MATH 2205: Multivariate Calculus Homework 4, due 12:45 Monday, 20 March 2017

You must justify your answers to receive full credit.

Some antiderivatives you may find useful:

$$\int \sec^2 x \, dx = \tan x + C,$$

$$\int \csc^2 x \, dx = -\cot x + C,$$

$$\int \sec x \tan x \, dx = \sec x + C,$$

$$\int \csc x \cot x \, dx = -\csc x + C,$$

$$\int \frac{1}{\sqrt{1 - x^2}} \, dx = \sin^{-1} x + C,$$

$$\int \frac{1}{1 + x^2} \, dx = \tan^{-1} x + C,$$

$$\int \sin^2 x \, dx = \frac{1}{2} (x - \sin x \cos x) + C,$$

$$\int \sin^3 x \, dx = -\cos x + \frac{1}{3} \cos^3 x + C.$$

$$\int \sin^4 x \, dx = \frac{1}{8} (3x - 3\sin x \cos x - 2\sin^3 x \cos x) + C,$$

$$\int \cos^2 x \, dx = \frac{1}{2} (x + \sin x \cos x) + C,$$

$$\int \cos^3 x \, dx = \sin x - \frac{1}{3} \sin^3 x + C.$$

$$\int \cos^4 x \, dx = \frac{1}{8} (3x + 3\sin x \cos x + 2\cos^3 x \sin x) + C.$$

• 6.5: Q9, 12, 15, 22:
$$\int_0^{\pi/2} \frac{\cos x}{(1-\sin x)^{2/3}} dx, \int_0^\infty \frac{x}{1+2x^2} dx, \int_0^{\pi/2} \tan x dx, \int_{-\infty}^\infty e^{-|x|} dx.$$

- 14.3 Q4, 12
- 12.2 Q3, 5, 11, 12
- 12.3 Q11, 36.
- 12.4 Q4 ,5, 17
- 12.6 Q2, 4
- 12.6 Q18, 19.

• 12.5 Q1, 2, 6, 17

The following two questions are to prepare you for the following week's class, and is unrelated to the material from recent classes.

- 1. Let \mathbf{v} be the vector $4\mathbf{i} \mathbf{j}$.
 - a) Calculate the dot product $\mathbf{v} \bullet (3\mathbf{i} + 2\mathbf{j})$.
 - b) Find a vector that is perpendicular to \mathbf{v} .
 - c) Find a unit vector in the same direction as \mathbf{v} .
- 2. Consider the function

$$f(x) = \frac{x^2}{x^2 + 1}$$

- a) Find and classify the critical points of f.
- b) Find the minimum and maximum values of f on the interval [1, 2].
- c) Find the second order Taylor polynomial of f about the point x=2.

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