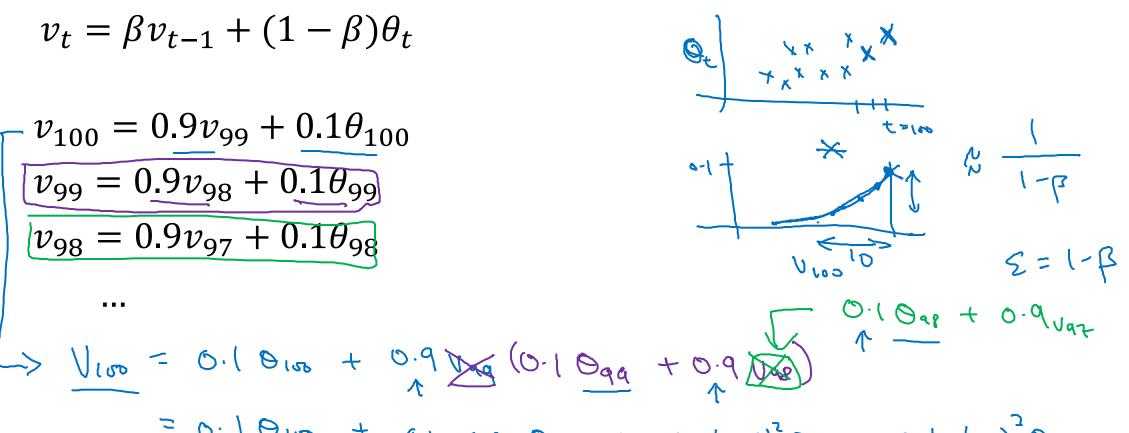
#### Exponentially weighted averages

$$v_t = \beta v_{t-1} + (1 - \beta)\theta_t$$

$$v_{100} = 0.9v_{99} + 0.1\theta_{100}$$

$$v_{99} = 0.9v_{98} + 0.1\theta_{99}$$

$$v_{98} = 0.9v_{97} + 0.1\theta_{98}$$
...



$$\frac{1}{\sqrt{2}} = \frac{1}{\sqrt{2}} = \frac{1$$

### Implementing exponentially weighted averages

$$v_0 = 0$$
  
 $v_1 = \beta v_0 + (1 - \beta) \theta_1$   
 $v_2 = \beta v_1 + (1 - \beta) \theta_2$   
 $v_3 = \beta v_2 + (1 - \beta) \theta_3$ 

$$V_{0} := 0$$
 $V_{0} := \beta V + (1-\beta) O_{1}$ 
 $V_{0} := \beta V + (1-\beta) O_{2}$ 
 $V_{0} := \beta V + (1-\beta) O_{2}$ 

> 
$$V_0 = 0$$

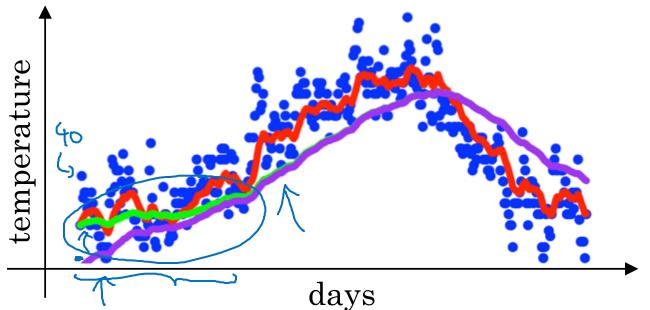
Repeat  $\xi$ 

Cut next  $0$ 
 $V_0 := \beta V_0 + (1-\beta)0$ 
 $\xi$ 



Bias correction in exponentially weighted average

#### Bias correction



0.0396

$$\frac{1-\beta^{t}}{1-\beta^{t}}$$

$$t=2: 1-\beta^{t} = 1-(0.98)^{2} = 0.0396$$

$$\frac{1-\beta^{t}}{0.0396} = 0.0396$$

$$\frac{1-\beta^{t}}{0.0396} = 0.0396$$

B = 0.08

$$v_{t} = \beta v_{t-1} + (1 - \beta)\theta_{t}$$

$$v_{0} = 0$$

$$v_{1} = 0.98 \quad v_{0} + 0.02 \quad \Theta_{1}$$

$$v_{1} = 0.98 \quad v_{0} + 0.02 \quad \Theta_{2}$$

$$v_{2} = 0.98 \quad v_{0} + 0.02 \quad \Theta_{2}$$

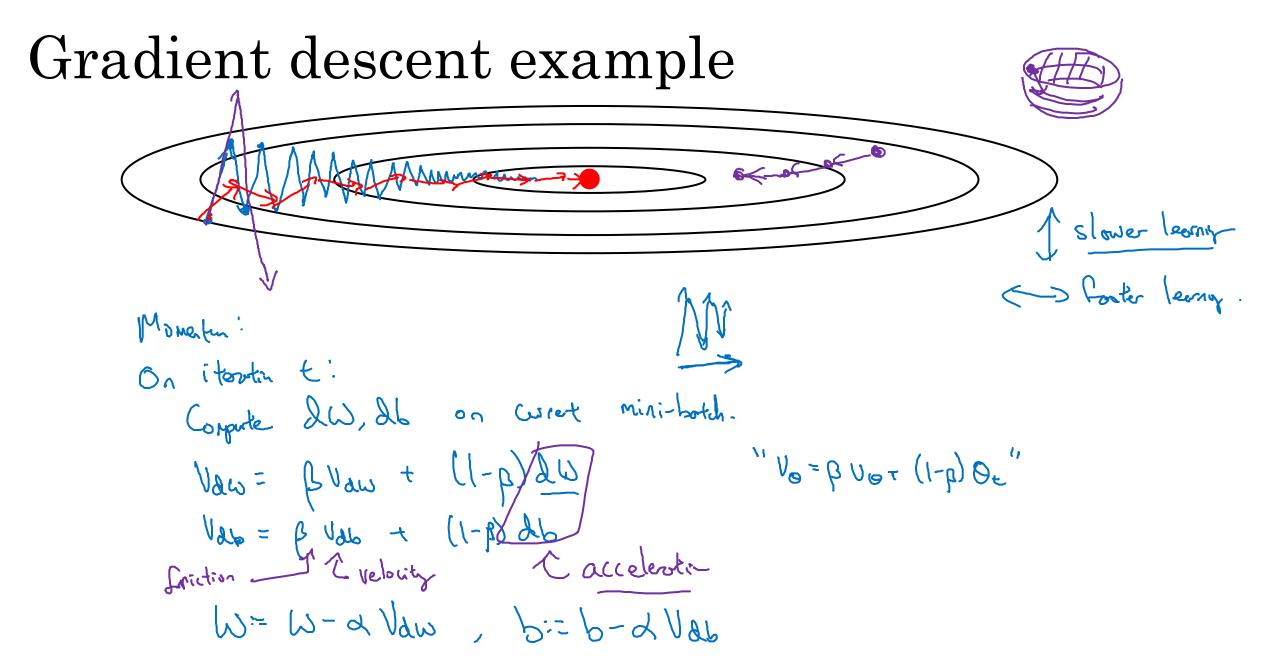
$$v_{3} = 0.98 \quad v_{0} + 0.02 \quad \Theta_{3}$$

$$v_{4} = 0.98 \quad v_{0} + 0.02 \quad \Theta_{2}$$

Andrew Ng



## Gradient descent with momentum



#### Implementation details

#### On iteration t:

Compute dW, db on the current mini-batch

$$v_{db} = \beta v_{db} + (1/\beta)db$$

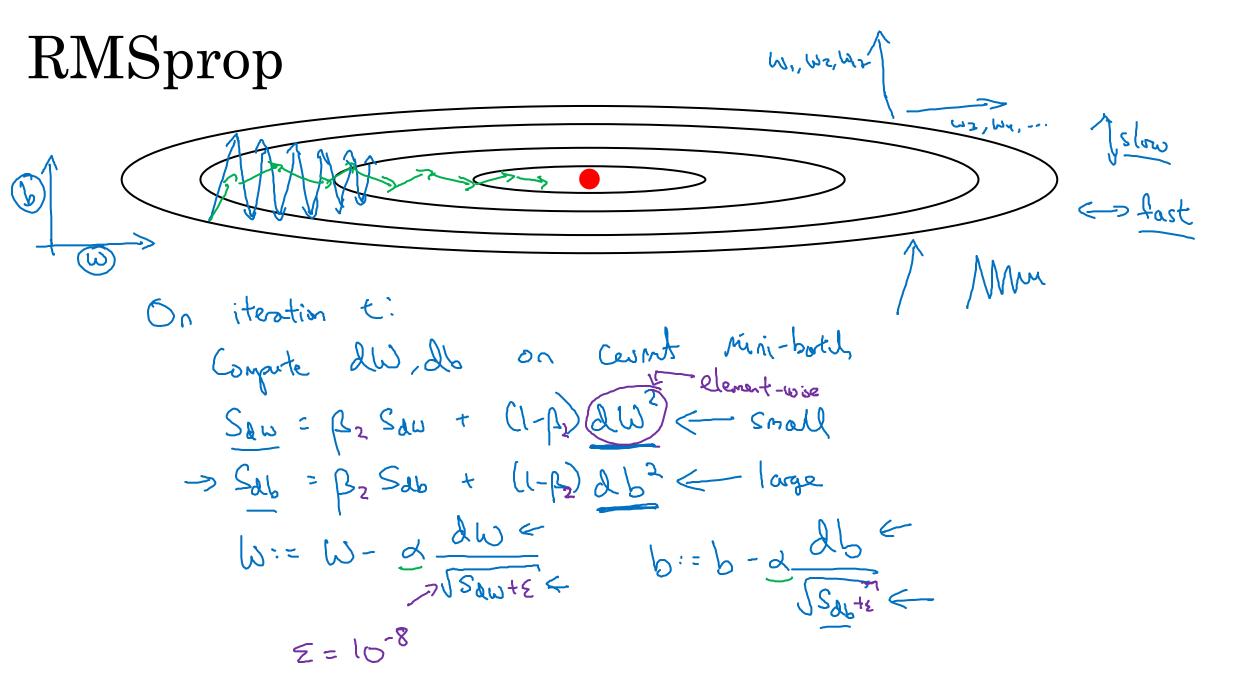
$$W = W - \alpha v_{dW}, \ b = \underline{b} - \alpha v_{db}$$

Hyperparameters: 
$$\alpha, \beta$$

$$\beta = 0.9$$
Overlose on lost 100 graduits



#### RMSprop





# Adam optimization algorithm

#### Adam optimization algorithm

#### Hyperparameters choice:

$$\rightarrow$$
  $\alpha$ : needs to be tune  
 $\rightarrow$   $\beta_i$ : 0.9  $\rightarrow$  ( $d\omega$ )  
 $\rightarrow$   $\beta_2$ : 0.999  $\rightarrow$  ( $d\omega^2$ )  
 $\rightarrow$   $\Sigma$ : 10-8

Adam: Adaptiv moment estimation

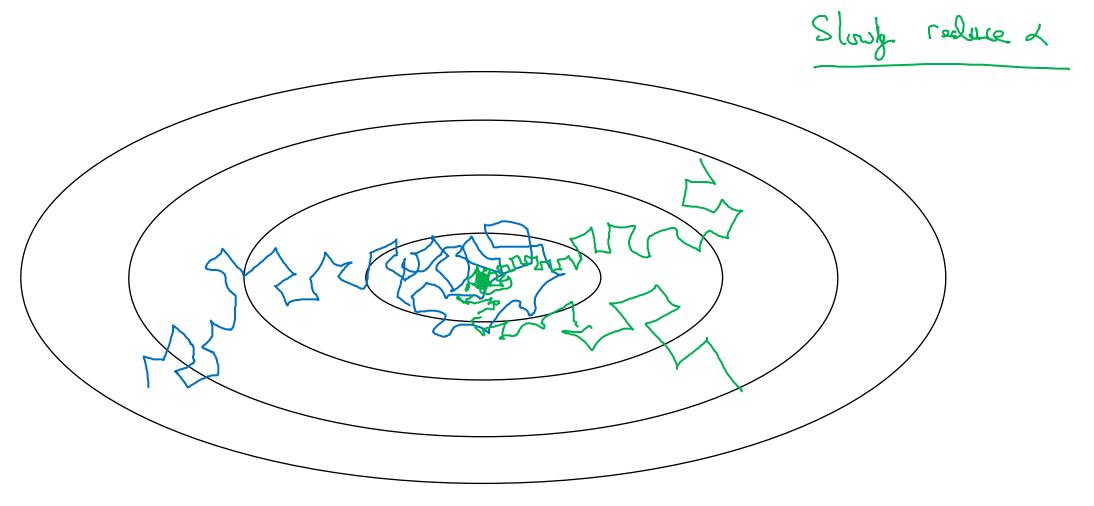


**Adam Coates** 

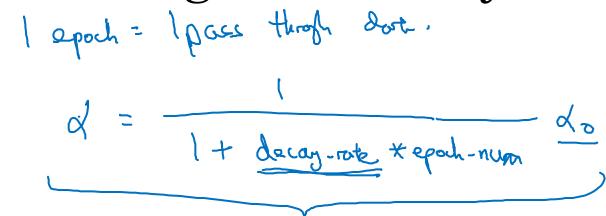


# Learning rate decay

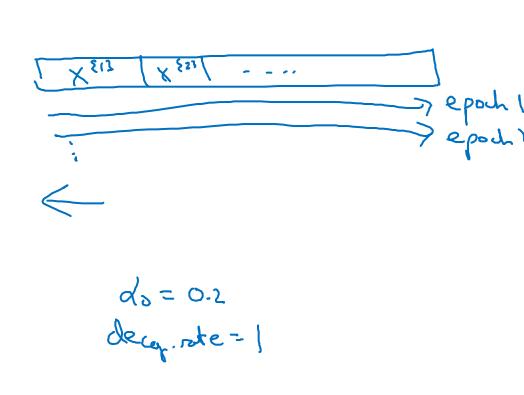
#### Learning rate decay

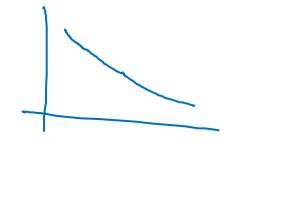


#### Learning rate decay

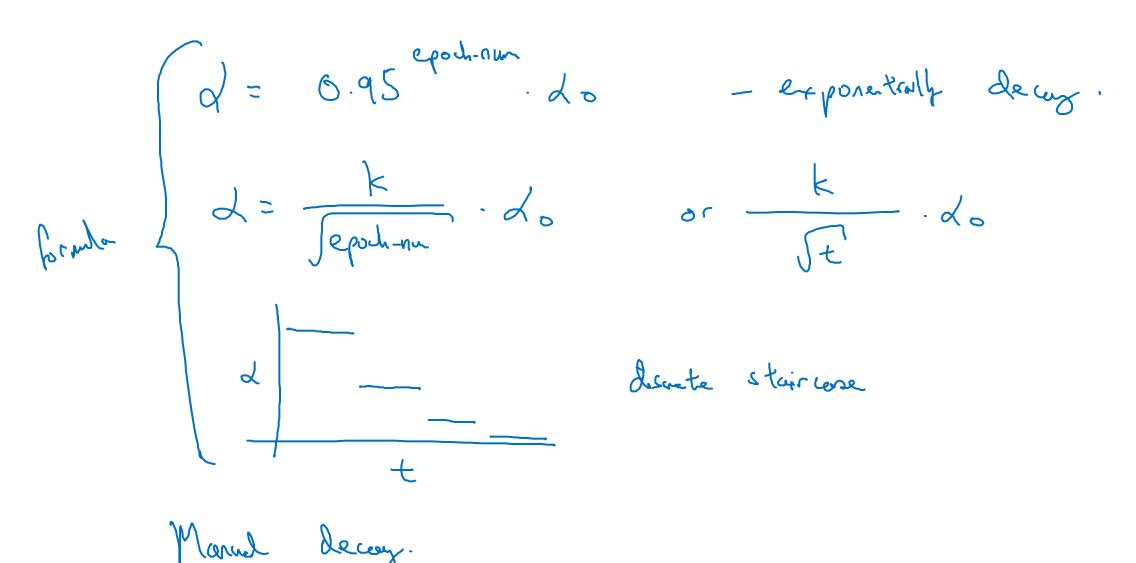


Epoch	2
	0.1
2	0.67
3	6.5
4	0.4
•	-





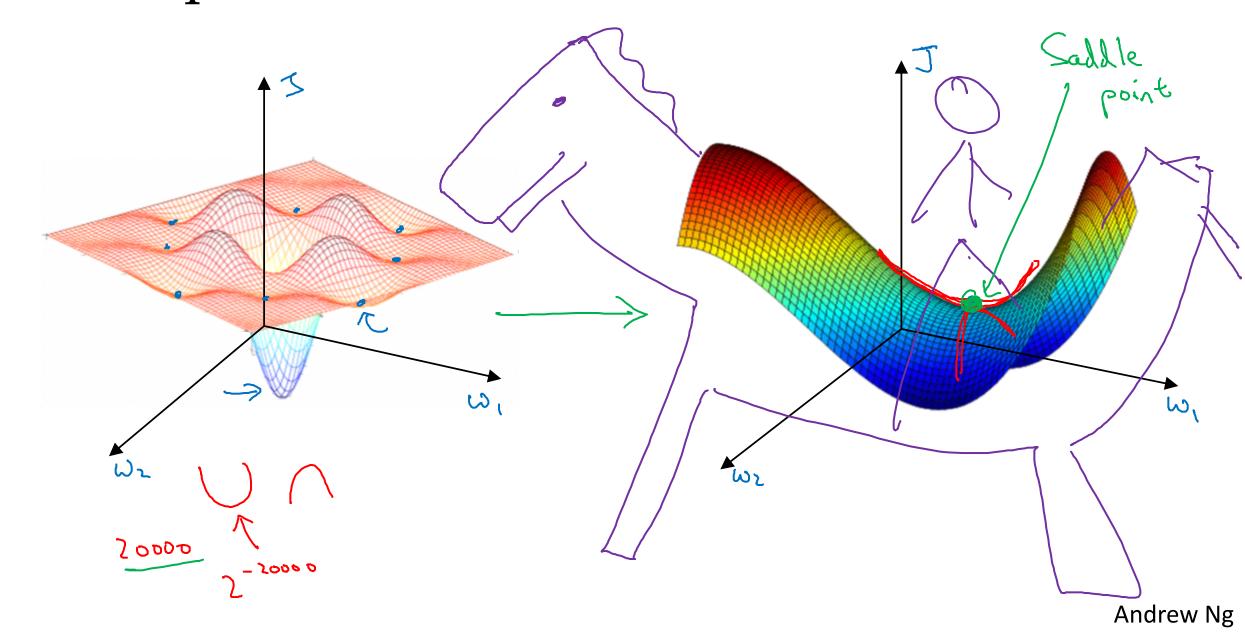
#### Other learning rate decay methods



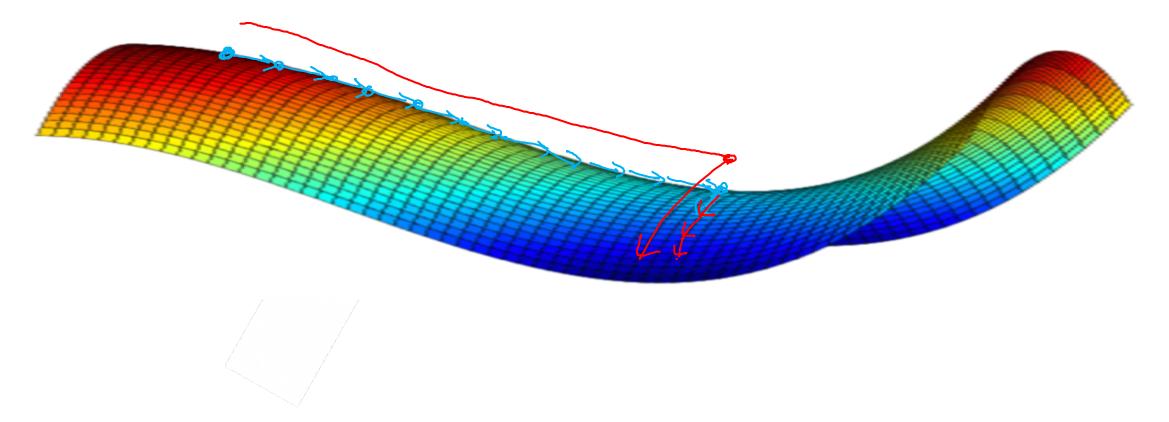


# The problem of local optima

#### Local optima in neural networks



#### Problem of plateaus



- Unlikely to get stuck in a bad local optima
- Plateaus can make learning slow