

# 1 Results

## 1.1 $2 \times 2$ lattice, analytical expressions

If we scale the value of  $\beta$  from  $1/k_B T$  to  $1/J$  (Scaling factor  $k_B T/J$ ) in the analytical expression from section ??, we will get a good benchmark for computer computations to come. These values are listed in table 1 below. Note that all values are divided by four, since we want the values per bond, and not for the entire lattice.

Mean energy, $\langle E \rangle$	-1.9960
Mean absolute magnetization, $\langle  \mathcal{M}  \rangle$	0.9987
Specific heat capacity, $C_V$	0.0321
Susceptibility, $\chi$	3.9933

Table 1: Benchmark for material characteristics per bond for a  $2 \times 2$  lattice

## 1.2 Ising model: simulation over temperature

We ran the program for different amounts of Monte Carlo cycles and plotted the error (analytical – simulated) in figure 9 below. Using  $10^7$  Monte Carlo cycles, we seem to be getting pretty accurate results.

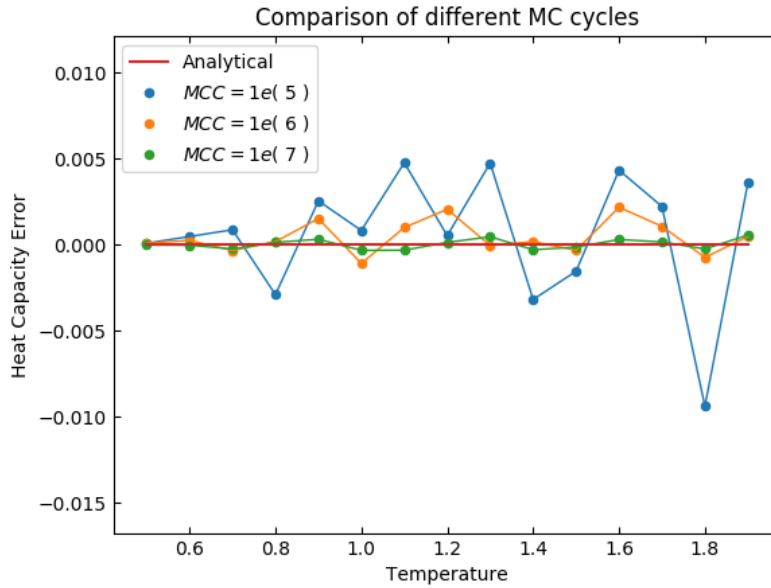


Figure 1: Shows the accuracy of different amount of MC cycles over temperature.

### 1.3 $20 \times 20$ lattice

$T = 1.0$

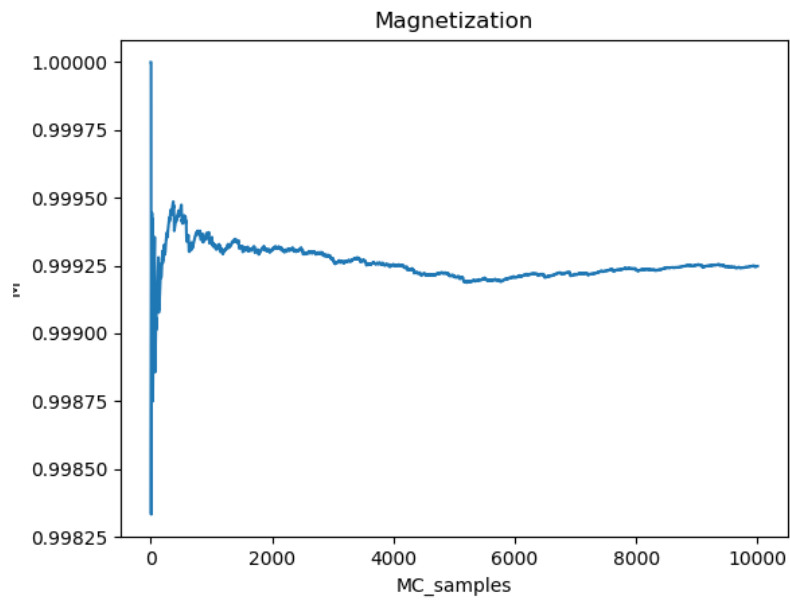


Figure 2: Shows the computed value for the mean magnetization, with ordered initialization, against the number of MC cycles. The scaled temperature is  $T = 1.0$

**Ordered spin orientation**

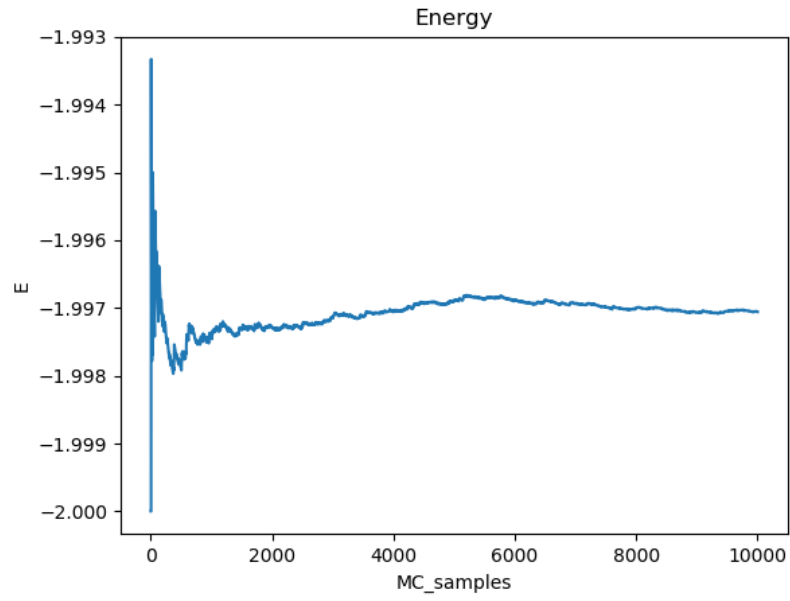


Figure 3: Shows the computed value for the mean magnetization, with ordered initialization, against the number of MC cycles. The scaled temperature is  $T = 1.0$

### Random spin orientation

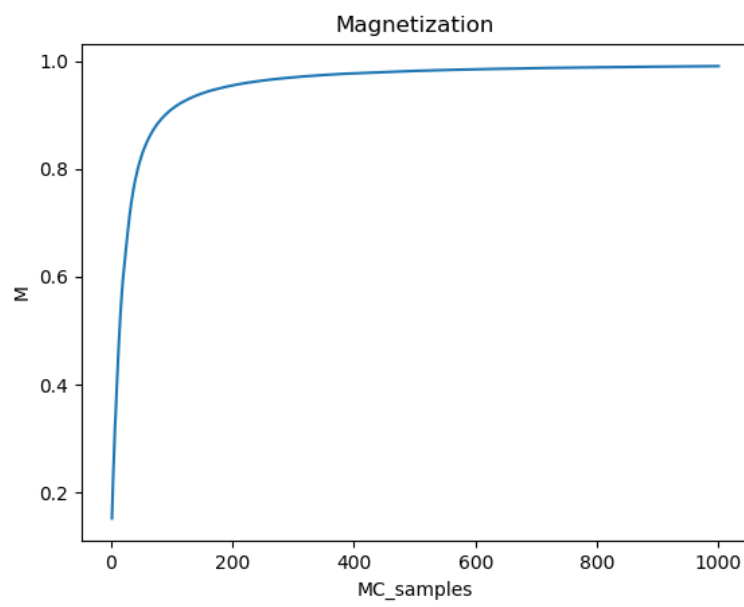


Figure 4: Shows the computed value for the mean magnetization, with random initialization, against the number of MC cycles. The scaled temperature is  $T = 1.0$

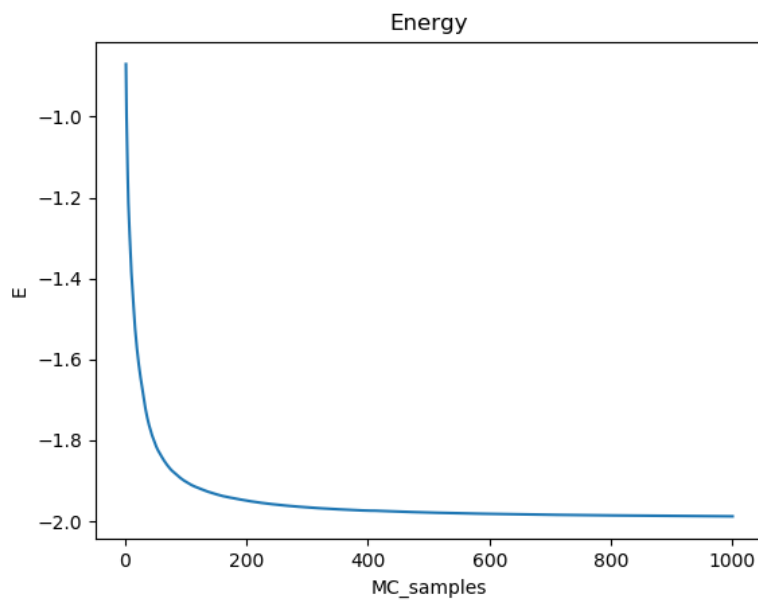


Figure 5: Shows the computed value for the mean magnetization, with random initialization, against the number of MC cycles. The scaled temperature is  $T = 1.0$

Likevekt ved:

$$T = 2.4$$

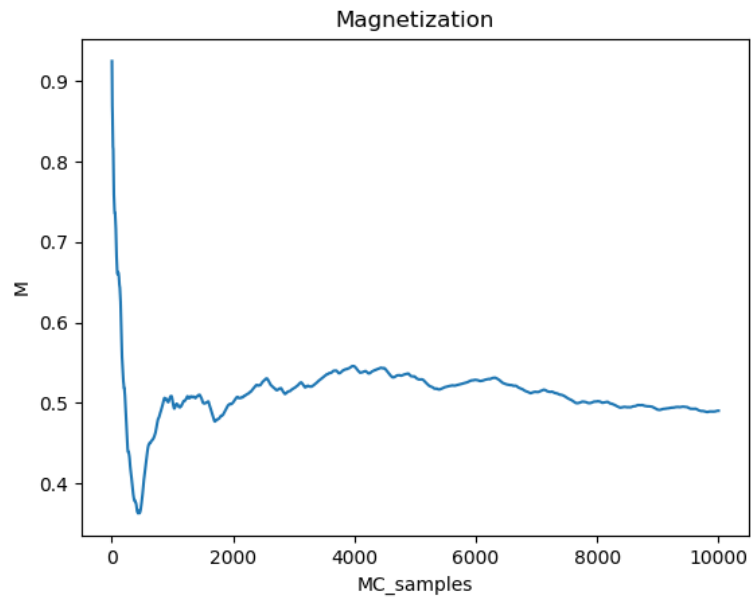


Figure 6: Shows the computed value for the mean magnetization, with ordered initialization, against the number of MC cycles. The scaled temperature is  $T = 2.4$

**Ordered spin orientation**

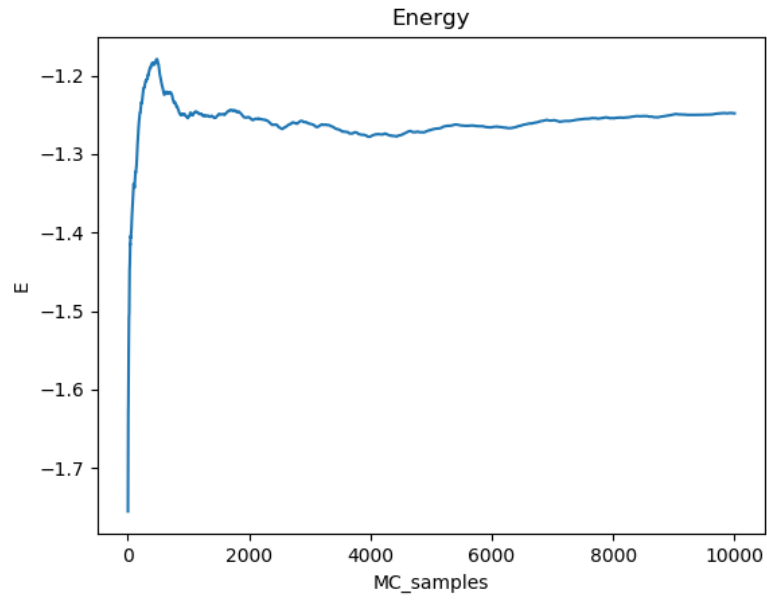


Figure 7: Shows the computed value for the mean magnetization, with ordered initialization, against the number of MC cycles. The scaled temperature is  $T = 2.4$

#### Random spin orientation

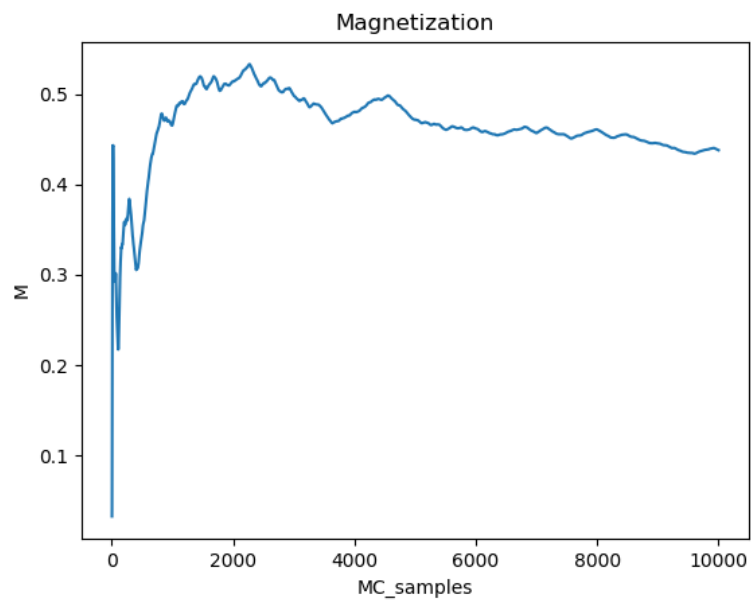


Figure 8: Shows the computed value for the mean magnetization, with random initialization, against the number of MC cycles. The scaled temperature is  $T = 2.4$



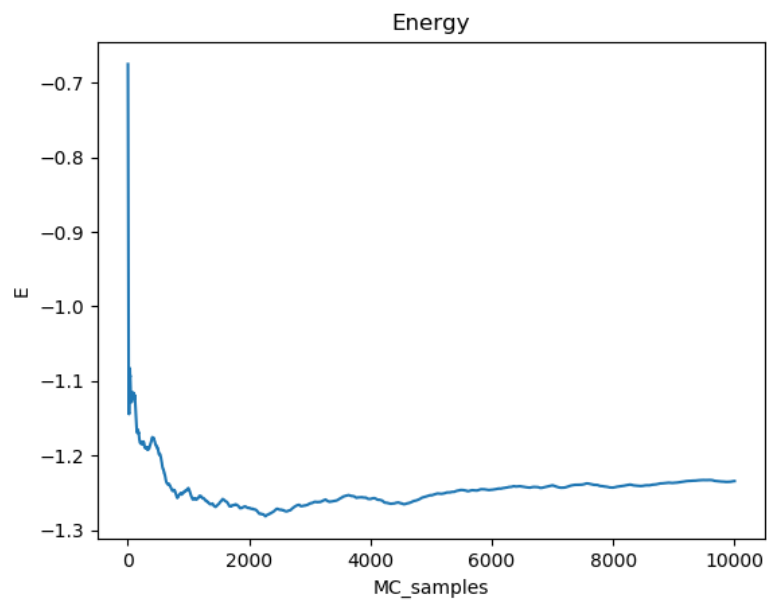


Figure 9: Shows the computed value for the mean magnetization, with random initialization, against the number of MC cycles. The scaled temperature is  $T = 2.4$

Antall aksepterte spinn totalt etter et gitt antall mcs(100k maks): Set start point T = 1 Bilde :*accepted<sub>s</sub>pinn<sub>T</sub>1<sub>mcs<sub>c</sub>umsum(y)</sub><sub>log10.png</sub>Stabiliserersegvedmcd = 1E3.5(allespinnblirheretterakseptert)*

T = 2.4 Bilde: *accepted<sub>s</sub>pinn<sub>T</sub>2<sub>mcs<sub>c</sub>umsum(y)</sub><sub>log10.png</sub>Stabiliserersegvedmcd = 1E3.5, mendetermangefleresomblirakseptert(Seyaksen)*

Random start point: T = 1: Bilde: *accepted<sub>s</sub>pins<sub>T</sub>1<sub>random<sub>c</sub>umsum(y)</sub><sub>mcs<sub>log10.png</sub>T = 2.4Bilde : accepted<sub>s</sub>pins<sub>T</sub>2<sub>random<sub>c</sub>umsum(y)</sub><sub>mcs<sub>log10.png</sub></sub></sub>*

Temperaturavhengighet(skall vi lage plot her også- eller holder det med kommentar i resultater?): Økt temperatur gjør at mange flere spinn aksepteres ved lavere antall mcs dvs tidligere.(sjekk prosenten på y akse) Ved random vs ikke random: omtrent like mange som aksepteres, men i random så aksepteres flere spinn ved lavere mcs. Ved T1 random får man en liten økning ved 1E1.5, mens hos T1 set startpnt så før vi ikke en økning i aksepterte spinn før ved 1E3.5

For T2 så får vi økningen på samme sted. 1E4 på både random og satt startpunkt.