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```
In [1]: import numpy as np
         from scipy.linalg import eig
         from scipy.linalg import svd
         def compute_svd(a):
             U, s, Vh = svd(a, full_matrices=False)
             print(a)
             print(U)
             print(s)
             print(Vh)
         A = np.array([[2, -4], [-1, -1]])
         B = np.array([[3, 1], [1, 3]])
         C = np.dot(A, B)
         D = np.dot(B, A)
         c = np.array([[3,1],[1, 3],[2,-4],[-1,-1]])
In [2]: w, vl, vr = eig(C, left=True)
         print(C)
         print(w)
         print(vr)
         print(vl)
         [[ 2 -10]
          \begin{bmatrix} -4 & -4 \end{bmatrix}
         [6.+0.j-8.+0.j]
         [[ 0.92847669  0.70710678]
          [-0.37139068 0.70710678]]
         [[ 0.70710678  0.37139068]
          [-0.70710678 0.92847669]]
In [3]: | w, vl, vr = eig(D, left=True)
         print(D)
         print(w)
         print(vr)
         print(vl)
         [[ 5 -13]
         \begin{bmatrix} -1 & -7 \end{bmatrix}
         [6.+0.j-8.+0.j]
         [[ 0.99705449  0.70710678]
          [-0.0766965
                         0.70710678]]
         [[ 0.70710678  0.0766965 ]
          [-0.70710678 \quad 0.99705449]]
In [4]: | compute_svd(A)
         [[2-4]
          [-1 -1]
         [[ 0.99402894  0.10911677]
          [ 0.10911677 -0.99402894]]
         [ 4.49661478 1.33433712]
         [[ 0.41785681 -0.9085129 ]
          [ 0.9085129  0.41785681]]
```

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In [5]: compute_svd(np.dot(A,A))
         [[8 - 4]
          [-1 \ 5]]
         [[-0.92036286 \quad 0.39106549]
          [ 0.39106549  0.92036286]]
         [ 9.58630798  3.75535608]
         [[-0.80885867
                         0.5880031 ]
          [ 0.5880031
                         0.80885867]]
In [6]: compute_svd(np.dot(A,B))
         [[ 2 -10]
          \begin{bmatrix} -4 & -4 \end{bmatrix}
         [[ 0.9347217
                         0.35538056]
          [ 0.35538056 -0.9347217 ]]
         [ 10.77805077
                          4.45349545]
         [[ 0.04155864 -0.99913607]
          [ 0.99913607  0.04155864]]
In [7]: compute_svd(np.dot(B,A))
         [[ 5 -13]
          \begin{bmatrix} -1 & -7 \end{bmatrix}
         [[ 0.90607303  0.42312134]
          [ 0.42312134 -0.90607303]]
         [ 15.30230699
                          3.13678193]
         [[ 0.26840683 -0.96330565]
          [ 0.96330565  0.26840683]]
In [8]: compute svd(c)
         [[ 3 1]
          [1 3]
          [2 -4]
          [-1 -1]
         [[-0.14395373
                         0.79545124]
          [-0.5586541
                         0.32209809]
          [ 0.79770252  0.4306424 ]
          [ 0.17565196 -0.27938733]]
         [ 5.20411016 3.86228397]
         [[ 0.08248053 -0.99659268]
          [ 0.99659268  0.08248053]]
In [ ]:
```