Principle of Locality

- Programs access a small proportion of their address space at any time
- Temporal locality
  - Items accessed recently are likely to be accessed again soon
  - e.g., instructions in a loop, induction variables
- Spatial locality
  - Items near those accessed recently are likely to be accessed soon
  - E.g., sequential instruction access, array data

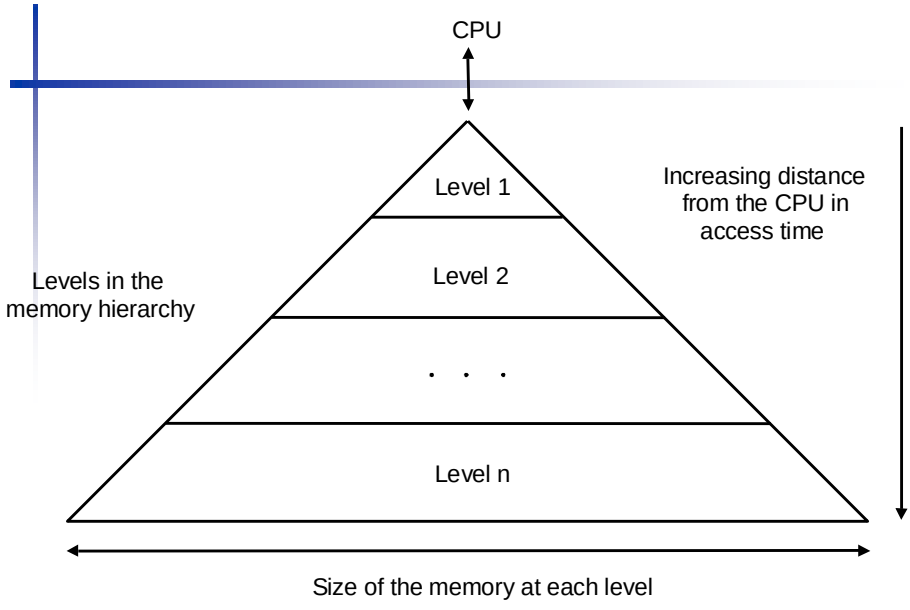
Taking Advantage of Locality

- Memory hierarchy
- Store everything on disk
- Copy recently accessed (and nearby) items from disk to smaller DRAM memory
  - Main memory
- Copy more recently accessed (and nearby) items from DRAM to smaller SRAM memory
  - Cache memory attached to CPU

Memory Hierarchy

The general idea is to build a hierarchy:

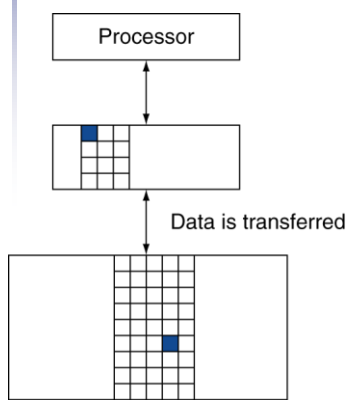
- at the top is a small, fast memory that is *close* to the processor.
- in the middle are larger, slower memories.
- At the bottom is massive memory with very slow access time.



Cache and Main Memory

- For now we will focus on a 2 level hierarchy:
  - cache (small, fast memory directly connected to the processor).
  - main memory (large, slow memory at level 2 in the hierarchy).

Memory Hierarchy Levels



- Block (aka line): unit of copying
  - May be multiple words
- If accessed data is present in upper level
  - Hit: access satisfied by upper level
    - Hit ratio: hits/accesses
- If accessed data is absent
  - Miss: block copied from lower level
    - Time taken: miss penalty
    - Miss ratio: misses/accesses = 1 – hit ratio
  - Then accessed data supplied from upper level

Terminology

- *hit*: when the memory location accessed by the processor is in the cache (upper level).
- *miss*: when the memory location accessed by the process is not in the cache.
- *block*: the minimum unit of information transferred between the cache and the main memory. Typically measured in bytes or words.

Terminology (cont.)

- *hit rate*: the ratio of *hits* to total memory accesses.
- *miss rate*: 1 – *hit rate*
- *hit time*: the time to access an element that is in the cache:
  - time to find out if it's in the cache.
  - time to transfer from cache to processor.

Terminology (cont.)

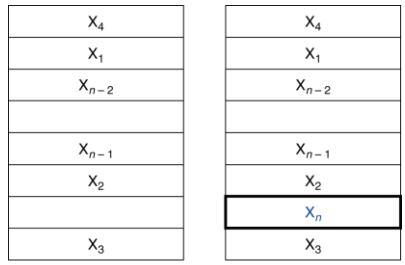
- *miss penalty*: the time to replace a block in the cache with a block from main memory and to deliver the element to the processor.
- *hit time* is small compared to *miss penalty* (otherwise we wouldn't bother with a memory hierarchy!)

Simple Cache Model

- Assume that the processor accesses memory one word at a time.
- A *block* consists of one word.
- When a word is referenced and is not in the cache, it is put in the cache (copied from main memory).

Cache Memory

- Cache memory
  - The level of the memory hierarchy closest to the CPU
- Given accesses $X_1, \ldots, X_{n-1}, X_n$

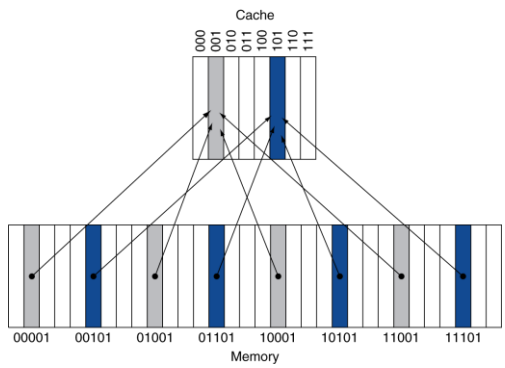


a. Before the reference to X_n b. After the reference to X_n

- How do we know if the data is present?
- Where do we look?

Direct Mapped Cache

- Location determined by address
- Direct mapped: only one choice
  - (Block address) modulo (#Blocks in cache)



- #Blocks is a power of 2
- Use low-order address bits

Tags and Valid Bits

- How do we know which particular block is stored in a cache location?
  - Store block address as well as the data
  - Actually, only need the high-order bits
  - Called the tag
- What if there is no data in a location?
  - Valid bit: 1 = present, 0 = not present
  - Initially 0

Pop Quiz

- In order to determine which block is cached, we need to compare:

- A: tag
- B: valid bit
- C: data
- D: A + B
- E: B + C

Cache Example

- 8-blocks, 1 word/block, direct mapped
- Initial state

Index	V	Tag	Data
000	N		
001	N		
010	N		
011	N		
100	N		
101	N		
110	N		
111	N		

Cache Example

Word addr	Binary addr	Hit/miss	Cache block
22	10 110	Miss	110

Index	V	Tag	Data
000	N		
001	N		
010	N		
011	N		
100	N		
101	N		
110	Y	10	Mem[10110]
111	N		

Cache Example

Word addr	Binary addr	Hit/miss	Cache block
26	11 010	Miss	010

Index	V	Tag	Data
000	N		
001	N		
010	Y	11	Mem[11010]
011	N		
100	N		
101	N		
110	Y	10	Mem[10110]
111	N		

Cache Example

Word addr	Binary addr	Hit/miss	Cache block
22	10 110	Hit	110
26	11 010	Hit	010

Index	V	Tag	Data
000	N		
001	N		
010	Y	11	Mem[11010]
011	N		
100	N		
101	N		
110	Y	10	Mem[10110]
111	N		

Cache Example

Word addr	Binary addr	Hit/miss	Cache block
16	10 000	Miss	000
3	00 011	Miss	011
16	10 000	Hit	000

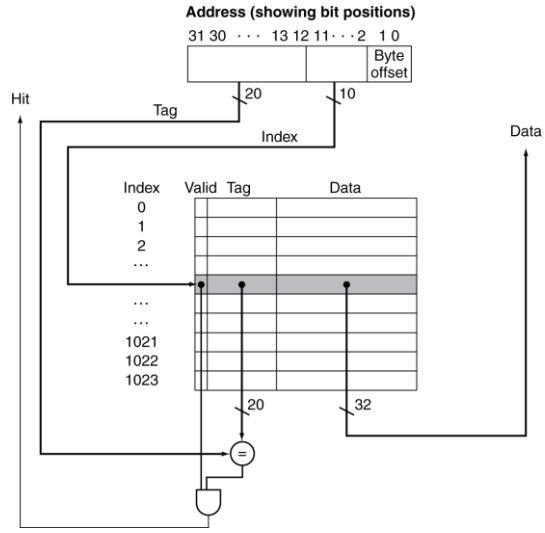
Index	V	Tag	Data
000	Y	10	Mem[10000]
001	N		
010	Y	11	Mem[11010]
011	Y	00	Mem[00011]
100	N		
101	N		
110	Y	10	Mem[10110]
111	N		

Cache Example

Word addr	Binary addr	Hit/miss	Cache block
18	10 010	Miss	010

Index	V	Tag	Data
000	Y	10	Mem[10000]
001	N		
010	Y	10	Mem[10010]
011	Y	00	Mem[00011]
100	N		
101	N		
110	Y	10	Mem[10110]
111	N		

Address Subdivision



Pop Quiz

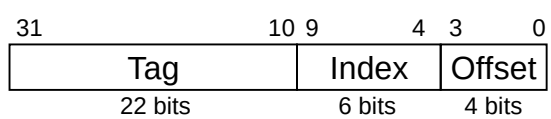
- Given the following:
  - 32 bit addresses (2^{32} byte memory, 2^{30} words)
  - 64 KB cache (16K words), each slot holds 1 word
  - Direct mapped cache
- How many bits are needed for each tag?
- A: 18 B: 16
- C: 14 D: 8

Answer

- Memory has 2^{30} words
- Cache has 16K = 2^{14} slots (words)
- Each cache slot can hold any one of 2^{30} / 2^{14} = 2^{16} memory locations so the tag must be 16 bits

Example: Larger Block Size

- 64 blocks, 16 bytes/block
  - To what block number does address 1200 map?
- Block address = $\lfloor 1200/16 \rfloor$ = 75
- Block number = 75 modulo 64 = 11



Block Size Considerations

- Larger blocks should reduce miss rate
  - Due to spatial locality
- But in a fixed-sized cache
  - Larger blocks ⇒ fewer of them
    - More competition ⇒ increased miss rate
  - Larger blocks ⇒ pollution
- Larger miss penalty
  - Can override benefit of reduced miss rate
  - Early restart and critical-word-first can help

Cache Misses

- On cache hit, CPU proceeds normally
- On cache miss
  - Stall the CPU pipeline
  - Fetch block from next level of hierarchy
  - Instruction cache miss
    - Restart instruction fetch
  - Data cache miss
    - Complete data access

Write-Through

- On data-write hit, could just update the block in cache
  - But then cache and memory would be inconsistent
- Write through: also update memory
- But makes writes take longer
  - e.g., if base CPI = 1, 10% of instructions are stores, write to memory takes 100 cycles
    - Effective CPI = 1 + 0.1×100 = 11
- Solution: write buffer
  - Holds data waiting to be written to memory
  - CPU continues immediately
    - Only stalls on write if write buffer is already full

Write-Back

- Alternative: On data-write hit, just update the block in cache
  - Keep track of whether each block is dirty
- When a dirty block is replaced
  - Write it back to memory
  - Can use a write buffer to allow replacing block to be read first

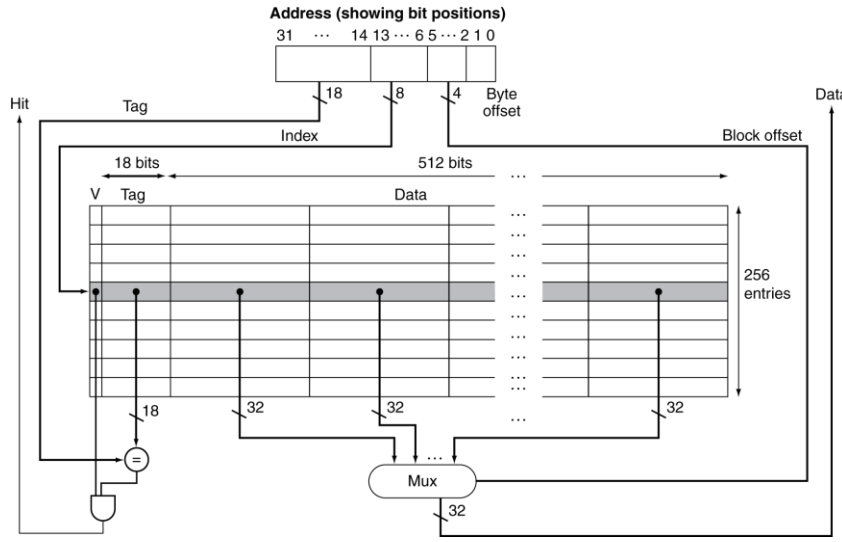
Write Allocation

- What should happen on a write miss?
- Alternatives for write-through
  - Allocate on miss: fetch the block
  - Write around: don't fetch the block
    - Since programs often write a whole block before reading it (e.g., initialization)
- For write-back
  - Usually fetch the block

Example: Intrinsity FastMATH

- Embedded MIPS processor
  - 12-stage pipeline
  - Instruction and data access on each cycle
- Split cache: separate I-cache and D-cache
  - Each 16KB: 256 blocks × 16 words/block
  - D-cache: write-through or write-back
- SPEC2000 miss rates
  - I-cache: 0.4%
  - D-cache: 11.4%
  - Weighted average: 3.2%

Example: Intrinsity FastMATH



Main Memory Supporting Caches

- Use DRAMs for main memory
  - Fixed width (e.g., 1 word)
  - Connected by fixed-width clocked bus
    - Bus clock is typically slower than CPU clock
- Example cache block read
  - 1 bus cycle for address transfer
  - 15 bus cycles per DRAM access
  - 1 bus cycle per data transfer
- For 4-word block, 1-word-wide DRAM
  - Miss penalty = 1 + 4×15 + 4×1 = 65 bus cycles
  - Bandwidth = 16 bytes / 65 cycles = 0.25 B/cycle