

# 1 Report

## 1.1 Linear Discriminant Analysis(LDA)

### 1.1.1 fit

In LDA, the parameters we estimate are class priors( $\pi_k$ ), mean( $\mu_k$ ) for each class and covariance matrix( $\Sigma$ ) from the training data.

- **Class Priors( $\pi_k$ )**

$$\pi_k = \frac{N_k}{N} \quad (1)$$

where  $N_k$  is the number of samples in class  $k$ , and  $N$  is the total number of samples.

- **class mean( $\mu_k$ )**

$$\mu_k = \frac{1}{N_k} \sum_{i=1}^{N_k} x_i \quad (2)$$

where  $N_k$  is the number of samples in class  $k$ , and  $x_i$  is the  $i^{\text{th}}$  sample in class  $k$ .

- **Covariance Matrix( $\Sigma$ )**

$$\Sigma = \frac{1}{N} \sum_{i=1}^N (X_i - \mu)(X_i - \mu)^T \quad (3)$$

where  $N$  is the number of samples,  $X_i$  is the  $i^{\text{th}}$  sample, and  $\mu$  is the mean of the samples.

### 1.1.2 predict

We predict of the test data by these estimates and get the accuracy of LDA in RGB and Grayscale versions of dataset.

- Accuracy of test data in RGB : **0.3713**
- Accuracy of test data in Grayscale : **0.2739**

## 1.2 (Quadratic Discriminant Analysis)QDA

### 1.2.1 fit

In QDA, the parameters we estimate are class priors( $\pi_k$ ), mean( $\mu_k$ ) and covariance matrix( $\Sigma_K$ ) for each class from the training data.

- **Class Priors( $\pi_k$ )**

$$\pi_k = \frac{N_k}{N} \quad (4)$$

where  $N_k$  is the number of samples in class  $k$ , and  $N$  is the total number of samples.

- **class mean( $\mu_k$ )**

$$\mu_k = \frac{1}{N_k} \sum_{i=1}^{N_k} x_i \quad (5)$$

where  $N_k$  is the number of samples in class  $k$ , and  $x_i$  is the  $i^{\text{th}}$  sample in class  $k$ .

- **Covariance Matrix( $\Sigma$ )**

$$\Sigma_k = \frac{1}{N_k} \sum_{i=1}^{N_k} (X_i - \mu_k)(X_i - \mu_k)^T \quad (6)$$

where  $N_k$  is the number of samples in class  $k$ ,  $X_i$  is the  $i^{\text{th}}$  sample in class  $k$ , and  $\mu_k$  is the mean of the samples in class  $k$ .

### 1.2.2 predict

We predict of the test data by these estimates and get the accuracy of QDA in RGB and Grayscale versions of dataset.

- Accuracy of test data in RGB : **0.2364**
- Accuracy of test data in Grayscale : **0.2602**

## 1.3 (Gaussian Naive Bayes)GNB

### 1.3.1 fit

In Gaussian Naive Baye, the parameters we estimate are class priors( $\pi_k$ ), mean( $\mu_k$ ) and variance( $\sigma_k^2$ ) for each class from the training data.

- **Class Priors( $\pi_k$ )**

$$\pi_k = \frac{N_k}{N} \quad (7)$$

where  $N_k$  is the number of samples in class  $k$ , and  $N$  is the total number of samples.

- **class mean( $\mu_k$ )**

$$\mu_k = \frac{1}{N_k} \sum_{i=1}^{N_k} x_i \quad (8)$$

where  $N_k$  is the number of samples in class  $k$ , and  $x_i$  is the  $i^{\text{th}}$  sample in class  $k$ .

- **class variance( $\sigma_k^2$ )**

$$\sigma_k^2 = \frac{1}{N_k} \sum_{i=1}^{N_k} (X_i - \mu_k)^2 \quad (9)$$

where  $N_k$  is the number of samples in class  $k$ ,  $X_i$  is the  $i^{\text{th}}$  sample in class  $k$ , and  $\mu_k$  is the mean of the samples in class  $k$ .

### 1.3.2 predict

We predict of the test data by these estimates and get the accuracy of QDA in RGB and Grayscale versions of dataset.

- Accuracy of test data in RGB : **0.2976**
- Accuracy of test data in Grayscale : **0.2662**