

1 Introduction

Development in methods for solving integrals has been important in order to solve problems with a increasing degree of complexety. Guassian quadrature is a good example which is a method first developed by Jacobi in 1676. The first version would produce exact results for algebraic polynomials of negree $n-1$ or less. The "new" Guassian version has a significant increase in accuaracy with exact results for polynomials of degree $2n-1$ or less due to free choise of weights.

KILDE: https://www.jstor.org/stable/24898684?seq=2metadata_infoabccontents

Gauss-Legendre and Gauss-Laguerre are two Guassian quadrature which, togheter with the well known Monte Carlo method, will be compared in acuaracy and speed for a multidimensional integral for a Helium atom.

The main idea of Gaussian quadrature is to integrate over a set of points x_i not equally spaced with weights w_i . A part of the job is to find these points and weights(Program:Gauleg and Gauss Legendre). The weights are found throug ortogonal polynomials a set interval. The points x_i are chosen in a optimal sense and lie in the interval.

Some theory is first presented with a following discussion of the three methodes mentioned above.