## 1 Results

## 1.1 $2 \times 2$ lattice, analytical expressoins

If we scale the value of  $\beta$  from  $1/k_BT$  to 1/J (Scaling factor  $k_BT/J$ ) in the analytical expression from section ??, we will get a good benchmark for computer computations to come. These values are listed in table 1 below.

Mean energy, $\langle E \rangle$ :	-7.9839J
Mean absolute magnetization, $\langle  \mathcal{M}  \rangle$ :	3.9893
Specific heat capacity, $C_V$ :	0.0165
Susceptibility, $\chi$ :	0.0160

Table 1: Material characteristics benchmark for a  $2\times 2$  lattice No. of MC-cycles before reaching good results: