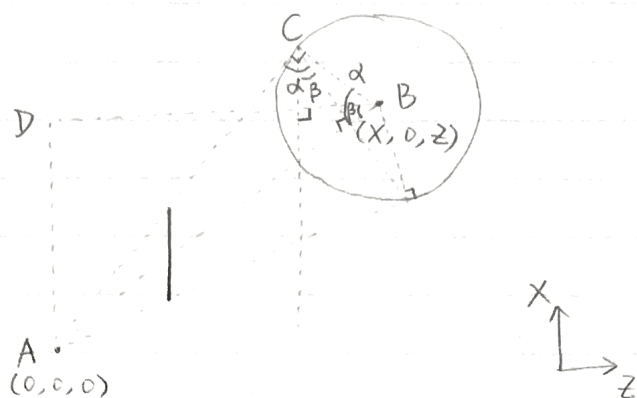


2)



The points on the sphere that relates to the edge of the silhouette form a cone with the origin $(0, 0, 0)$, as shown above

we know that a proper cut on the cone can be an ellipse, with eccentricity calculated by

$$e = \frac{\sin \beta}{\sin \alpha}$$

α and β are defined above in the figure

A, B, C, D are points also defined above

$$\sin \alpha = \frac{AC}{AB} = \frac{\sqrt{x^2 + z^2 - r^2}}{\sqrt{x^2 + z^2}}$$

$$\sin \beta = \frac{AD}{AB} = \frac{x}{\sqrt{x^2 + z^2}}$$

$$\text{then } e = \frac{\sin \beta}{\sin \alpha} = \frac{x}{\sqrt{x^2 + z^2 - r^2}} \quad \text{when } z > r, \text{ ellipse}$$

when $z = r$ or $x \gg z, r$

$e \rightarrow 1$ then it will look like a parabola

when $z < r$, $e > 1$, then it will look like a hyperbola.