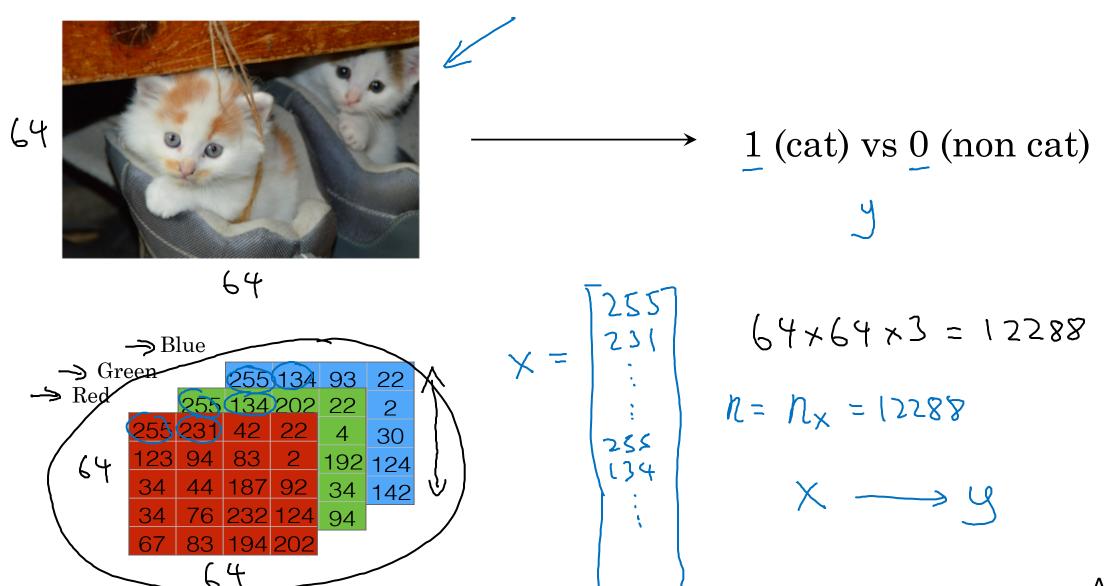


Basics of Neural Network Programming

Binary Classification

Binary Classification



Andrew Ng

Notation

$$(x,y) \times \mathbb{CR}^{n_{x}}, y \in \{0,1\}$$

$$m \text{ training evarples}: \{(x^{(1)},y^{(1)}), (x^{(1)},y^{(2)}), \dots, (x^{(m)},y^{(m)})\}$$

$$M = M \text{ train} \qquad M \text{ test} = \text{ $\#$ test examples}.$$

$$X = \begin{bmatrix} x^{(1)} & x^{(2)} & \dots & x^{(m)} \\ x^{(m)} & x^{(m)} & \dots & x^{(m)} \end{bmatrix}$$

$$X = \begin{bmatrix} x^{(1)} & x^{(2)} & \dots & x^{(m)} \\ x^{(m)} & x^{(m)} & \dots & x^{(m)} \end{bmatrix}$$

$$X \in \mathbb{R}^{n_{x} \times m}$$



Basics of Neural Network Programming

Logistic Regression

Logistic Regression

Given
$$x$$
, want $y = P(y=1|x)$
 $x \in \mathbb{R}^{n}x$
Parareters: $w \in \mathbb{R}^{n}x$, $b \in \mathbb{R}$.
Output $y = \sigma(w^{T}x + b)$
Output $y = \sigma(x)$

$$X_0 = 1, \quad x \in \mathbb{R}^{n_x + 1}$$

$$\hat{y} = 6 (0^{T}x)$$

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Basics of Neural Network Programming

Logistic Regression cost function

Logistic Regression cost function

Given
$$\{(x^{(1)}, y^{(1)}), \dots, (x^{(m)}, y^{(m)})\}$$
, want $\hat{y}^{(i)} \approx y^{(i)}$.

Since $\{(x^{(1)}, y^{(1)}), \dots, (x^{(m)}, y^{(m)})\}$, want $\hat{y}^{(i)} \approx y^{(i)}$.

Loss (error) function: $\int_{\mathcal{C}} (\hat{y}, y) = \frac{1}{2} (\hat{y} - y)^2$

The entropy of the second of the



Basics of Neural Network Programming

Gradient Descent

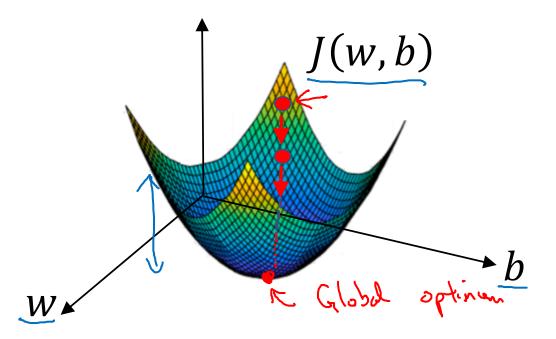
deeplearning.ai

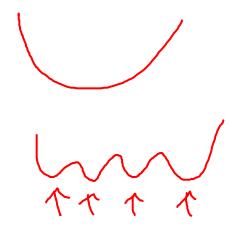
Gradient Descent

Recap:
$$\hat{y} = \sigma(w^T x + b)$$
, $\sigma(z) = \frac{1}{1 + e^{-z}}$

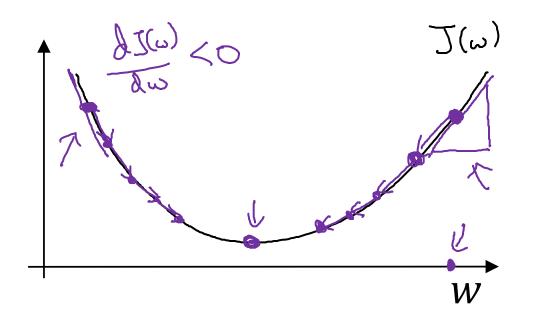
$$\underline{J(w,b)} = \frac{1}{m} \sum_{i=1}^{m} \mathcal{L}(\hat{y}^{(i)}, y^{(i)}) = -\frac{1}{m} \sum_{i=1}^{m} y^{(i)} \log \hat{y}^{(i)} + (1 - y^{(i)}) \log(1 - \hat{y}^{(i)})$$

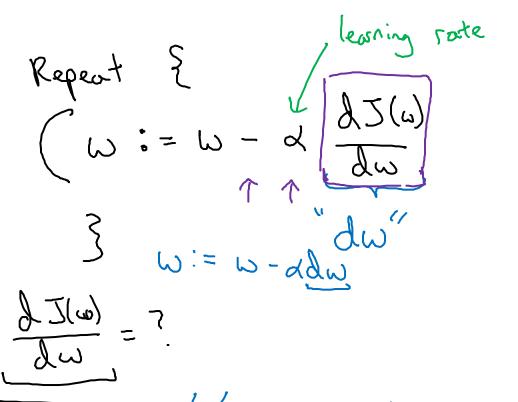
Want to find w, b that minimize J(w, b)

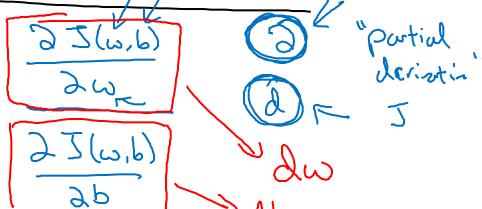




Gradient Descent





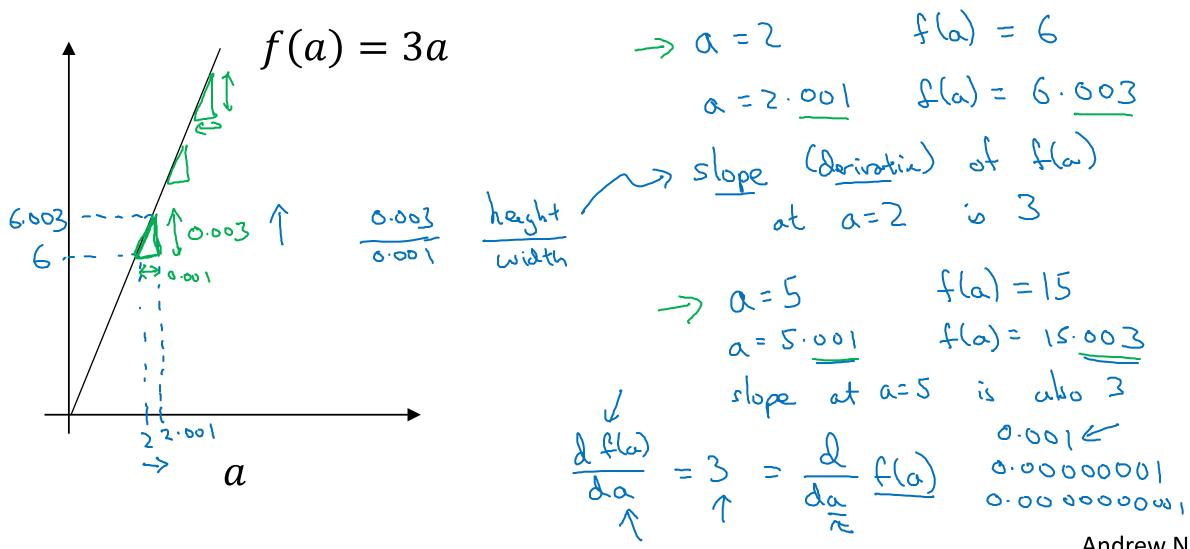




Basics of Neural Network Programming

Derivatives

Intuition about derivatives



Andrew Ng



Basics of Neural Network Programming

More derivatives examples

Intuition about derivatives







More derivative examples

$$f(a) = a^2$$

$$f(\omega) = \alpha^3$$

$$\frac{\lambda}{\lambda a} (a) = 3a^{2}$$
 $3x2^{3} = 12$

$$a = 2$$
 $f(a) = 4$
 $a = 2-001$ $f(a) = 4-004$

$$\sigma = 5.001$$
 $t(r) = 8$

$$Q = 5.001 \quad \text{fm} \approx 0.64312$$

$$Q = 5.001 \quad \text{fm} \approx 0.64362$$



Basics of Neural Network Programming

Computation Graph

Computation Graph

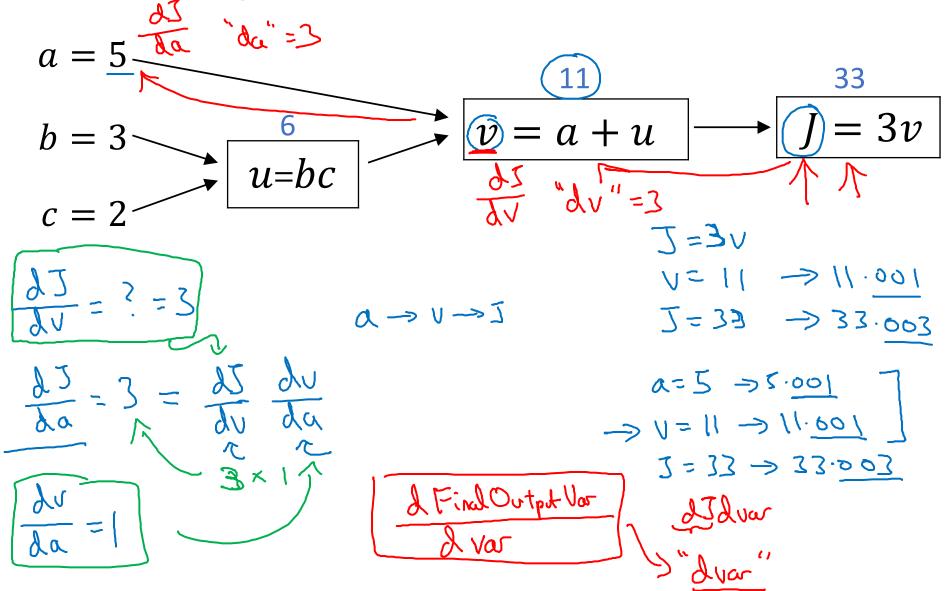
$$J(a,b,c) = 3(a+bc) = 3(5+3\pi^2) = 33$$
 $U = bc$
 $V = atu$
 $J = 3v$
 $V = a+u$
 $J = 3v$
 $V = a+u$
 $J = 3v$

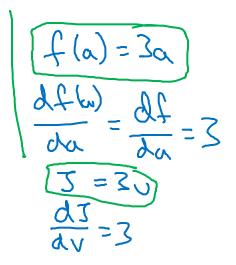


Basics of Neural Network Programming

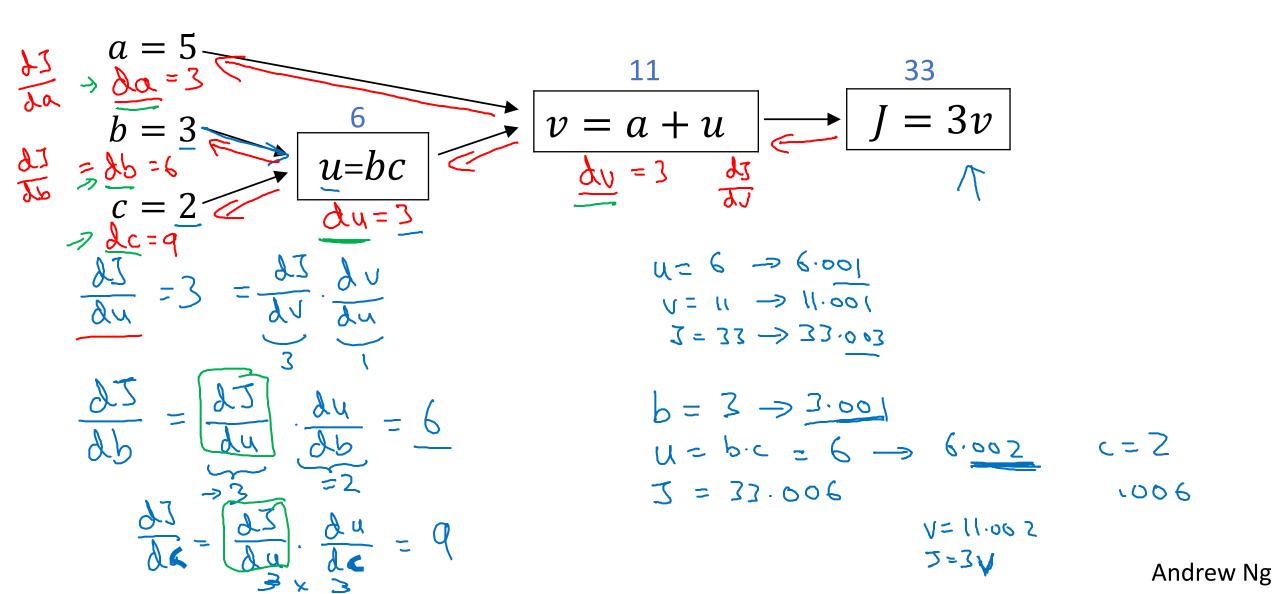
Derivatives with a Computation Graph

Computing derivatives





Computing derivatives





Basics of Neural Network Programming

Logistic Regression Gradient descent

Logistic regression recap

$$\Rightarrow z = w^{T}x + b$$

$$\Rightarrow \hat{y} = a = \sigma(z)$$

$$\Rightarrow \mathcal{L}(a, y) = -(y \log(a) + (1 - y) \log(1 - a))$$

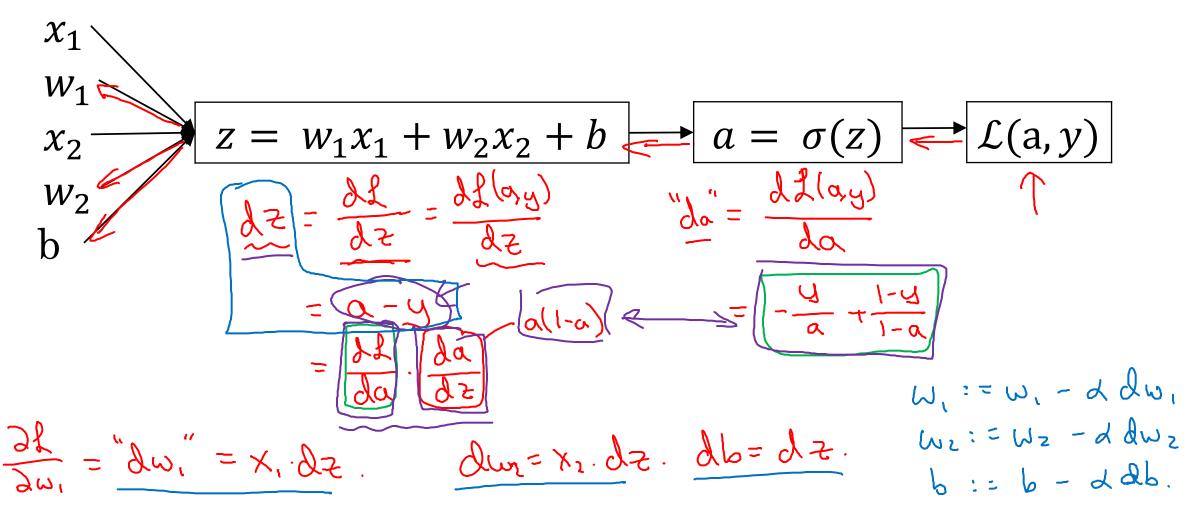
$$\begin{cases} \lambda_{1} \\ \lambda_{2} \\ \lambda_{3} \end{cases}$$

$$\begin{cases} \lambda_{1} \\ \lambda_{2} \\ \lambda_{3} \end{cases}$$

$$\begin{cases} \lambda_{2} \\ \lambda_{3} \end{cases}$$

$$\begin{cases} \lambda_{1} \\ \lambda_{2} \\ \lambda_{3} \end{cases}$$

Logistic regression derivatives





Basics of Neural Network Programming

Gradient descent on m examples

Logistic regression on m examples

$$\frac{J(u,b)}{J(u,b)} = \frac{1}{m} \sum_{i=1}^{m} f(a^{(i)}, y^{(i)}) \\
\Rightarrow a^{(i)} = f(x^{(i)}) = G(x^{(i)}, y^{(i)}) \\
\frac{\partial}{\partial u_i} J(u,b) = \frac{1}{m} \sum_{i=1}^{m} \frac{\partial}{\partial u_i} f(a^{(i)}, y^{(i)}) \\
\frac{\partial u_i}{\partial u_i} - (x^{(i)}, y^{(i)})$$

Logistic regression on m examples

$$J=0; dw_{1}=0; dw_{2}=0; db=0$$

$$For i=1 to m$$

$$Z^{(i)}=\omega^{T}x^{(i)}+b$$

$$Q^{(i)}=6(Z^{(i)})$$

$$J+=-[y^{(i)}(og Q^{(i)}+(1-y^{(i)})(og(1-q^{(i)})]$$

$$dz^{(i)}=Q^{(i)}-y^{(i)}$$

$$dw_{1}+=x^{(i)}dz^{(i)}$$

$$dw_{2}+=x^{(i)}dz^{(i)}$$

$$J=0; dw_{2}(1-q^{(i)})$$

$$dz^{(i)}=Q^{(i)}-y^{(i)}$$

$$dz^{(i)}=Q^{(i)}-y^{(i)}$$

$$dw_{1}+=x^{(i)}dz^{(i)}$$

$$dw_{2}+=x^{(i)}dz^{(i)}$$

$$J=0; dw_{2}(1-q^{(i)})$$

$$dz^{(i)}=Q^{(i)}$$

$$dw_{2}+=Q^{(i)}$$

$$dw_{3}+=Q^{(i)}$$

$$dw_{4}+=Q^{(i)}$$

$$dw_{4}+=Q^{(i)}$$

$$dw_{5}+=Q^{(i)}$$

$$dw_{6}+=Q^{(i)}$$

$$dw_{7}+=m; dw_{7}+=m; db/=m.$$

$$d\omega_1 = \frac{\partial J}{\partial \omega_1}$$
 $\omega_1 := \omega_1 - d d\omega_1$
 $\omega_2 := \omega_2 - \alpha d\omega_2$
 $b := b - d db$

We to right is a sum of the sum o



Basics of Neural Network Programming

Vectorization

What is vectorization?

for i in ray
$$(n-x)$$
:
 $2+=\omega [1] \times x$



Basics of Neural Network Programming

More vectorization examples

Neural network programming guideline

Whenever possible, avoid explicit for-loops.

$$U = AV$$

$$U_{i} = \sum_{i} \sum_{j} A_{ij} V_{ij}$$

$$U = np. zevos((n, i))$$

$$for i \dots \subseteq ACIT_{i} \exists *vC_{i} \exists$$

$$uCi \exists t = ACIT_{i} \exists *vC_{i} \exists$$

Vectors and matrix valued functions

Say you need to apply the exponential operation on every element of a matrix/vector.

$$v = \begin{bmatrix} v_1 \\ \vdots \\ v_n \end{bmatrix} \rightarrow \mathbf{u} = \begin{bmatrix} \mathbf{e}^{\mathbf{v}_1} \\ \mathbf{e}^{\mathbf{v}_2} \end{bmatrix}$$

$$v = \begin{bmatrix} v_1 \\ \vdots \\ v_n \end{bmatrix} \rightarrow u = \begin{bmatrix} e^{v_1} \\ e^{v_n} \end{bmatrix}$$

$$u = \text{np. exp}(v) \leftarrow$$

$$\text{np. log}(v)$$

$$\text{np. abs}(v)$$

$$\text{np. havinum}(v, o)$$

Logistic regression derivatives

$$J = 0, \quad dw1 = 0, \quad dw2 = 0, \quad db = 0$$

$$\Rightarrow \text{ for } i = 1 \text{ to } n:$$

$$z^{(i)} = w^{T}x^{(i)} + b$$

$$a^{(i)} = \sigma(z^{(i)})$$

$$J + = -[y^{(i)}\log\hat{y}^{(i)} + (1 - y^{(i)})\log(1 - \hat{y}^{(i)})]$$

$$dz^{(i)} = a^{(i)}(1 - a^{(i)})$$

$$dw_{1} + x_{1}^{(i)}dz^{(i)}$$

$$dw_{2} + x_{2}^{(i)}dz^{(i)}$$

$$db + dz^{(i)}$$

$$J = J/m, \quad dw_{1} = dw_{1}/m, \quad dw_{2} = dw_{2}/m, \quad db = db/m$$

$$d\omega / = m$$



Basics of Neural Network Programming

Vectorizing Logistic Regression

deeplearning.ai

Vectorizing Logistic Regression

$$Z^{(1)} = w^{T}x^{(1)} + b$$

$$Z^{(2)} = w^{T}x^{(2)} + b$$

$$Z^{(3)} = w^{T}x^{(3)} + b$$

$$Z^{(3)} = \sigma(z^{(3)})$$

$$Z^$$



Basics of Neural Network Programming

Vectorizing Logistic Regression's Gradient Computation

Vectorizing Logistic Regression

$$\frac{dz^{(1)} = a^{(1)} - y^{(1)}}{dz^{(2)}} = \frac{dz^{(2)} - y^{(2)}}{dz^{(2)}} - \frac{dz^{(2)}}{dz^{(2)}} - \frac{dz^{(2)}}{dz^{(2)}} = \frac{dz^{(2)} - y^{(2)}}{dz^{(2)}} - \frac{dz^{(2)}}{dz^{(2)}} = \frac{dz^{(2)} - y^{(2)}}{dz^{(2)}} - \frac{dz^{(2)}}{dz^{(2)}} - \frac$$

$$db = \frac{1}{m} \sum_{i=1}^{m} dz^{(i)}$$

$$= \frac{1}{m} \left[x^{(i)} + \dots + x^{(n)} dz^{(m)} \right]$$

$$= \frac{1}{m} \left[x^{(i)} + \dots + x^{(n)} dz^{(m)} \right]$$

$$= \frac{1}{m} \left[x^{(i)} + \dots + x^{(n)} dz^{(m)} \right]$$

$$= \frac{1}{m} \left[x^{(i)} + \dots + x^{(n)} dz^{(m)} \right]$$

Implementing Logistic Regression

J = 0,
$$dw_1 = 0$$
, $dw_2 = 0$, $db = 0$

for i = 1 to m:

$$z^{(i)} = w^T x^{(i)} + b$$

$$a^{(i)} = \sigma(z^{(i)}) \checkmark$$

$$J += -[y^{(i)} \log a^{(i)} + (1 - y^{(i)}) \log(1 - a^{(i)})]$$

$$dz^{(i)} = a^{(i)} - y^{(i)} \checkmark$$

$$dw_1 += x_1^{(i)} dz^{(i)}$$

$$dw_2 += x_2^{(i)} dz^{(i)}$$

$$dw_2 += dz^{(i)}$$

$$dw_1 += dz^{(i)}$$

$$dw_2 += dz^{(i)}$$

$$dw_3 += dz^{(i)}$$

$$dw_4 += dz^{(i)}$$

$$dw_5 += dz^{(i)}$$

$$dw_6 += dz^{(i)}$$

$$dw_7 += dw_7 / m$$

$$dw_7 = dw_7 / m$$

$$dw_7 = dw_7 / m$$

iter in range (1000)!
$$\angle$$

$$Z = \omega^{T} X + b$$

$$= n p \cdot dot (\omega \cdot T \cdot X) + b$$

$$A = \epsilon (Z)$$

$$A = \epsilon (Z)$$

$$A = \Delta - Y$$

$$A$$



Basics of Neural Network Programming

Broadcasting in Python

Broadcasting example

Calories from Carbs, Proteins, Fats in 100g of different foods:

Apples Beef Eggs Potatoes

Carb
$$56.0$$
 0.0 4.4 68.0

Protein 1.2 104.0 52.0 8.0

Fat 1.8 135.0 99.0 0.9 (3,4)

Squal Section from Cab, Poten, Fort. Can you do the arphint for-loop?

Cal = A.sum(axis = 0)

percentage = $100*A/(cal Abstrace(1.6))$

Broadcasting example

$$\begin{bmatrix} 1 \\ 2 \\ 3 \\ 4 \end{bmatrix} + \begin{bmatrix} 100 \\ 100 \\ 100 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix} + \begin{bmatrix} 100 & 200 & 300 \\ 100 & 200 & 300 \end{bmatrix}$$

$$(m,n) \quad (2,3)$$

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix} + \begin{bmatrix} 100 & 100 & 100 \\ 200 & 200 \end{bmatrix} = \begin{bmatrix} (m,n) & 2 & 100 \\ (m,n) & 2 & 100 \end{bmatrix}$$

General Principle

$$(m, n)$$
 $\frac{t}{x}$ (n, i) m (m, n) $($

Mathab/Octave: bsxfun



Basics of Neural Network Programming

Explanation of logistic regression cost function (Optional)

Logistic regression cost function

Logistic regression cost function

If
$$y = 1$$
: $p(y|x) = \hat{y}$

If $y = 0$: $p(y|x) = 1 - \hat{y}$

$$p(y|x) = \hat{y} \cdot (1 - \hat{y})$$

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Cost on *m* examples

log
$$p(lolods)$$
 in troops set) = log $\prod_{i=1}^{m} p(y^{(i)}|\chi^{(i)})$

log $p(----) = \sum_{i=1}^{m} log p(y^{(i)}|\chi^{(i)})$

Movimum likelihood setiment

$$- \chi(y^{(i)}, y^{(i)})$$

$$= -\sum_{i=1}^{m} \chi(y^{(i)}, y^{(i)})$$

(ost: $J(w, b) = \frac{1}{m} \sum_{i=1}^{m} \chi(y^{(i)}, y^{(i)})$

(minimize)