Mini-Course 2, Module 1 Monte Carlo Methods for Prediction & Control

CMPUT 365 Fall 2021

October 4, 2021

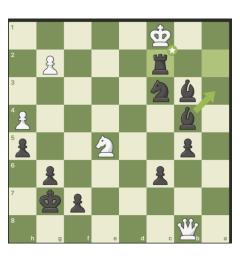
- Friday (8th) at noon: Graded quiz DUE
 - Don't forget Lab on Wednesday! Don't use up all your attempts before getting help!
- In Lab Andy will also review solution to last week's DP notebook
- Any questions about course admin?

Planning vs learning from interaction

- Recall: the universe consists of you, a chess board and pieces AND me (but I only play chess and I never talk, never respond to you)
 - The only thing you can do in life is play chess against me!!
- There are two ways you could figure out how to beat me:
 - Play me over and over and figure out how the game works; figure out my play.
 Trial and error learning (like in a bandit)
 - Dynamic Programming: If you had a book describing the rules & how I play (Adam is part of the environment)

Using Monte Carlo to beat me in chess

- You start with some policy: say move the piece forward closest to my nearest piece
- 1. Play a full game till the end against me:
 - 1.1.Policy/strategy is frozen during the game
 - 1.2. Record the states of the game you see (board) and the rewards
- 2. After the game:
 - 2.1. Update your value function for all the board configurations you saw
 - 2.2. Update your policy/strategy
 - 2.3. Goto 1

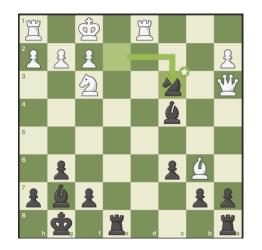












Why is MC a good idea here?

- Model free: Don't need p(s',r|s,a) —the book explaining the rules AND how Adam plays
- It's adaptive:
 - What if Adam changes how he plays?? The book would be wrong!!
 - Then the MC agent can change its policy in response
 - What if Adam disappears and Martha becomes your new opponent? MC can adapt!
- Scalable: if |S| is big, then p(s',r|s,a) is big
- **Focused** on relevant data: DP learns the optimal policy. Even in states Adam never plays in, MC does not! It *specializes to its opponent!*

Monte Carlo is a first principles algorithm

- Consider policy evaluation: estimating v_\pi given some policy \pi
- What is the definition of v_\pi? $v_{\pi}(s) \doteq \mathbb{E}_{\pi}[R_{t+1} + \gamma R_{t+2} + \dots | S_t = s] = \mathbb{E}_{\pi}[G_t | S_t = s]$
- v_\pi is equal to the expected return
 - It's the expected value of the random variable G_t
- How do we estimate an expected value?
 - We can use a sample average!
 - Generate some samples of G_t, then compute the average of them and that's it!

Monte Carlo is just a sample average

- Let's use MC to estimate the value function for the start state S_0:
 - Generate 30 episodes starting in S_0 and taking actions according to \pi
 - Episode 1: S_0, A_0~\pi, R_1, S_1, A_1~\pi, R_2, S_2, ..., R_365, S_365
 Episode 1: S_0, A_0~\pi, R_1, S_1, A_1~\pi, R_2, S_2, ..., R_12 S_12
 ...
 Episode 30: S_0, A_0~\pi, R_1, S_1, A_1~\pi, R_2, S_2, ..., R_204 S_204

Each episode might be a different length & generate different rewards

• Compute:

- $G^{(1)}$ for episode 1 = $R_1 + R_2 + ... + R_365$; lets say its 14.25 ... $G^{(30)}$ for episode 30 = $R_1 + R_2 + ... + R_204$; lets say its 8.45
- Average: $V(S_0) = (G^{(1)} + ... + G^{(30)}) = (14.25 + ... + 8.45) / 30 = 11.14$

The states and rewards observed during the episode will differ from episode to episode

Monte Carlo is just a sample average

- So if we wanted to use MC to estimate the value function for the start state S_0, we
 do the following:
 - Generate; Compute; Average

Review of C2M1 Monte Carlo

Video 1: What is Monte Carlo?

- The term "Monte Carlo" is often used more broadly for any estimation method that relies on repeated random sampling
- In RL, Monte-Carlo methods allow us to estimate values directly from experience: from sequences of states, actions, and rewards.
- Goals:
 - Understand how Monte-Carlo methods can be used to estimate value functions from sample interaction
 - Identify problems that can be solved using Monte-Carlo methods
- If we only have the model -p(s',r|s,a) can we still do Monte Carlo?

Video 2: Using Monte Carlo for Prediction

- Discussed the **Monte Carlo Policy Evaluation algorithm**. We also looked at a **results** of using MC to evaluate one particular policy in Blackjack
- Goals:
 - Use Monte Carlo prediction to estimate the value function for a given policy.
- How could policy evaluation be useful in the real world? Hint: think of an example like Ad Serving online.

Every-Visit Monte Carlo prediction, for estimating V

```
Input: a policy \pi to be evaluated
Initialize:
    V(s) \in \mathbb{R}, arbitrarily, for all s \in S
    Returns(s) \leftarrow an empty list, for all s \in S
Loop forever (for each episode):
    Generate an episode following \pi: S_0, A_0, R_1, S_1, \ldots, S_{T-1}, A_{T-1}, R_T
    G \leftarrow 0
    Loop for each step of episode, t = T - 1, T - 2, ..., 0
         G \leftarrow \gamma G + R_{t+1}
         Append G to Returns(S_t)
         V(S_t) \leftarrow average(Returns(S_t))
```

Video 3: Using Monte Carlo to Estimate Action-Values

- How to estimate q_{π} instead of v_{π} with MC: Q(S_t, A_t) instead of V(S_t). We also tackled the exploration problem in MC.
- Goals:
 - Estimate action-value functions using Monte Carlo and
 - Understand the importance of maintaining exploration in Monte Carlo algorithms
- Why do we need to explore when learning Q(S_t, .)? Hint: imagine policy \pi never chooses action 1 in state S_t?
- Why do we care that Q(S_t, .) is accurate for all actions in state S_t? Hint: What is the goal of RL?

Video 4: Using Monte Carlo Methods for Generalized Policy Iteration

- Our first control Monte Carlo algorithm. Using Exploring Starts to handle the exploration problem
- Goals:
 - Understand how to use Monte Carlo methods to implement a GPI algorithm.
- We can think of Dynamic programming algorithms as doing policy evaluation (recompute the value func) and improvement (greedify policy in all states) as two interacting processes
- We can think of bandit algorithms as doing policy evaluation (updating Q) and improvement (picking a greedy action) on a step by step basis
- Monte Carlo methods are said to perform policy evaluation and policy improvement on a ____ by ____ basis. Fill in the blank. Hint: how often do you update the policy in a MC method?

Video 5: Solving the Blackjack Example

 Using Monte Carlo Control with Exploring Starts to learn an optimal policy in Blackjack!

- Apply Monte Carlo with exploring starts to solve an example MDP.
- What is a major limitation of MC methods for control (the ones we study in this chapter)? **Hint**: think of using **On-policy MC control** to learn to beat Adam in a game of tennis, but Adam sometimes changes his policy during a match.

Video 6: Epsilon-Soft Policies

 Exploring starts is not always the best idea. Think of estimating the value function for a car on a freeway. Turns out we can combine Monte-Carlo control with epsilongreedy

- Understand why Exploring Starts can be problematic in real problems
- Describe an alternative exploration method for Monte Carlo control, using Epsilon-soft policies
- Why would Epsilon-soft also be bad?

Video 7: Why Does Off-Policy Learning Matter?

• Off-policy learning is **another way to handle exploration**. You have one policy called the **behavior policy** in charge of acting, and another policy, called the **target policy** that you want to learn the value function for.

- Understand how off-policy learning can help deal with the exploration problem.
- Examples of target policies
- and examples of behavior policies.
- Do people perform off-policy learning? Can you think of some examples?

Video 8: Importance Sampling

• Statistics review: estimating the expected value of one random variable, with samples drawn according to a different distribution: estimate $E_{\pi}[X]$ with samples drawn according to distribution b, where π != b

- use **importance sampling** to estimate the expected value of a target distribution using samples from a different distribution.
- Imagine we use data generated by a person in a motion capture suite to learn a policy for a robot (say picking up boxes). The person is generating the training data. The distribution b is coming from the person! What is the challenge using importance sampling with this motion capture data?

Video 9: Off-Policy MC Prediction

• Now that we know how to use importance sampling, we can use it with Monte Carlo to estimate v_{π} off-policy. We will do off-policy control later. We keep it simple for now!

- Understand how to use importance sampling to correct returns
- And you will understand how to modify the Monte Carlo prediction algorithm for offpolicy learning.
- The importance sampling correction is: prob_episode_according_to_pi / prob_episode_according_to_b
 When could this number be really huge? Should we worry about that?

Practice Question

. (Exercise 5.5 S&B) Consider an MDP with a single nonterminal state s and a single action that transitions back to s with probability p and transitions to the terminal state with probability 1-p. Let the rewards be +1 on all transitions, and let $\gamma=1$. Suppose you observe one episode that lasts 10 steps, with return of 10. What is the (every-visit) Monte-carlo estimator of the value of the nonterminal state s?

Generate an episode following
$$\pi: S_0, A_0, R_1, S_1, \ldots, S_{T-1}, A_{T-1}, R_T$$
 $G \leftarrow 0$

Loop for each step of episode, t = T - 1, T - 2, ..., 0

$$G \leftarrow \gamma G + R_{t+1}$$

Append G to $Returns(S_t)$

 $V(S_t) \leftarrow average(Returns(S_t))$

- . (Exercise 5.5 S&B) Consider an MDP with a single nonterminal state s and a single action that transitions back to s with probability p and transitions to the terminal state with probability 1-p. Let the rewards be +1 on all transitions, and let $\gamma=1$. Suppose you observe one episode that lasts 10 steps, with return of 10. What is the (every-visit) Monte-carlo estimator of the value of the nonterminal state s?
 - What are the non-terminal states?
 - Just 's'
 - So we only need to compute V(s)
 - Let's look at the trajectory:
 - s, a, 1, s
 - How many times did we visit 's'? 10 times
 - What was the return from the first visit to 's'? 10
 - How many samples of G from 's' do we have? How many returns? 10

. (Exercise 5.5 S&B) Consider an MDP with a single nonterminal state s and a single action that transitions back to s with probability p and transitions to the terminal state with probability 1-p. Let the rewards be +1 on all transitions, and let $\gamma=1$. Suppose you observe one episode that lasts 10 steps, with return of 10. What is the (every-visit) Monte-carlo estimator of the value of the nonterminal state s?

- Let's look at the trajectory:
 s, a, 1
 s, a, 1, s, a, 1
 s, a, 1
 - What was the return from the first visit to 's'? 10
 - What was the return from the second visit to 's'?
 - What was the return from the last visit to 's'?
- Since it is every-visit MC, we simply average the 10 returns

Terminology Review

- In Monte Carlo there are no models, and no bootstrapping
- **Experience**: data generate by the agent taking actions and getting reward feedback for the action it selected.
 - different from what Dynamic Programming does. DP updates the value of states using p(s',r|s,a). DP knows all the rewards in each state via p
- Sample episodes: starting in the start state, run policy pi (select actions according to pi) until termination, recording the states, actions, and rewards observed
- MC methods update the value estimates on an episode-by-episode basis. Must wait until the end of an episode to update the values of each state the agent observed

Terminology Review (2)

- Maintaining exploration: Why we need exploration in MC. Assume pi never takes action b in state S. If we want to estimate q(S,b) we will have no data about the reward you get from state S when pi chooses action b
- Exploring starts: every episode must begin in a random state, and the first action must be randomly selected, even if that action is not what pi would do
 - guarantees we visit every state-action pair
- **Epsilon-soft policies:** a stochastic policy. A policy where each action is selected with at least epsilon probability. (e.g., epsilon-greedy)

Terminology Review (3)

- Off-policy: learning about one policy, while following another
 - e.g., learning the value function for the optimal policy (q*) while following some exploration policy b (i.e. b=random_policy)
- Target policy: the policy you want to learn about. We always call it pi. We either want to learn v_{π} or (q* and pi*)
- **Behavior policy:** the policy used to select actions, to generate the data. We always call it *b*. It is usually an exploratory policy (e.g., epsilon-greedy with respect to Q)
- Importance sampling: a statistical technique for estimating the expected value when the samples used to compute the average don't match the distribution you want.